

# Planning and application of electrical drives (PAED) - Drives for electric vehicles



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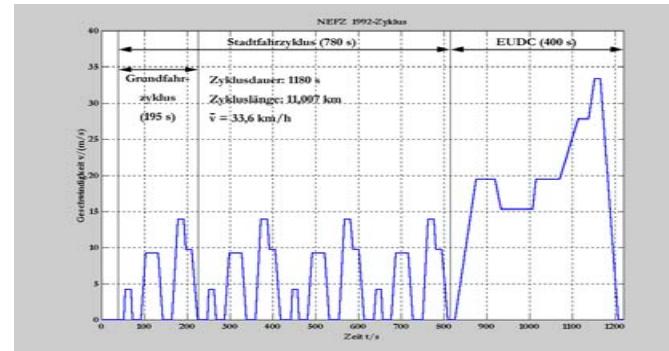
TU DARMSTADT – Basics of Drive Calculations

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Based on literature by M. Ade,  
S. Dewenter, M. Brüggemann  
and P. Morrison



Source: Daimler

# Contents



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- Hybrid vehicles - Overview
- Electric vehicles – Overview
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- Electric vehicles – Simulation vehicle - track
- Electric vehicles – Simulation of the drive components
- Electric vehicles – Examples of simulation



**TESLA Roadster**





## **Hybrid vehicles - Overview**

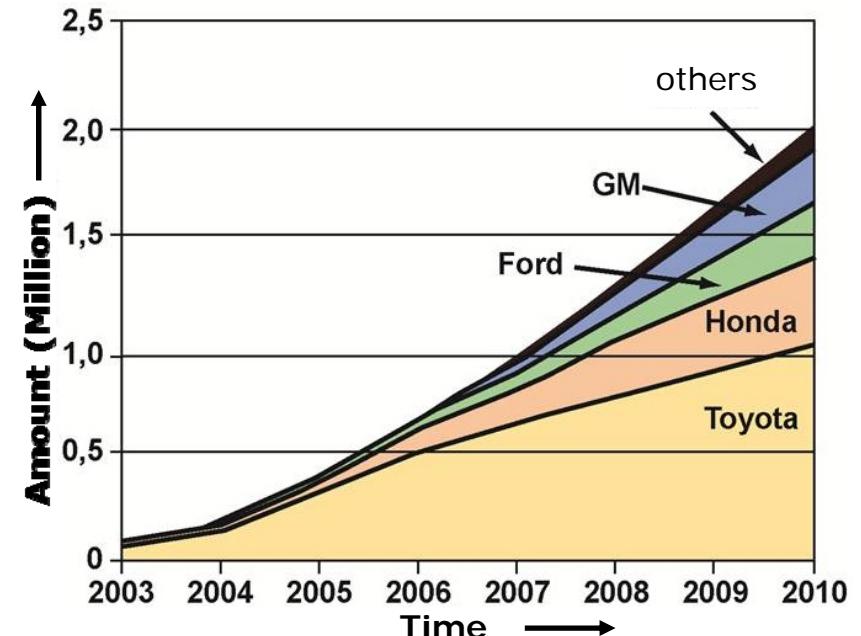
# Motivation for hybrid drives



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## ▪ Market prognosis 2010

- Global production approx. 65 Mio. cars
- Market share HEV approx. 3 % (market segment Mini in FRG 2006 approx. 3 %)
- Share of European brands small
  - Demand for catch up production / sale
  - Further development e.g. by the use of simulation programs



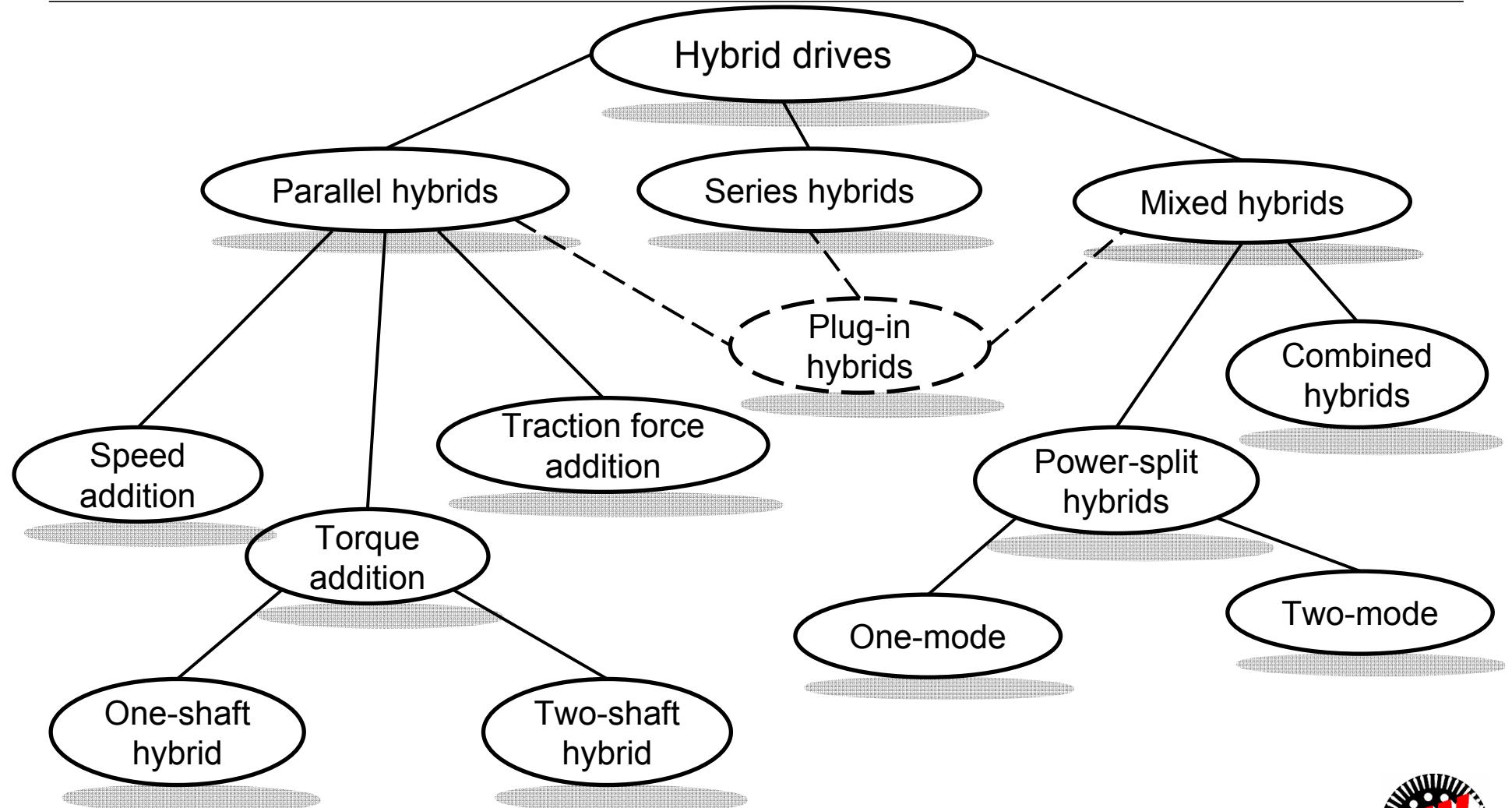
## ▪ Advantages of simulation models

- Build-up of know how / development tools
- Design / tuning / dimensioning of drive train components before manufacturing of prototype
  - Contribution to reduction of development costs

# Possible hybrid topologies



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# Overview hybrid vehicles



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	Micro hybrid	Mild hybrid	Full hybrid
Power range in kW	2-3	10-15	> 15
Voltage in V	12	42	> 100
Motor start/stop	X	X	X
Recuperation		X	X
Boost			X
Purely electric driving			X

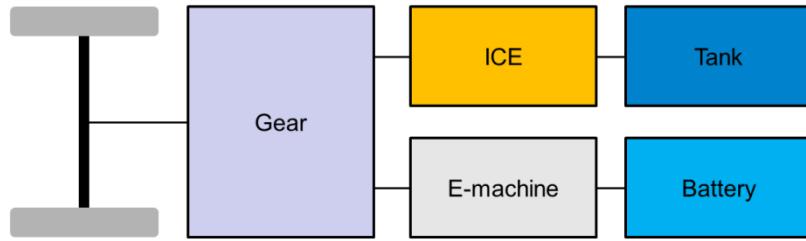


# Overview hybrid vehicles

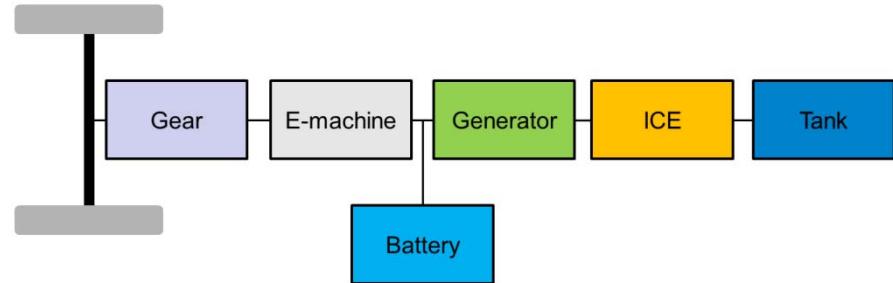


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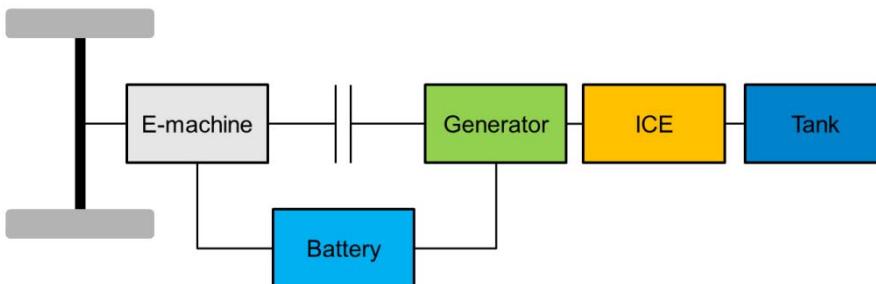
Parallel hybrid



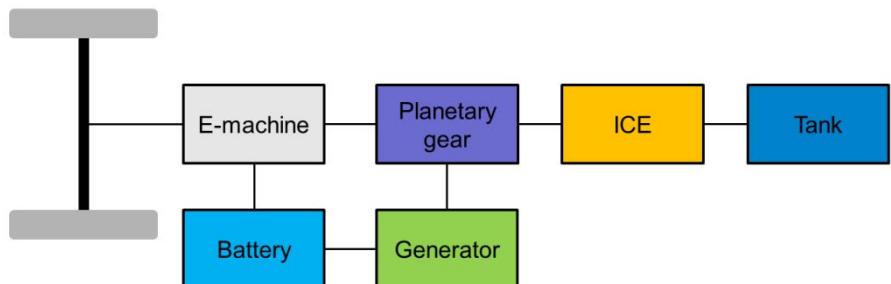
Series hybrid



Combined hybrid



Power split hybrid

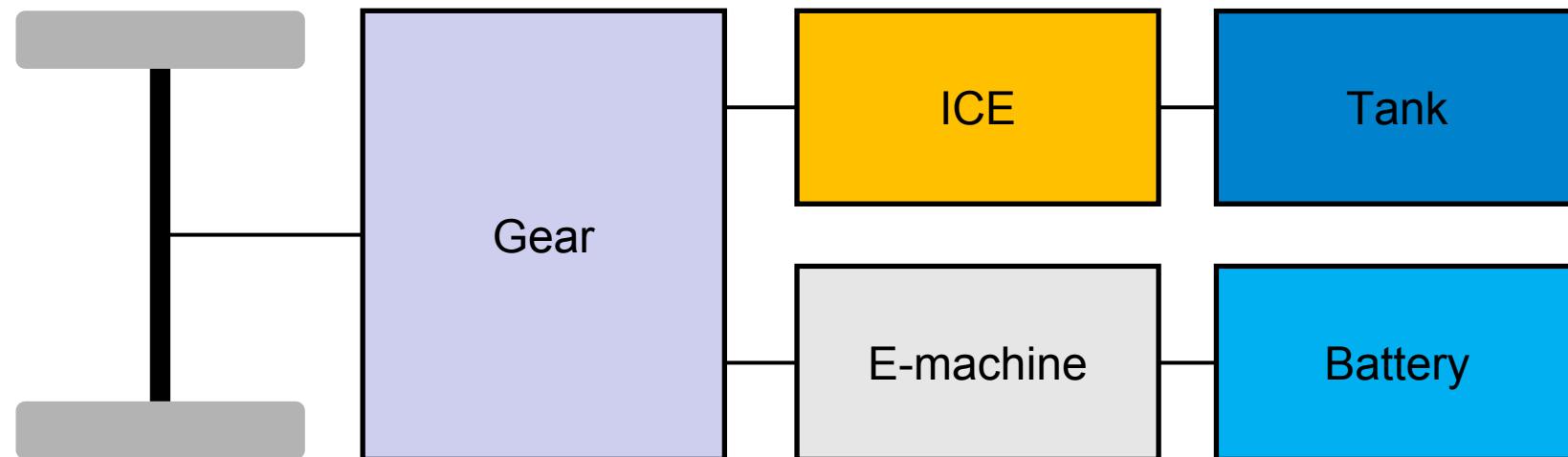


# Parallel hybrid



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## Parallel hybrid drive



# Parallel hybrid

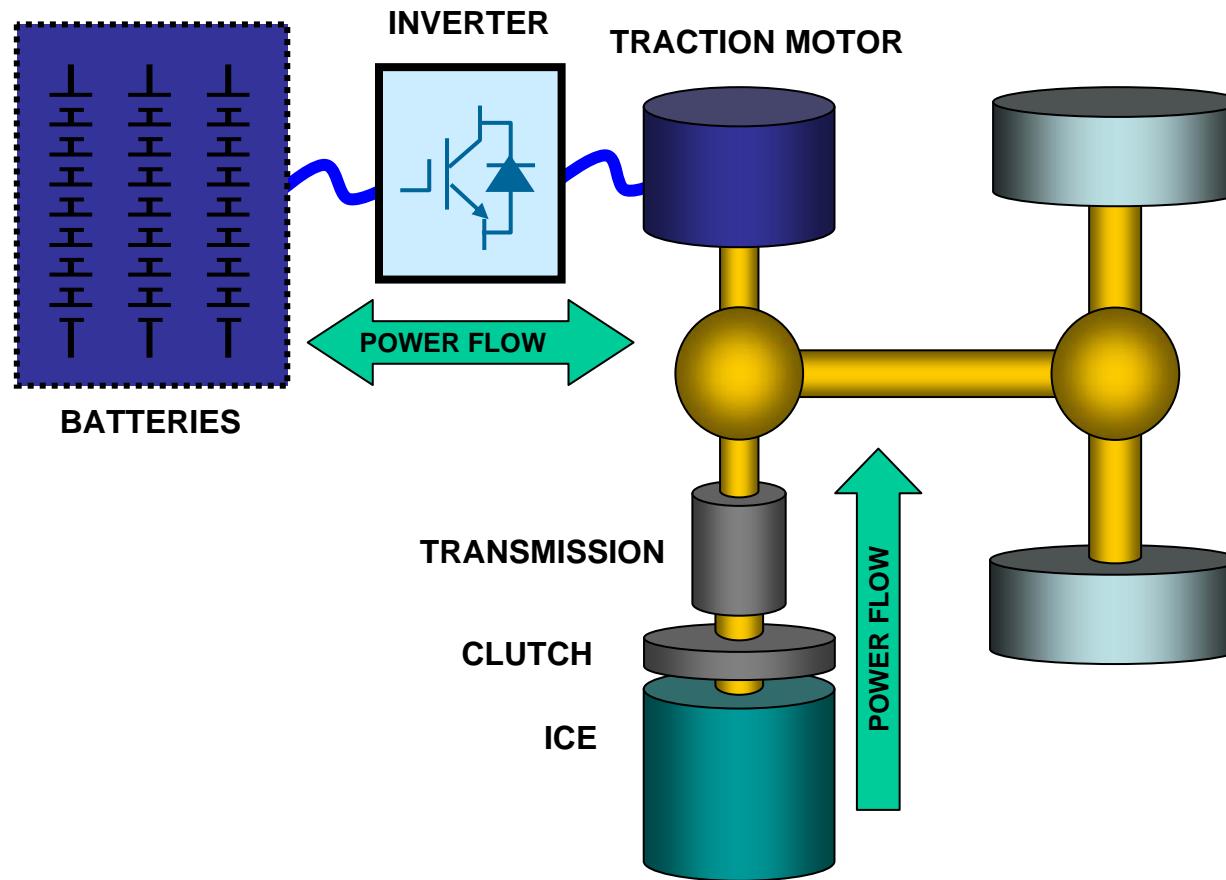
## Different variants of parallel hybrid

- Torque addition:
  - Fixed connection of both drive types  
(e.g. by chain or spur gear)
  - Distinction between one- and two shaft hybrid
- Tractive force addition („*Through-the-road hybrid*“):
  - Special case of torque addition
  - Coupling of both drive types over track
- Rotational speed addition:
  - Connection by planetary gear
  - Fixed torque ratio between drives, therefore free choice of rotational speed

# Parallel hybrid



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Source:

Parker Hannifin

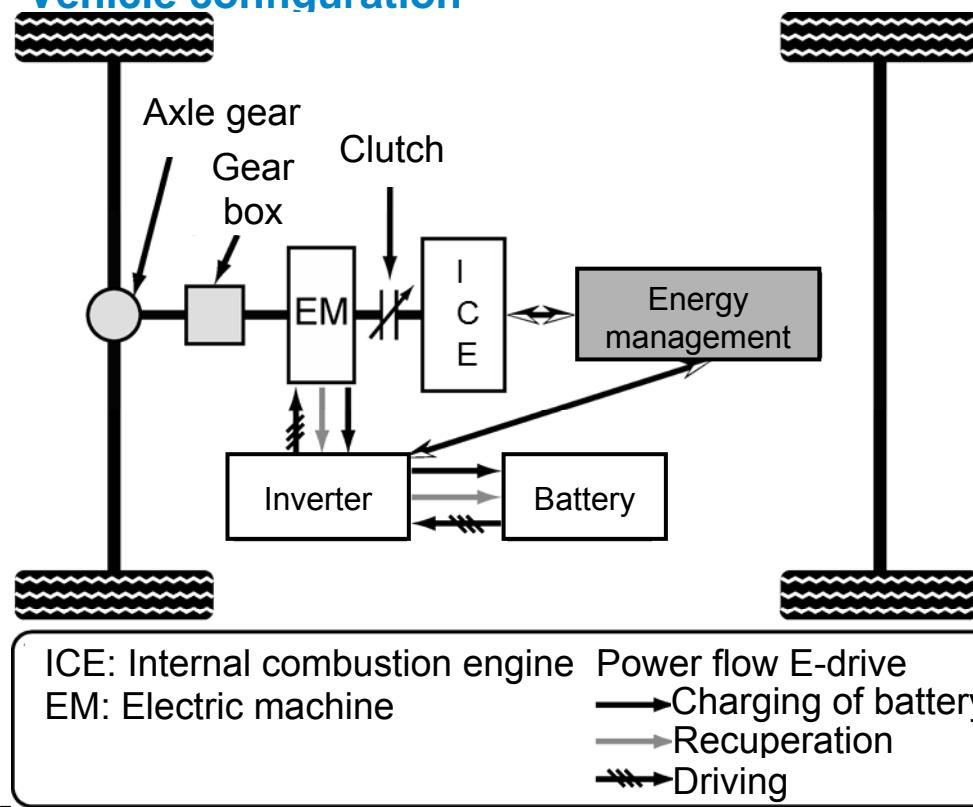
- - - - - Mechanical load sharing - - - - -

# Parallel hybrid



- **Mercedes Benz (MB) E-Class 220 CDI**
  - Vehicle: fictive
  - Electrically supplied ancillary units
  - Max. additional power consumption

- **Vehicle configuration**



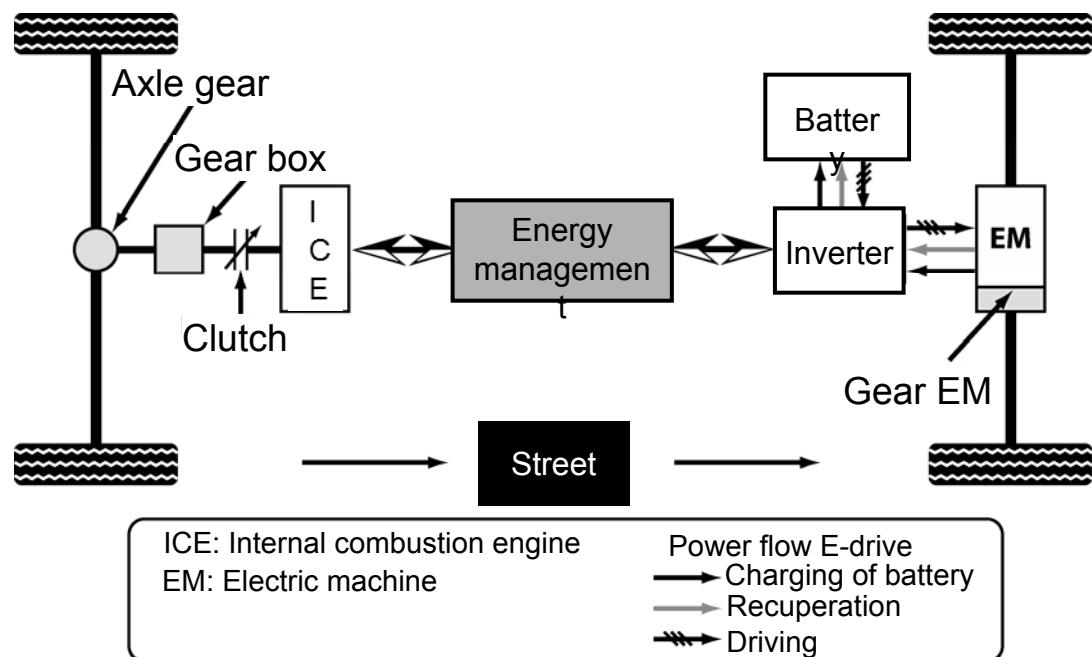
*Example: Vehicle data P-HEV1*

ICE	2,2 l CDI
Cylinders	4
$M_N / P_N$	300 Nm / 105 kW
Gear	Automatic
Transmission ratios gear 1 ... 5	3.95 / 2.42 / 1.49 / 1.00 / 0.83
Axle gear	2,87
Vehicle	MB E Class
$c_w$ -value	0,27
Reference area	~ 2.25 m <sup>2</sup>
Wheels	$r = 0,299$ m
Empty mass	1640 kg
Battery	40 kg
E-Machine	60 kg
Inverter	10 kg
DC/DC-converter	5 kg
Board battery	-10 kg
Alternator	-5 kg
<b>Total weight</b>	<b>1740 kg</b>
<b>→ Additional weight</b>	<b>approx. 100 kg</b>



# Parallel hybrid „Through the road“

- **Mercedes Benz (MB) B-Class**
  - Vehicle: fictive
  - Electrically supplied ancillary units
  - Max. additional power consumption
- **Vehicle configuration**



*Example: Vehicle data P-HEV2*

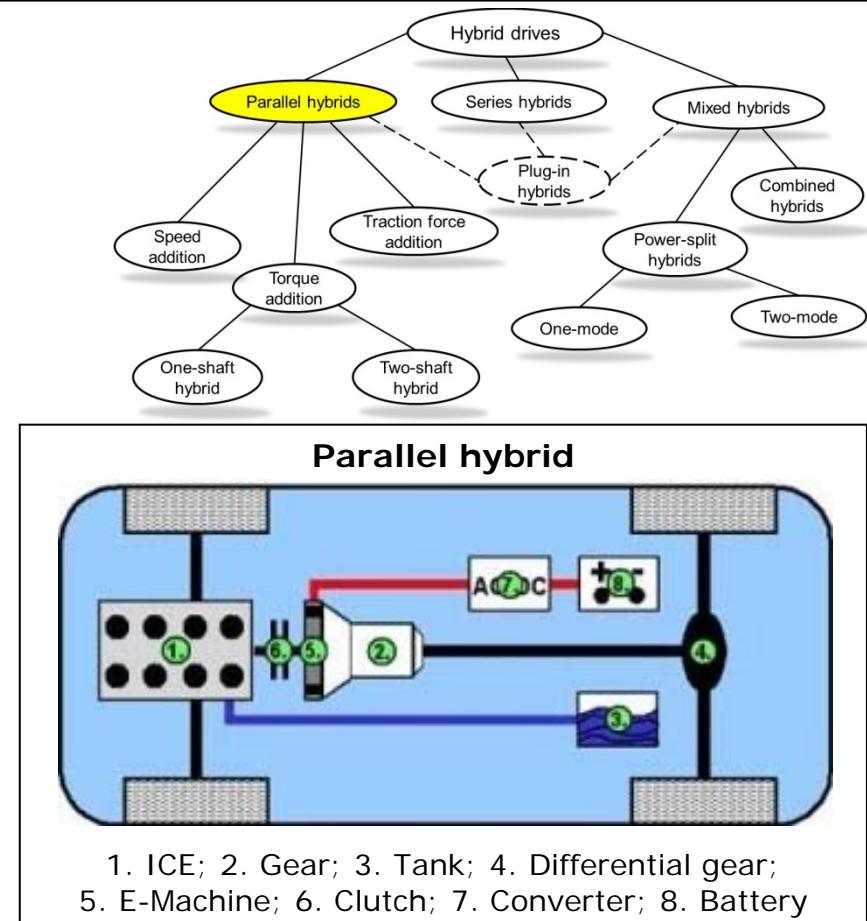
ICE	1,7 l CDI
Zylinders	4
$M_N / P_N$	180 Nm / 67 kW
Gear	Automatic
Transmission ratios gear 1 ... 5	2.72 / 1.69 / 1.12 / 0.79 / 0.65
Axle gear	3,95
Vehicle	MB B Class
$c_w$ -value	0,3
Reference area	~ 2.42 m <sup>2</sup>
Wheels	$r = 0,3205 \text{ m}$
Empty mass	1435 kg
Battery	40 kg
E-Machine	42 kg
Inverter	8.5 kg
DC/DC-converter	5 kg
Board battery	-10 kg
Alternator	-5kg
<b>Total weight</b>	<b>1515 kg</b>
<b>→ Additional weight</b>	
ca. 80 kg	



# Parallel hybrid



- ICE and E-Machine can both drive
- Advantage:
  - Only two machines
  - Part of traction directly by ICE (no „unnecessary“ energy conversion)
  - Further saving potentials by „downsizing“
- Draw backs:
  - ICE - operating points depend on cruise environment
  - More complex energy management



(Source: Hybrid-Autos.info)

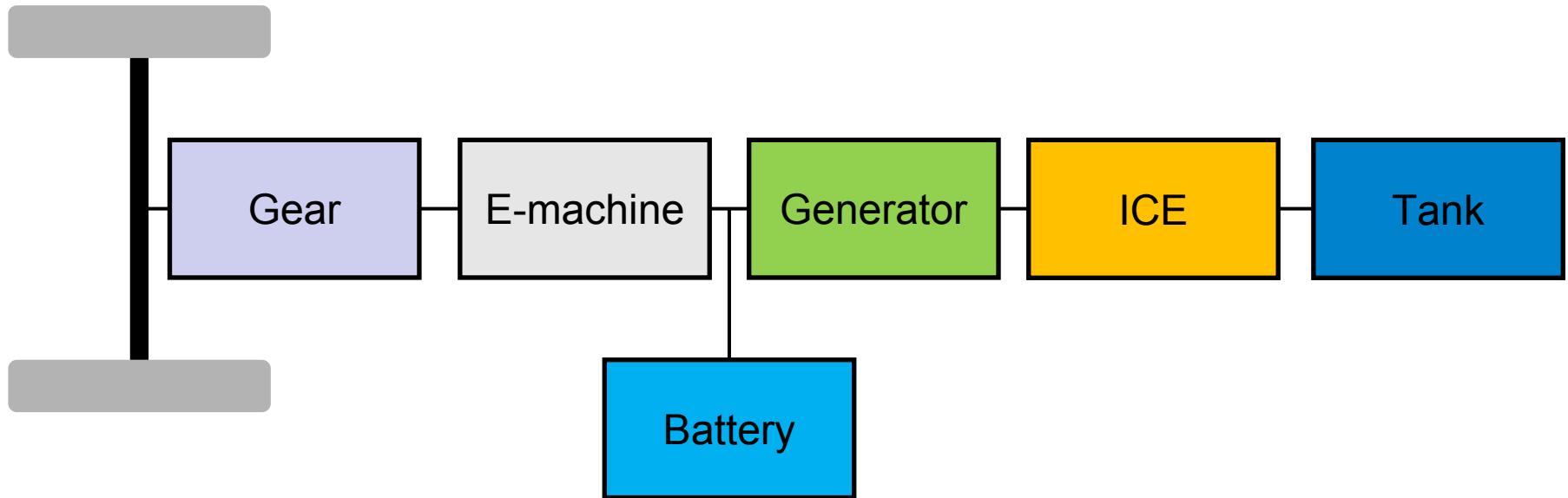


# Series hybrid



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## Series hybrid drive



Example: Diesel-electric city busses: Diesel engine runs in optimal operating point = max. efficiency (e. g. 43%)

E-machines + converter → speed variable!

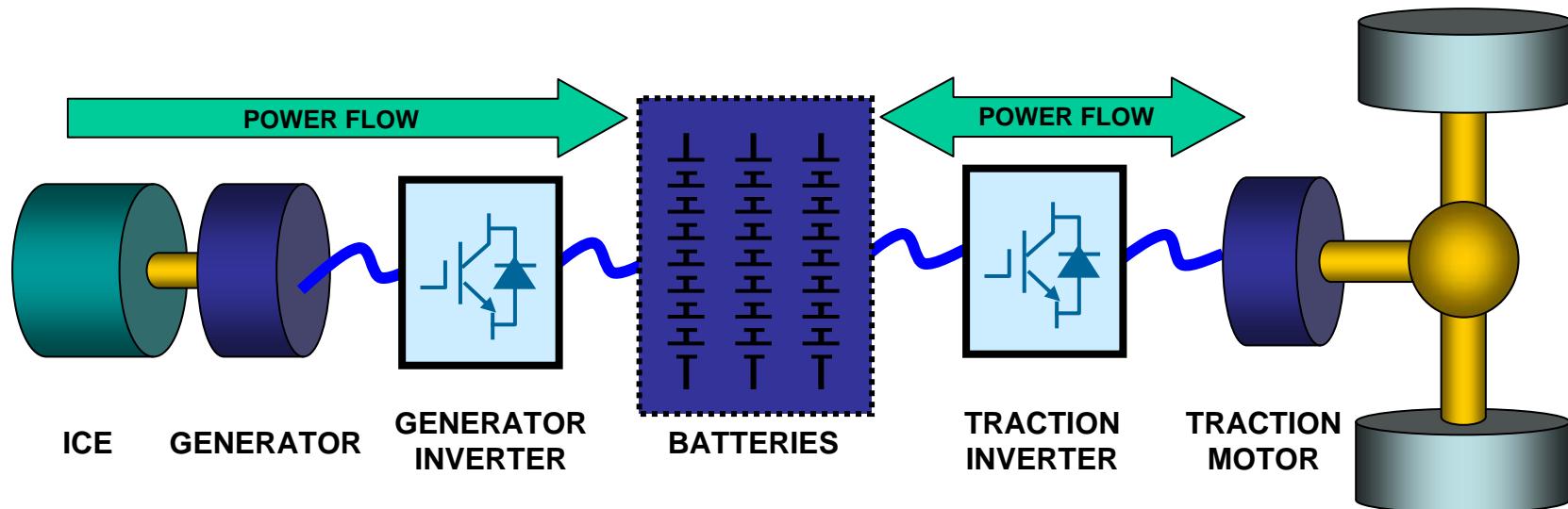
# Series hybrid



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Source:

Parker Hannifin



- - - - No mechanical connection - - - -

# Series hybrid busses



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Electric components:

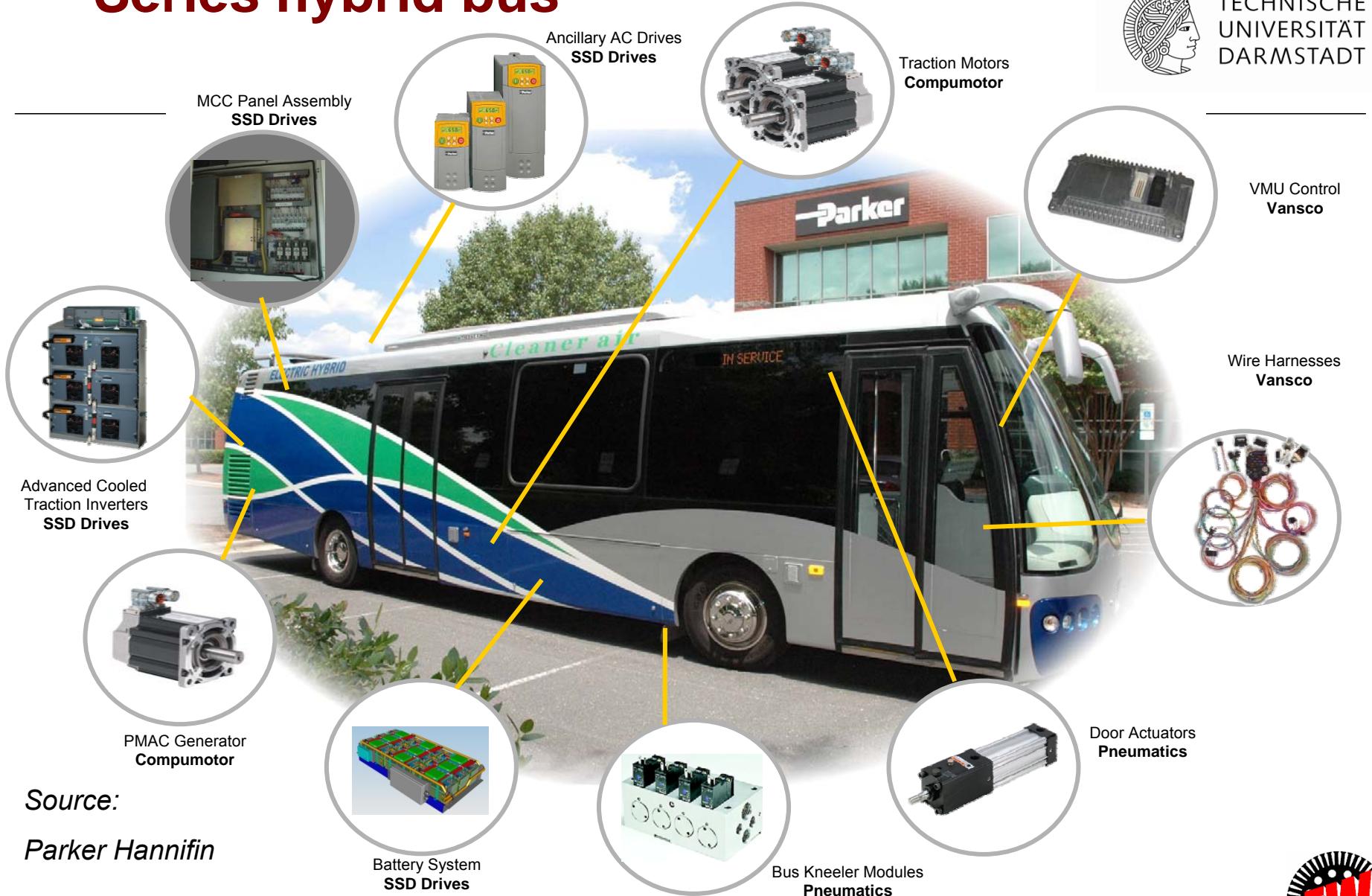
- Control panels
- Traction inverters
- Advanced battery system
- Traction motors
- Generators (PM AC)
- Charging inverters



Source:

*Parker Hannifin*

# Series hybrid bus



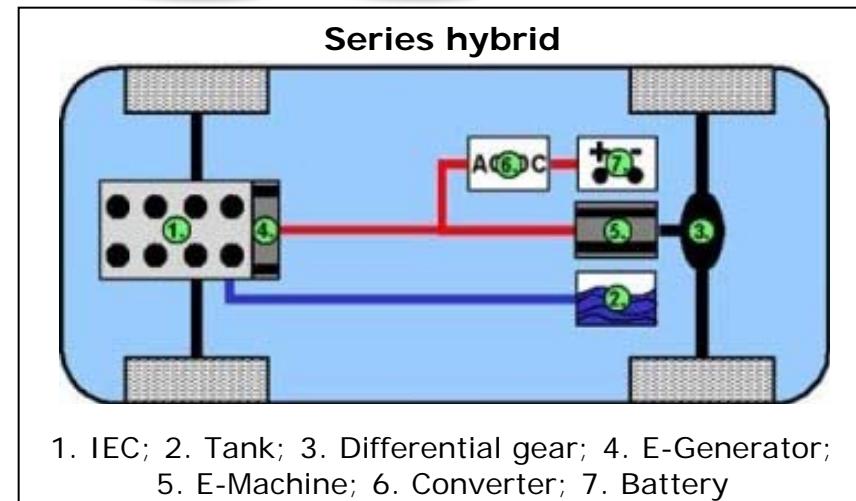
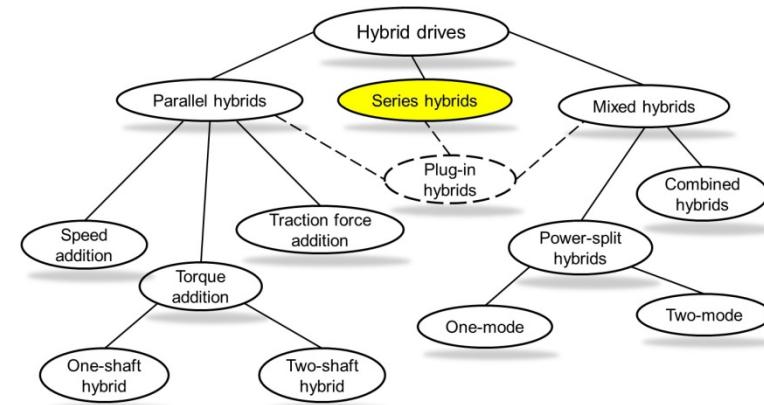
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# Series hybrid



- ICE only for electricity generation
- No mechanic connection of IEC and track
- Advantages:
  - Degrees of freedom in vehicle design
  - IEC operates in point of best efficiency
  - No gear needed
- Draw backs:
  - Additional, double energy conversion
  - Three full-valued machines  
(→ Full hybrid!)



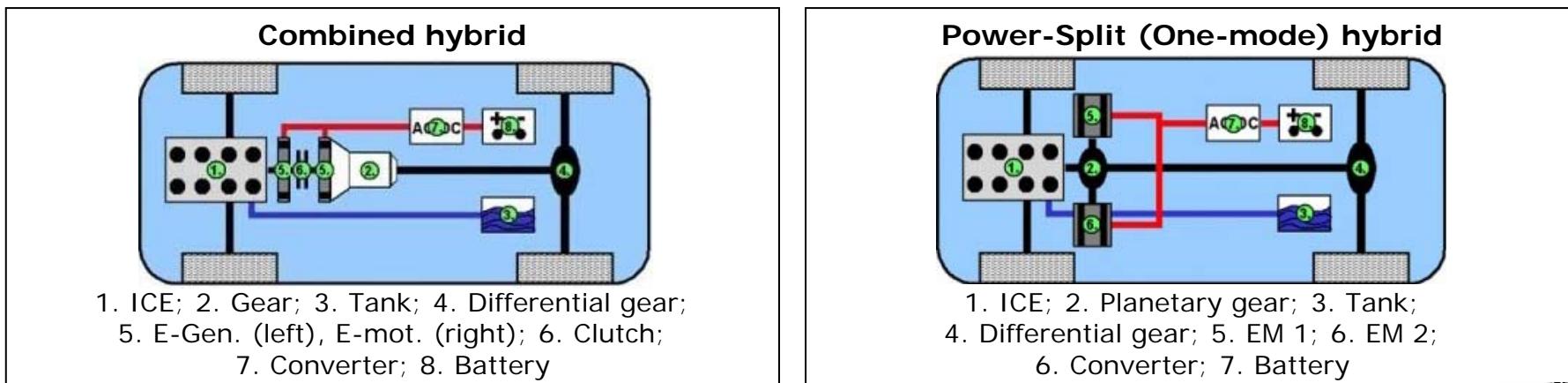
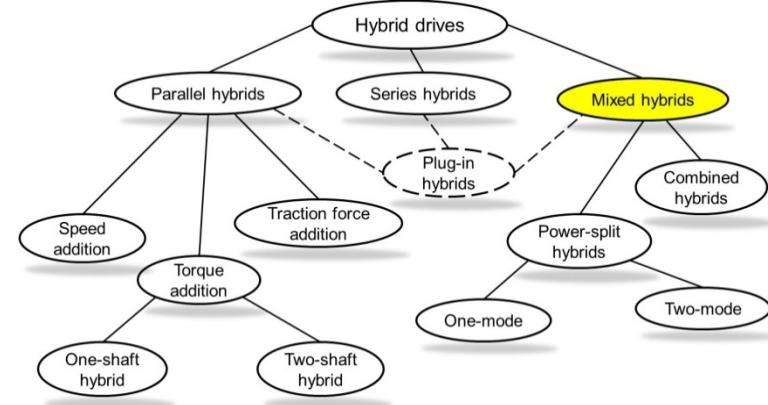
(Source: Hybrid-Autos.info)



# Mixed hybrid



- Different variants of mixed hybrid
- Combined Hybrid:
  - Elective drive either as series or parallel hybrid
- Power-split Hybrid
  - One-Mode: one fixed range of operating
  - Dual-Mode: two ranges of operating and four fixed gears



(Source: Hybrid-Autos.info)

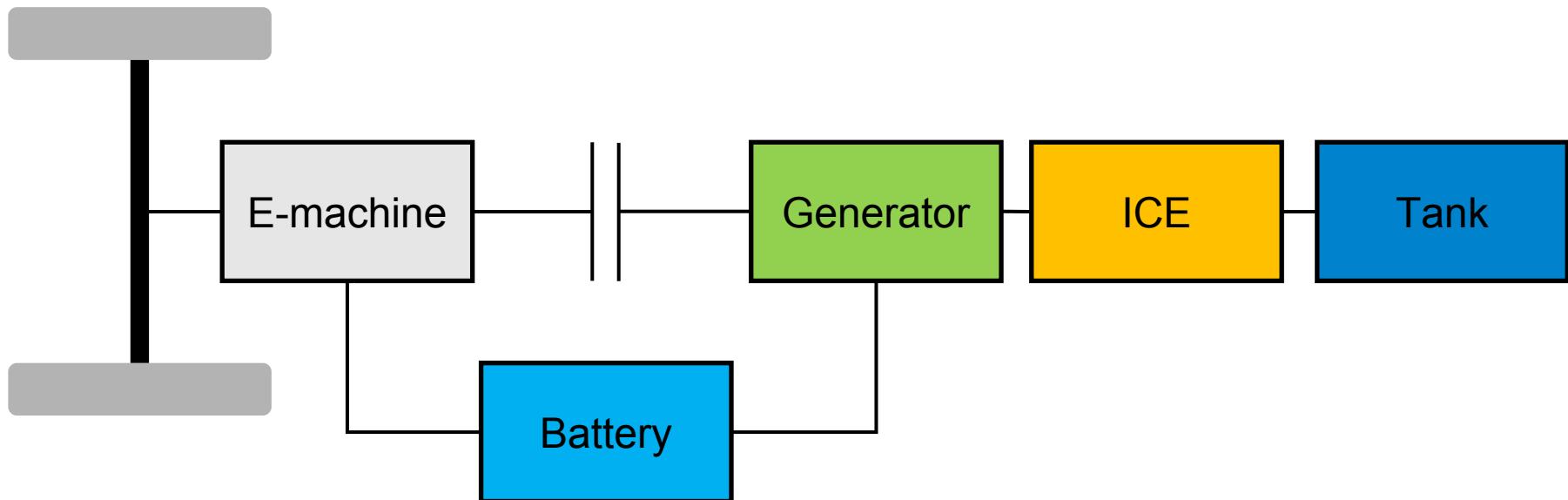


# Combined hybrid



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## Combined hybrid drive

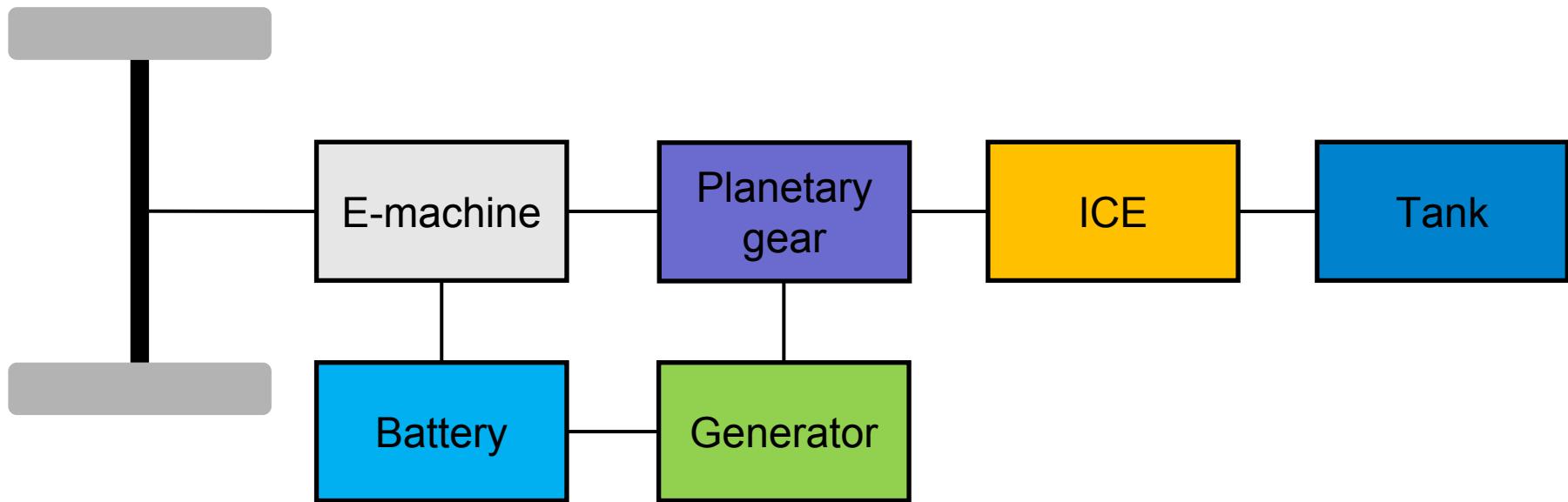


# Power-split hybrid



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## Power-split hybrid drive



Example: Toyota Prius: power splitting gear,  
Ni-MH-battery

# Hybridization classes



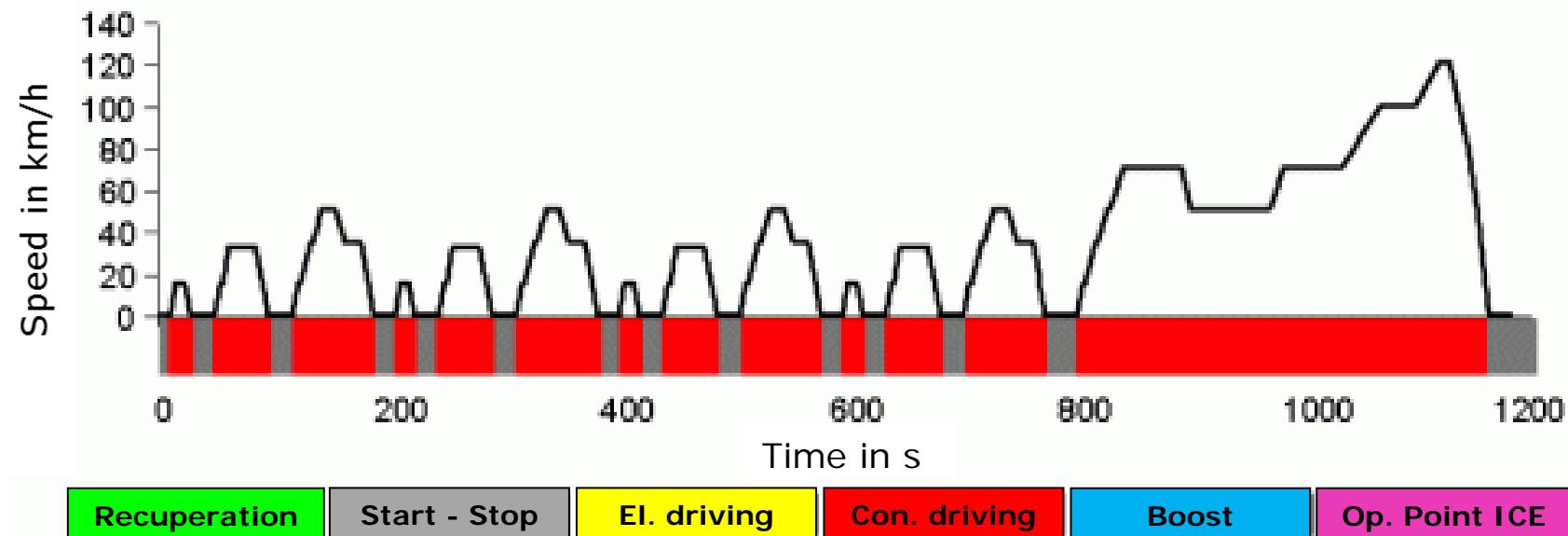
Class	Micro hybrid	Mild hybrid	Full hybrid
Power range	2 – 3 kW	10 – 15 kW	>15 kW
Operating voltage	12 V	42 – 144 V (with DC – DC - converter)	>> 100 V (with DC – DC - converter)
Characteristics	<ul style="list-style-type: none"> <li>• hardly any difference to a conventional vehicle</li> <li>• starter-generator instead of an alternator</li> </ul>	<ul style="list-style-type: none"> <li>• traction- instead of board battery</li> <li>• use of crankshaft-stator-generators</li> <li>• „downsizing“ – option</li> </ul>	<ul style="list-style-type: none"> <li>• sufficiently big dimensioned traction batteries and electric machines for purely electric drive</li> </ul>
Components of one operating strategy	<ul style="list-style-type: none"> <li>• no „real“ recuperation, but optimized charging of board battery</li> <li>• start – stop - function</li> </ul>	<ul style="list-style-type: none"> <li>• “real” recuperation</li> <li>• start - stop – function</li> <li>• „boost“ - option</li> <li>• load-point shift</li> </ul>	<ul style="list-style-type: none"> <li>• real recuperation</li> <li>• start – stop - function</li> <li>• „boost“ – option</li> <li>• load-point shift</li> <li>• purely electric driving possible</li> </ul>
Saving potentials *	2 – 10 %	10 – 20 %	20 – 50 %

(\* C. C. Chan: „Electric, Hybrid, and Fuel-Cell Vehicles: Architectures and Modeling“)

# Micro hybrid



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(Source: Hybrid-Autos.info)

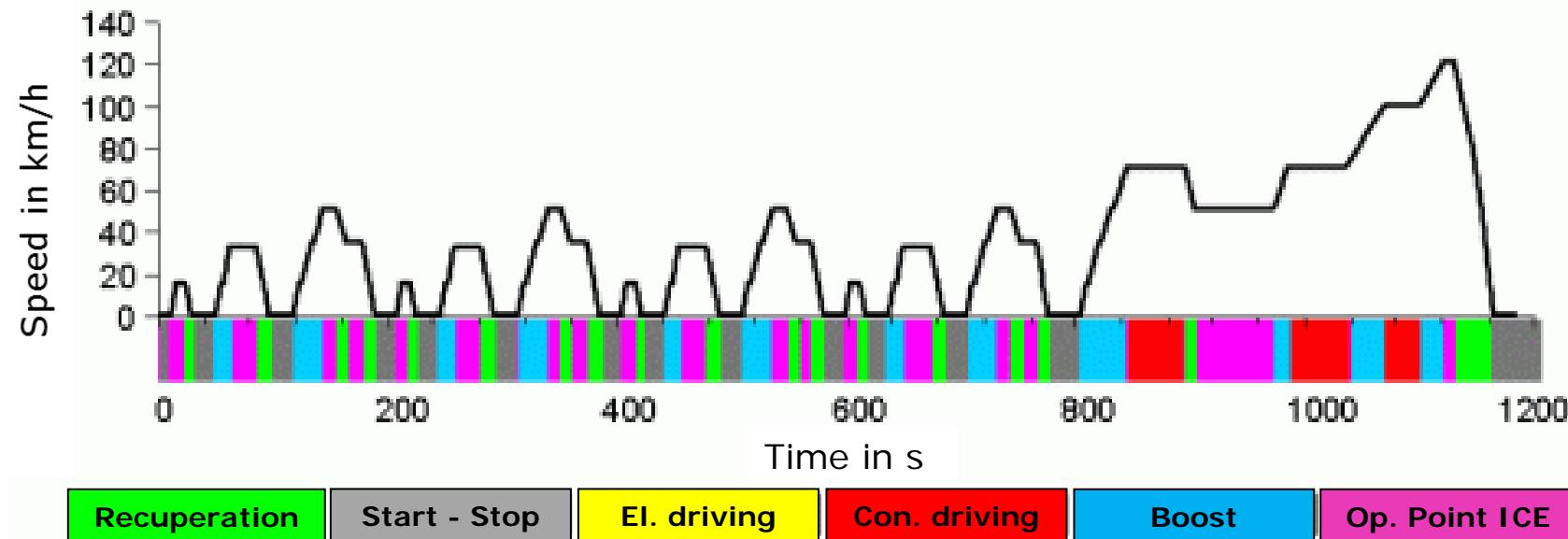
- Start – stop
- conventional driving



# Mild hybrid



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(Source: Hybrid-Autos.info)

Additionally to micro hybrid:

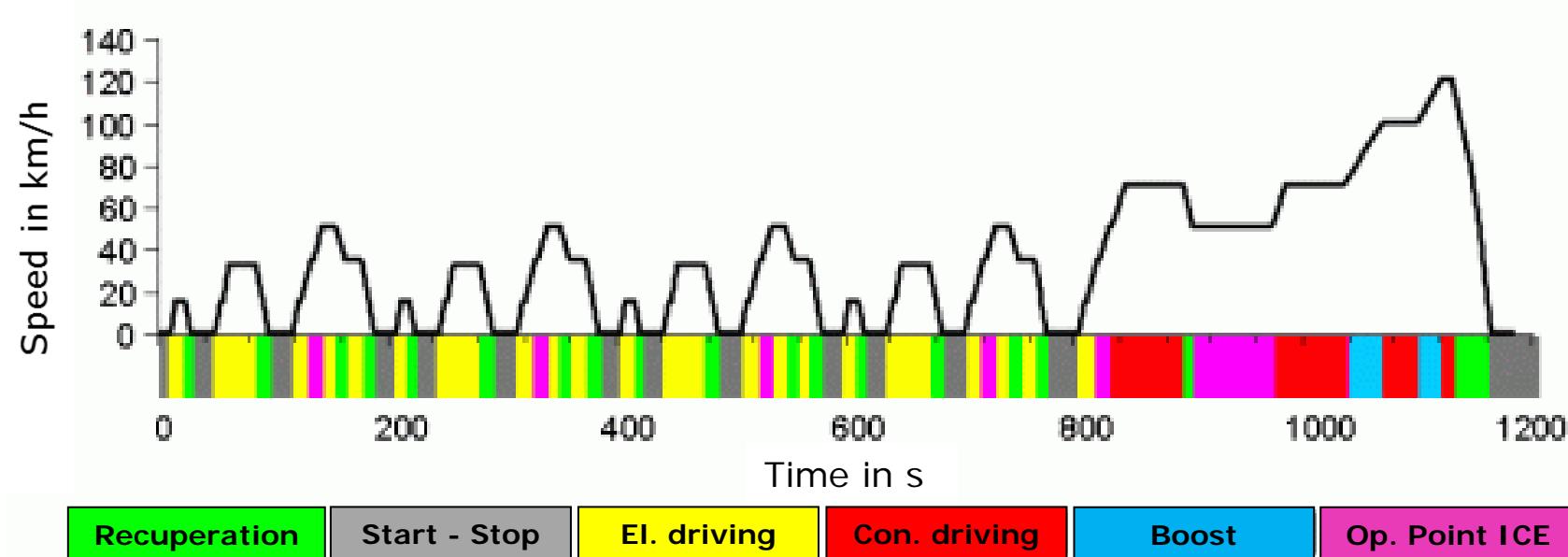
- Recuperation
- Boost
- Load point shift



# Full hybrid



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(Source: Hybrid-Autos.info)

Additionally to mild hybrid:

- Pure electric driving

# Current and future hybrid vehicles (selection)



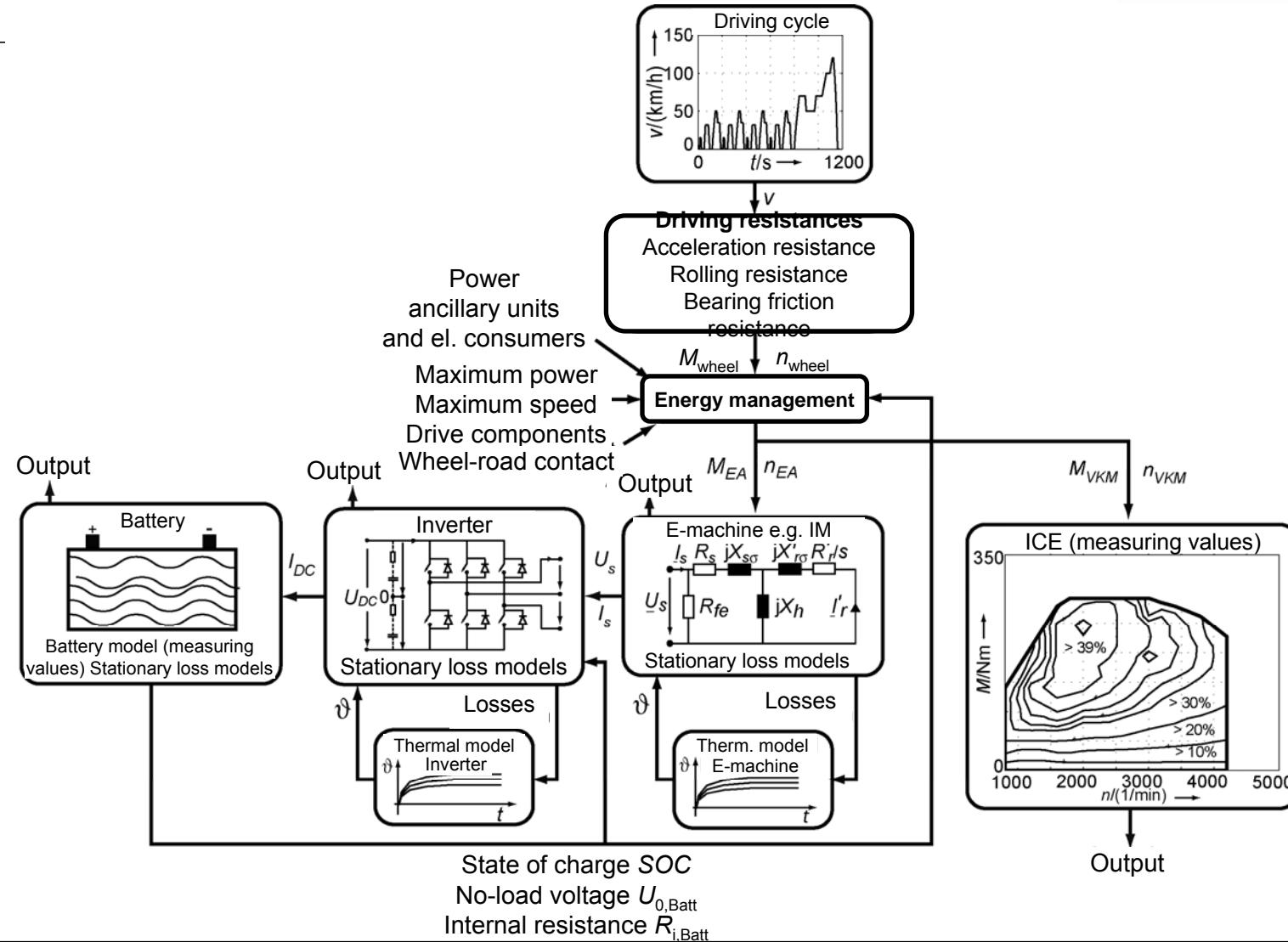
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	Series hybrid	Parallel hybrid: Torque-addition	Parallel hybrid: Tractive force-addition	Mixed hybrid: Combined	Mixed hybrid: Power-split (One-Mode)	Mixed hybrid: Power-split (Two-Mode)
Mild hybrid	(does not make sense)	<p>Honda („IMA“):</p> <ul style="list-style-type: none"> <li>• <a href="#">Jazz</a></li> <li>• <a href="#">Insight</a></li> <li>• <a href="#">CR-Z</a></li> </ul> <p>BMW:</p> <ul style="list-style-type: none"> <li>• <a href="#">ActiveHybrid 7</a></li> </ul> <p>Mercedes-Benz:</p> <ul style="list-style-type: none"> <li>• <a href="#">S400 BlueHYBRID</a></li> </ul>	(unknown)	(does not make sense)	(does not make sense)	(does not make sense)
Full hybrid	<p>Audi:</p> <ul style="list-style-type: none"> <li>• <a href="#">A1 e-tron (2013)</a></li> </ul> <p>BMW:</p> <ul style="list-style-type: none"> <li>• <a href="#">Megacity Vehicle (2013)</a></li> </ul>	<p>Audi:</p> <ul style="list-style-type: none"> <li>• <a href="#">Q5 Hybrid (2011)</a></li> <li>• <a href="#">A8 Hybrid (2011)</a></li> </ul> <p>VW:</p> <ul style="list-style-type: none"> <li>• <a href="#">Touareg Hybrid (2011)</a></li> </ul> <p>Porsche:</p> <ul style="list-style-type: none"> <li>• <a href="#">Cayenne S Hybrid</a></li> </ul>	<p>Peugeot („Hybrid4“):</p> <ul style="list-style-type: none"> <li>• <a href="#">3008 (2011)</a></li> </ul>	<p>Opel:</p> <ul style="list-style-type: none"> <li>• <a href="#">Ampera (2011)</a></li> </ul> <p>Chevrolet:</p> <ul style="list-style-type: none"> <li>• <a href="#">Volt (2011)</a></li> </ul>	<p>Toyota („HSD“):</p> <ul style="list-style-type: none"> <li>• <a href="#">Prius 3</a></li> <li>• <a href="#">Auris HSD</a></li> </ul> <p>Lexus („HSD“):</p> <ul style="list-style-type: none"> <li>• <a href="#">CT 200h</a></li> <li>• <a href="#">HS 240h</a></li> <li>• <a href="#">GS 450h</a></li> <li>• <a href="#">LS 600h</a></li> <li>• <a href="#">RX 450h</a></li> </ul>	<p>BMW:</p> <ul style="list-style-type: none"> <li>• <a href="#">X6 ActiveHybrid</a></li> </ul> <p>Mercedes:</p> <ul style="list-style-type: none"> <li>• <a href="#">ML 450 Hybrid</a></li> </ul>

Vehicle classes: [compact class](#) [middle class](#) [upper middle class](#) [upper class](#) [off-road vehicle](#)



# Simulation models for hybrid drives



# Hybrid operation: Energy management



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## Aim of an energy management strategy:

→ Reaching the destination with...

- Minimal consumption  
(Criterion for performed Matlab-Simulation)
- Minimal emission
- Etc.

## Challenge: (partly) missing previous knowledge of...

- Traffic density
- Driving behavior of driver
- Topography of route
- Weather (→ Use of headlight, air conditioning, etc.)
- Charging possibilities at grid (→ Plug-In hybrid)
- ...

## Conclusion:

- THE optimal operating strategy does not exist, but
- Many different, more or less good approximations



# Hybrid operation: Energy management



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- **Task:**

- Generating set values for drives with consideration of a desired aim
- General validity

- **Aim:** Minimizing of fuel consumption

- **Method:** Use of hybrid functions

- ICE - start/stop
- ICE – load-point shift
- Electric driving
- Electric boost

- **Boundary conditions:**

- Limit of starting processes ICE
  - Follow up time / minimum duty cycle
- SOC within band  $SOC_{min} \dots SOC_{max}$
- Max. torque of rotating drive parts (ICE, electric machine, gear)
- Max. power of static drive components (battery, inverter)
- Max. temperature of active parts inverter and electric machine

# Hybrid operation: Energy management



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## Towards a good energy management strategy:

- Tactical separation of total power and distribution on the single machines
- Considering characteristics of electric machine and ICE and variable parameters (e. g. in battery)

## Two basic optimizing approaches:

### Foreseeing energy management

- Approximation of demanded power based on past power demand

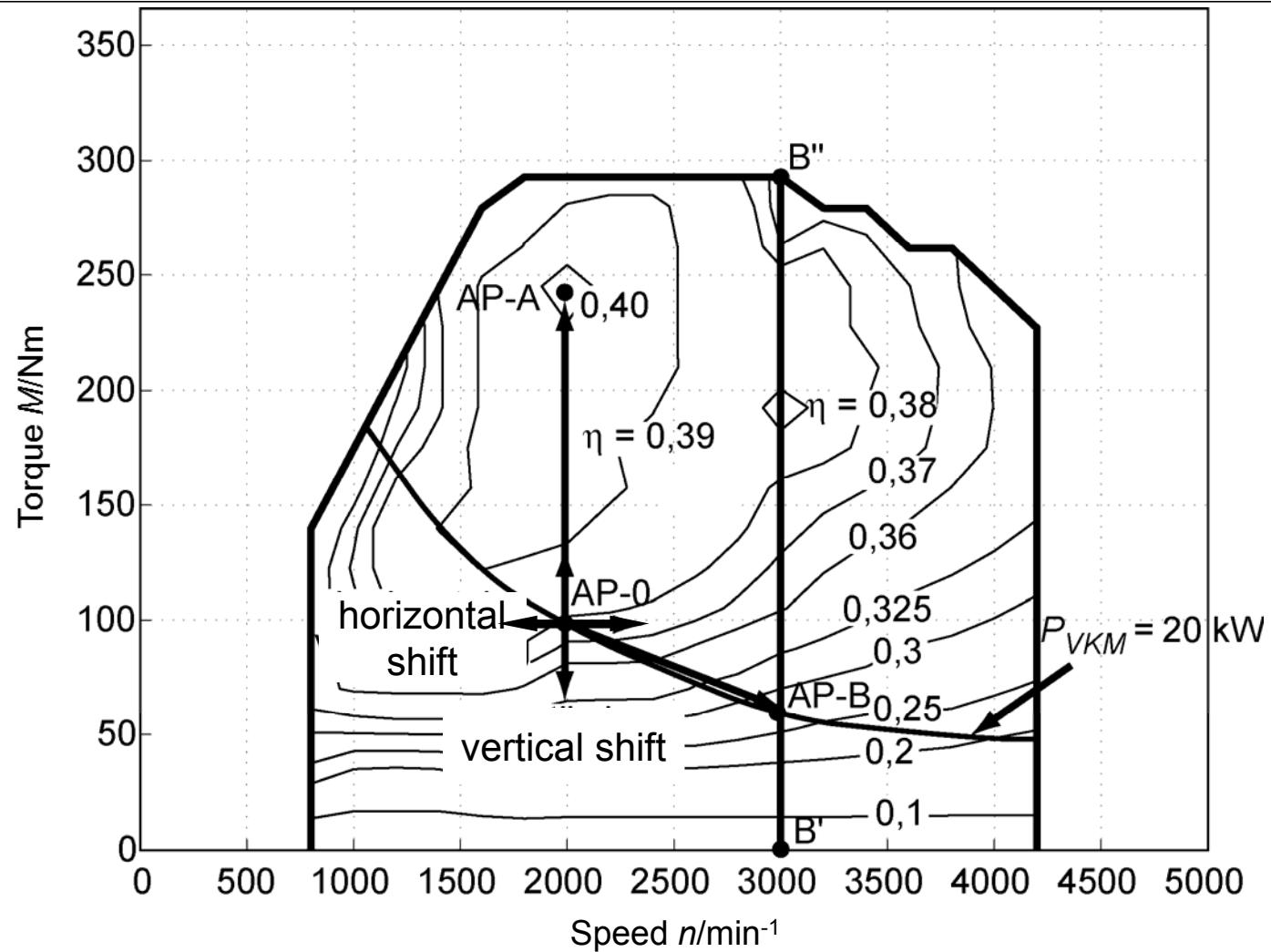
### Operating state management of ICE

- Consideration of boundary conditions e. g. ICE temperature
- → Load-point shift

## Example: ICE-load point shift



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# ICE – Load-point shift – Battery charge



- Battery effective power equals the charging resp. discharging power reduced by the battery losses
- Charging of the battery is done (except for regenerative braking) by **load-point shift of ICE** under expense of fuel.
- While discharging of battery this fuel consumption is converted into drive power. This amount of charge is to be replaced **at a later time** by the ICE.
- The **loading of the drive train** (resulting drive train losses) due to the battery charging is considered.
- Charging:  $P_{B,\text{eff}}$  added to the losses, discharging: losses subtracted from  $P_{B,\text{eff}}$ .
- Influence of this load-point shift **weighted with factor  $k_{\text{Batt}} = 1, 2, \text{ or } 3$** :
- $k_{\text{Batt}} \cdot P_{B,\text{eff}}$  added to resp. subtracted from losses: allows analysis of sensitivity during simulation for minimal total losses.

## Example: Calculation of fuel consumption HEV



### ■ Results P-HEV1

Cycle	$k_{\text{Batt}}$	$P_{\text{E-Drive,max}}$ kW	$\Delta \text{SOC}$ %	Min. consumption l/(100 km)		Fuel savings
				P-HEV1	ICE- vehicle	
NEDC	1	10	5	8,1	10,2	20 %
UDDS	2	10	10	8,4	10,6	21 %
Japan-10-15	2	10	10	9,6	12,9	25 %
Highway-FET	1	15	5	6,2	6,5	5 %

### ■ Results P-HEV2

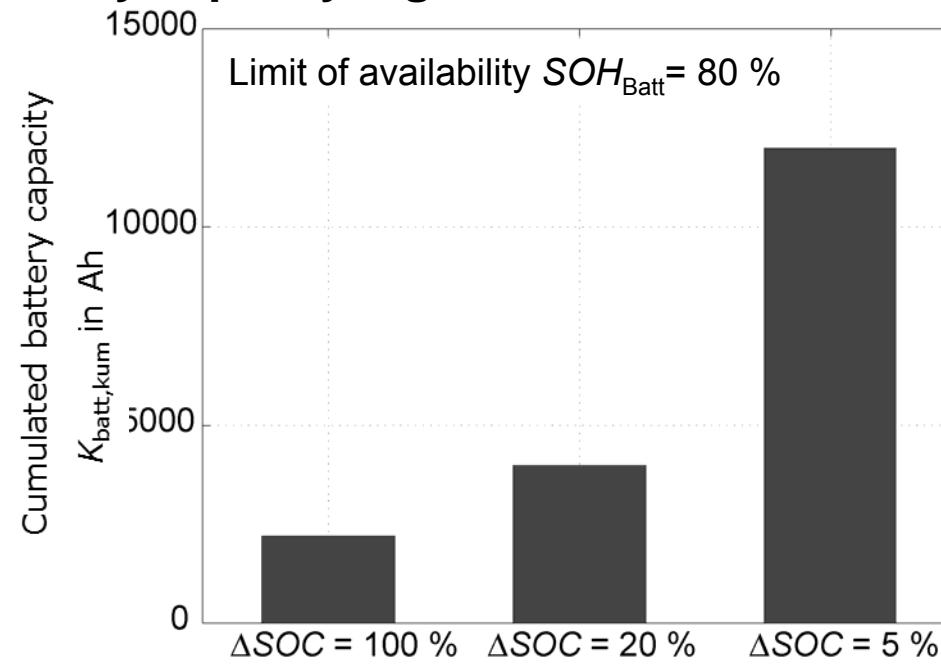
Cycle	$k_{\text{Batt}}$	$P_{\text{E-Drive,max}}$ kW	$\Delta \text{SOC}$ %	Min. consumption l/(100 km)		Fuel savings
				P-HEV2	ICE- vehicle	
NEFZ	1	15	5	8,1	9,3	13 %
UDDS	1	10	5	8,5	9,8	13 %
Japan-10-15	1	10	5	9,5	11,7	19 %
Highway-FET	1	10	5	6,1	6,1	0 %



## Example: Calculation of fuel consumption HEV



- Results depend on driving cycle and configuration of HEV
- $k_{\text{Batt}}$ : battery charging not / only slightly artificially forced
- $P_{\text{E-Drive, max}}$ : electric starting is limited to small power
- $\Delta \text{SOC}$ : Battery usage limited on a small window  $\Delta \text{SOC}$   
→ cumulated battery capacity high





## Specific aspects of energy management for different topologies

- Series hybrid:
  - 2-dimensional (torque- and speed-) load-point shift
  - Only one driving motor → simple energy management
  - „One-point-operation“ vs. „trajectory operation“
- Parallel hybrid:
  - Torque addition: torque-load-point shift
  - Speed addition: speed-load-point shift
- Power-split hybrid:
  - E-machine 1 at driving shaft: torque-load-point shift
  - ICE and E-machine 2: 2-dim. Load-point shift

(as long as gear equations are fulfilled)



# **Planning and application of electrical drives (PAED) – Drives for electric vehicles**



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## **Electric vehicles - Overview**

# Zero emission vehicle – Definition

- Definition zero emission vehicle:

Zero emission of any kind of pollutant in operation and standstill, no evaporation emission, no indirect emission
- Based on the environment legislation of *California Air Resources Board* (CARB)
- Exhaust gas legislation der CARB valid in *California* and also 12 other states of the USA
- By law subsidized ZEV-share is rising
  - From 10% in 2003 to
  - 16% in 2018

# California – Classification of vehicles



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- **TLEV: Transitional low emission vehicle**  
This is the weakest emission standard in *California*. TLEVs expire in 2004 and are being removed from the market.
- **LEV: Low emission vehicle**  
All vehicles which were sold after 2004 in *California* match at least this standard.
- **ULEV: Ultra low emission vehicle**  
ULEVs are 50% cleaner than the average vehicle of the current build year.
- **SULEV: Super ultra low emission vehicle**  
SULEVs are 90% cleaner than the average vehicle of the current build year.

# California – Classification of vehicles



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- **ZEV – Zero emission vehicles**

ZEVs have no exhaust gas emission. This includes battery powered fuel cell based electric vehicles. The category ZEV includes two additional classes [18]:

- PZEV: Partial zero emission vehicle

PZEVs fulfill the SULEV exhaust gas emission standards, have no evaporation emission and a 15 years / 150.000 miles warranty. No evaporation emission means, that vehicles have less emission, while driving than typical vehicles with ICE in turn-off state.

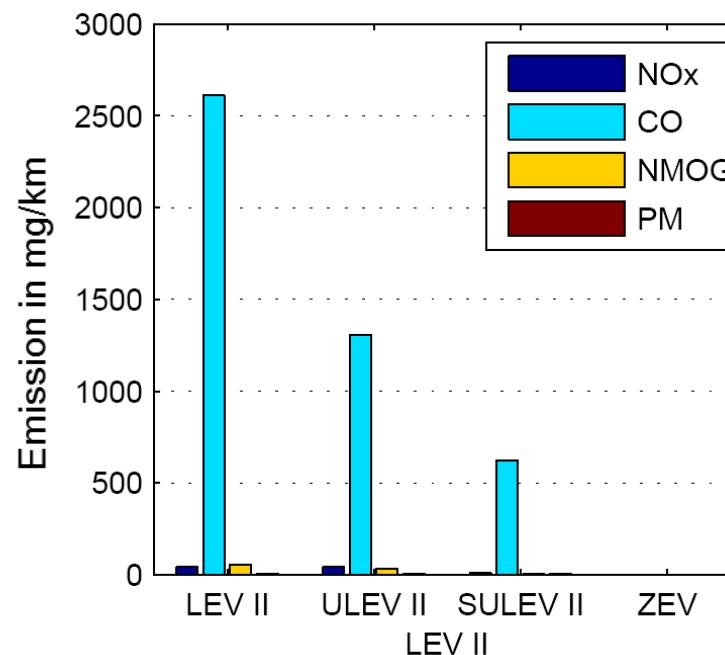
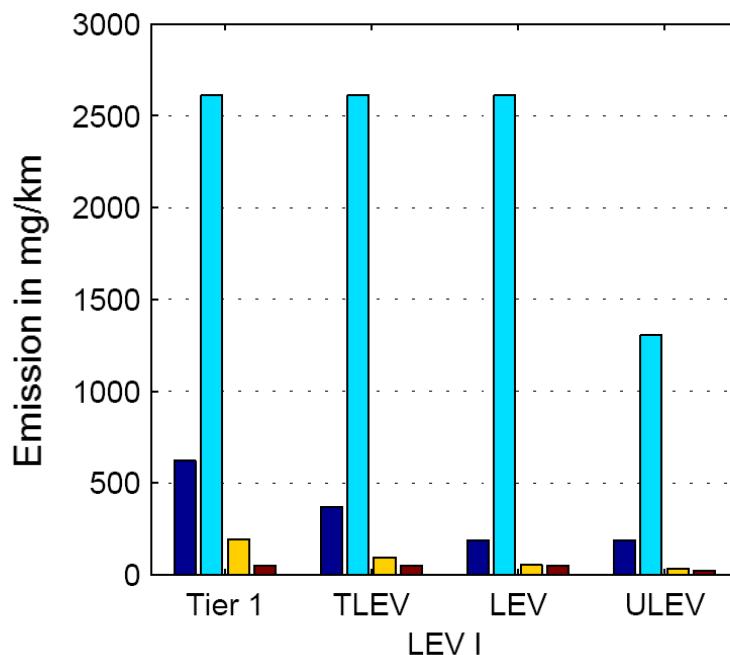
- AT PZEV: Advanced technology PZEVs

AT PZEVs fulfill the PZEV requirements and have additionally ZEV- similar properties. A CNG-vehicle (compressed natural gas) or a hybrid vehicle with engine emission, which fulfill the PZEV standards, would be classified as AT PZEV.

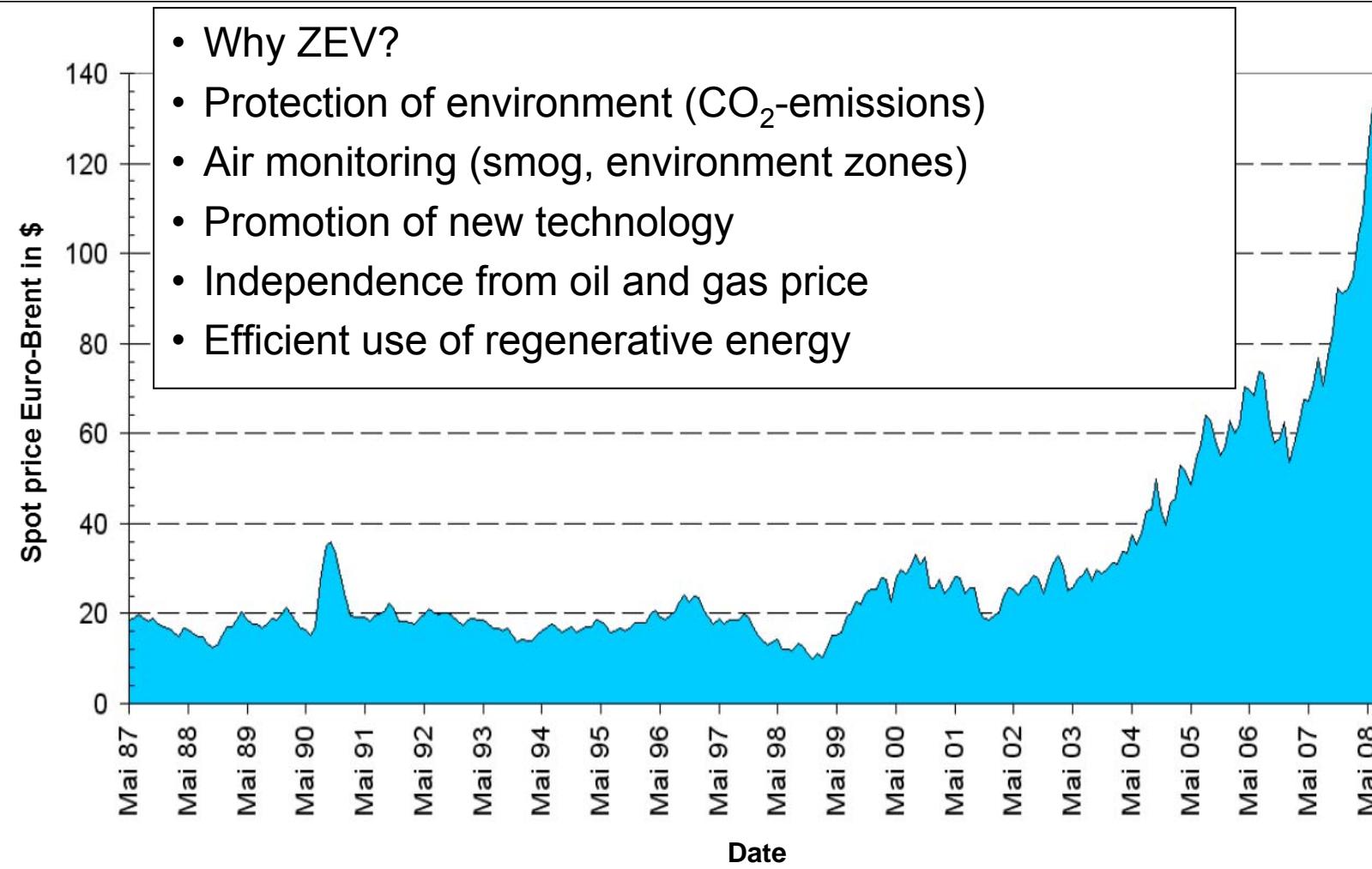
# Zero emission vehicle – Legislation



- ZEV with conventional drive / exhaust gas treatment unfeasible
- Possibility of allowance of partial-zero-emission-vehicle-credits
  - Share can also be fulfilled by SULEV II+ certified



# Zero emission vehicle – Motivation



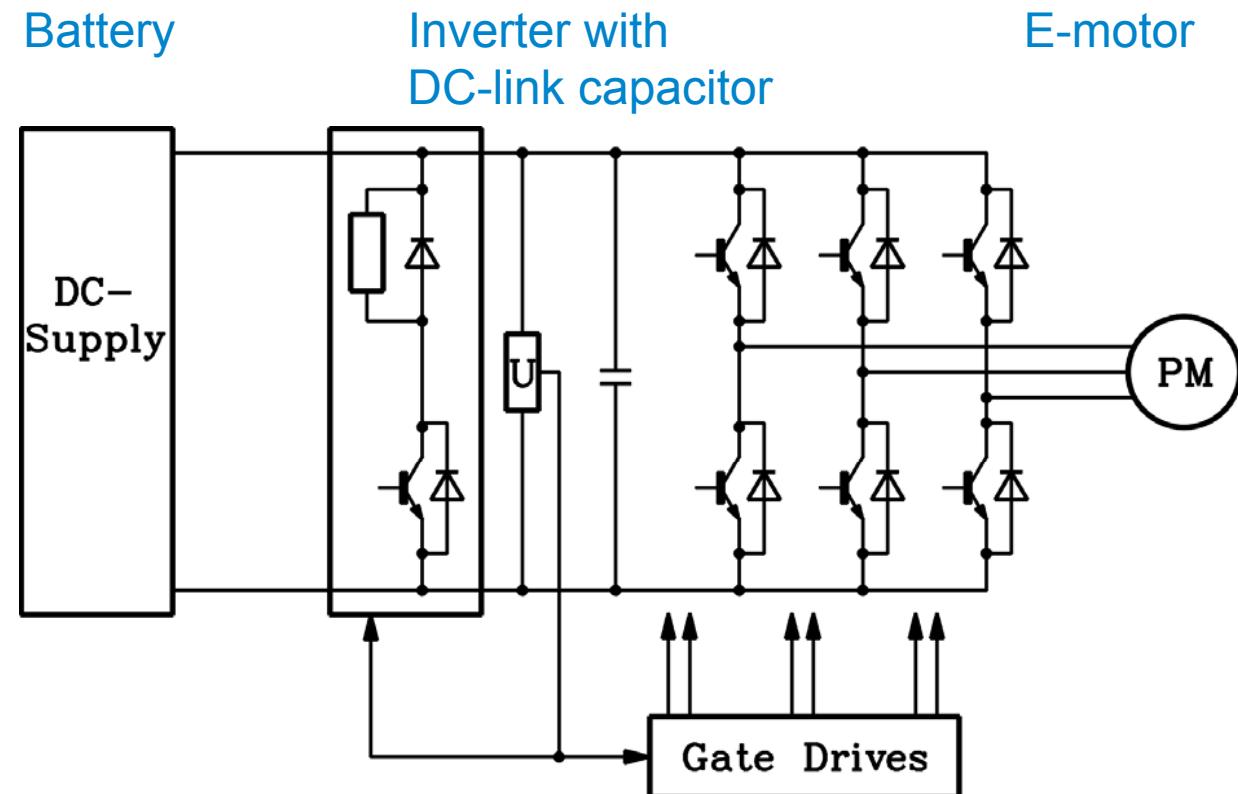
# Battery powered vehicles



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## System:

- a) Battery
- b) Inverter
- c) E-motor
- d) Gear
- e) Wheel
- f) Track



# Drive variants for ZEV target and aim quantities



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- Example-requirements for a zero emission vehicle:
- By law requested range in FTP-72 driving cycle 100 miles  
→ **110 miles (177 km) range** as desired value during FTP-72 driving cycle
- Target in example:
  - Sprint from zero to 100 km/h in 7 seconds
  - Feature for sportive driving  
→ compare **VW Golf GTI, Tesla Roadster**
  - Temporary **max. speed 150 km/h**
    - No long range - limousine for highway journeys,
    - Rather commuter vehicle for city traffic
  - Assumption **empty weight of vehicle 900kg**
    - Comparable to *Smart Fortwo*
    - Air resistance  $c_w A = 0.5$  (comparable to *Smart Roadster*)

# **TESLA Roadster (USA)**



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- Lithium-ion-battery:  
6381 cells = 11 series modules  
1 module = 9 series component  
1 component = 69 parallel cells
- Max. torque 271 Nm
- Max. power 185 kW
- Sports vehicle
- 1.2 tons empty weight
- 0 ... 100 km/h in 4 seconds
- max. 200 km/h ( 125 mph)
- max. motor speed: 13000/min
- Squirrel cage induction machine
- Price: 110.000 USD



- Range: 392 km in combined EPA-test cycle with 45 kWh battery energy
- 3.5 h charging time
- Lifespan 500 cycles:  $500 \times 392 = 200000$  km

*Tesla Roadster (Source: <http://www.teslamotors.com/>)*

# ***Lightning GT (UK)***



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- Lithium-ion-batteries:  
*(AltairNano: „NanoSafe“)*  
Nano-titanat-technology instead of  
graphite
- Max. power 552 kW
- Sports vehicle
- Carbon fiber-Kevlar-  
composite chassis
- 0 ... 100 km/h in 4 seconds
- Max. 210 km/h
- 4 PM-synchronous motors as  
brushless-DC hub motors  
 $(P_N = 120 \text{ kW each Motor})$ ,

*PML Flightlink Ltd.*



- Range: 415 km with fully charged  
battery
- 10 min. quick-charge: 155 km range
- Lifespan: after 15000 cycles: 85% of  
new-capacity

*Source: Lightning Car Company, UK*



## **Electric vehicles – Drive components**

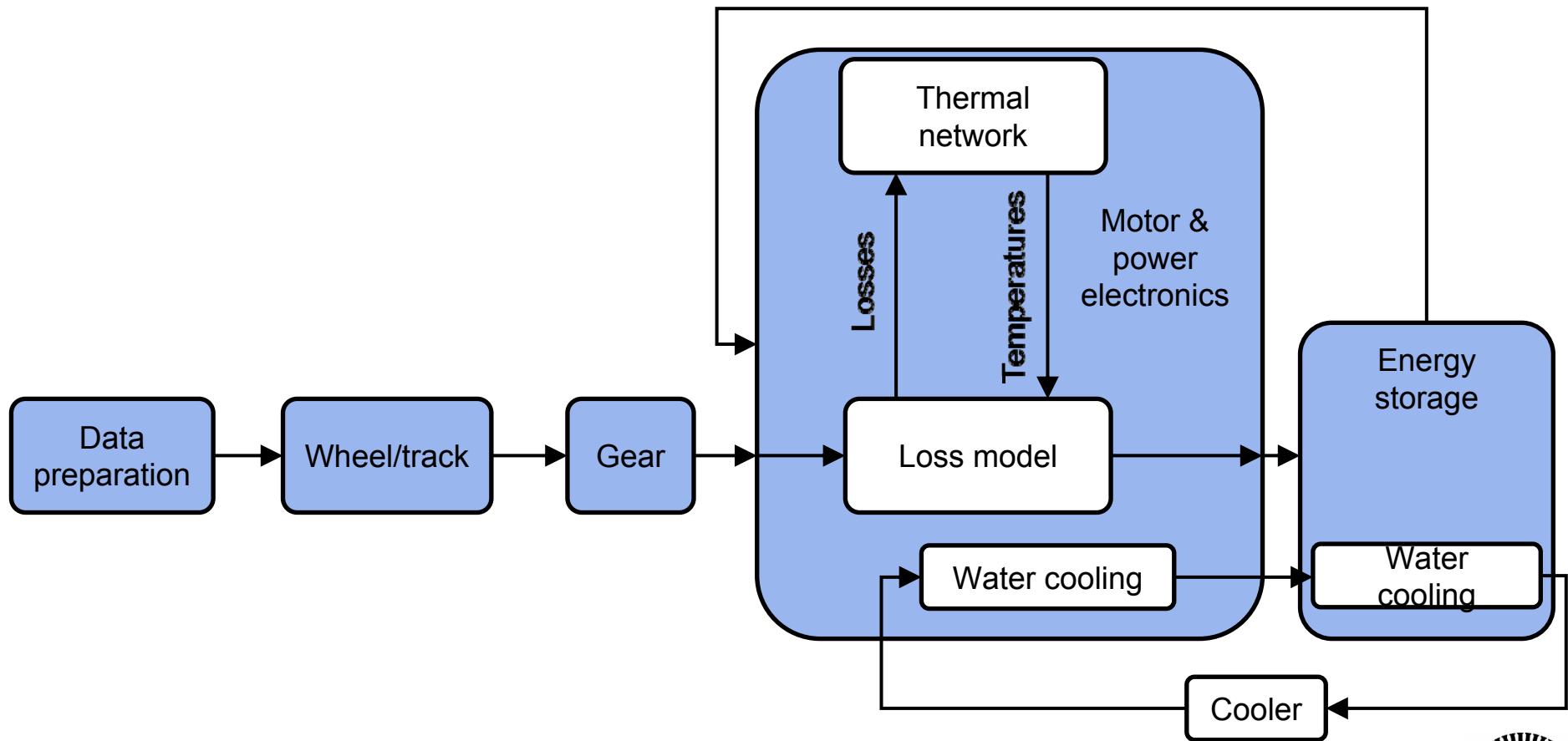
# Drive variants for ZEV

## Simulation – Simulation model



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- Simulation model implementation in *Matlab Simulink*



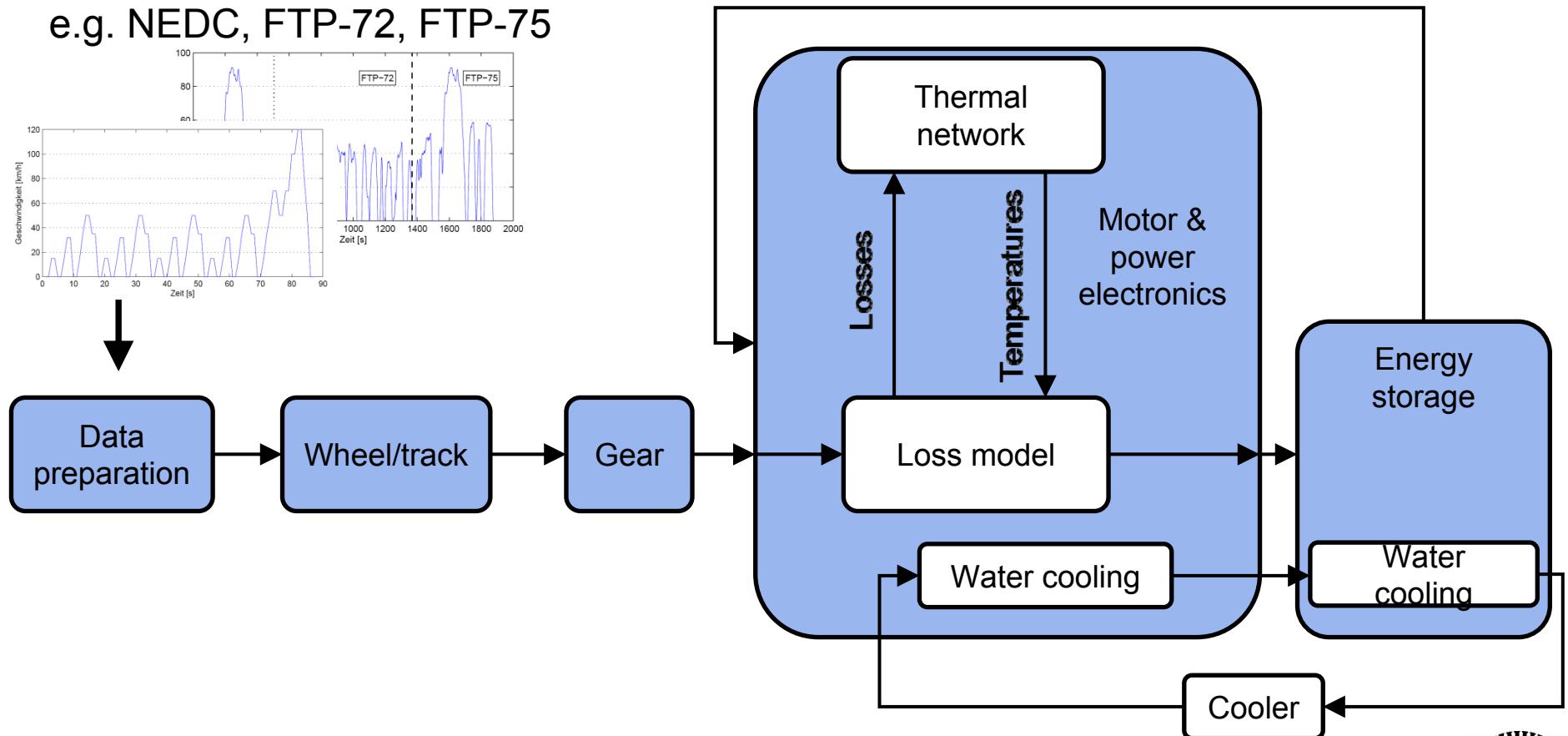
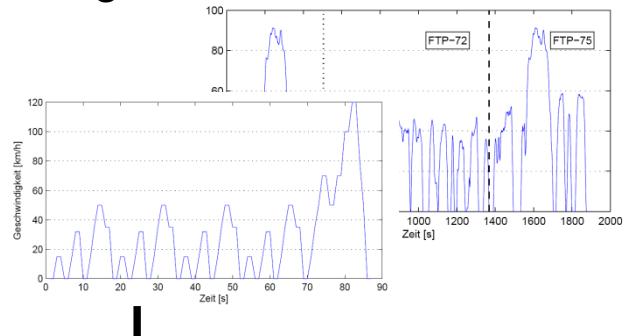
# Driving cycles for ZEV Simulation – Simulation model



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Driving cycles

e.g. NEDC, FTP-72, FTP-75

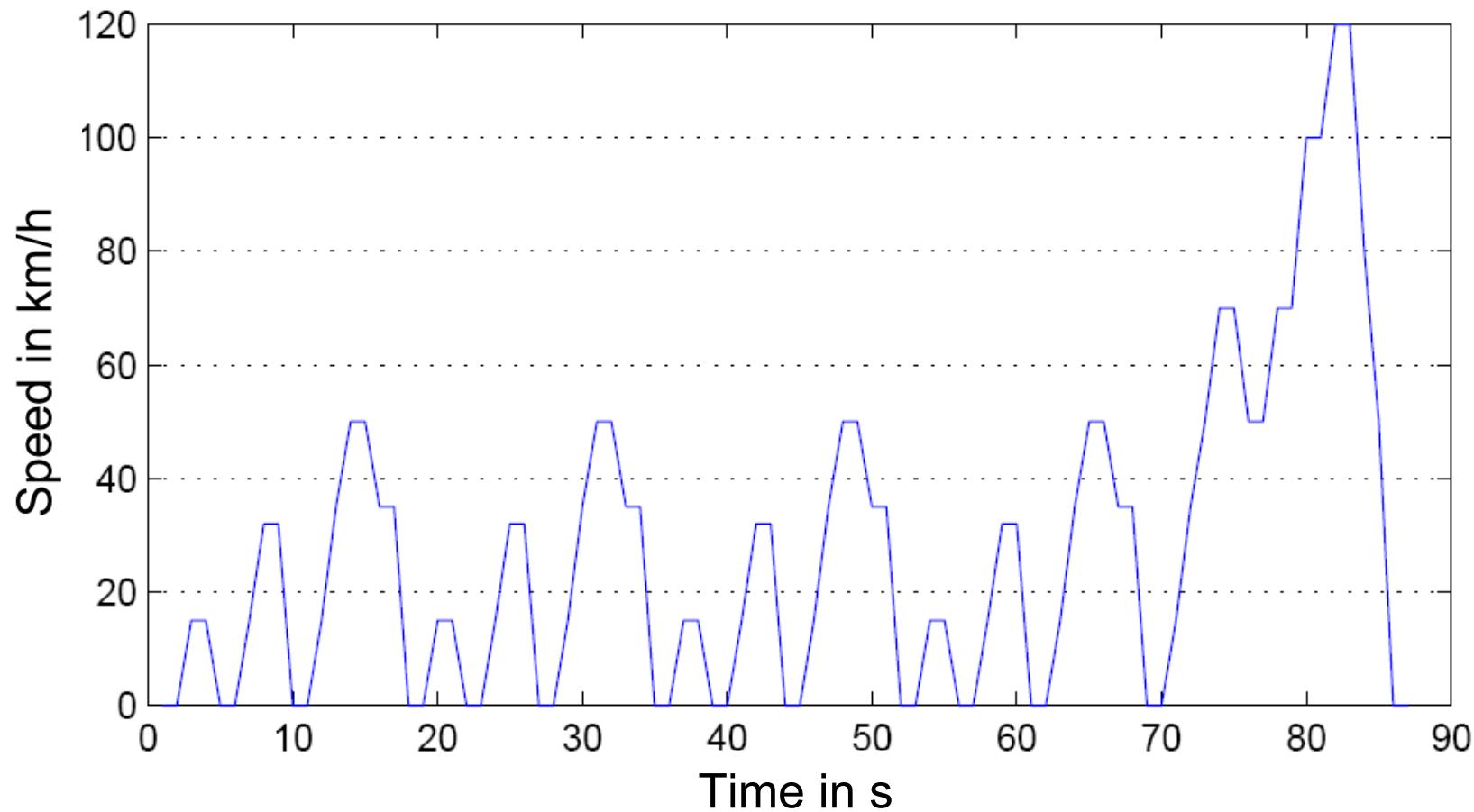


# Driving cycle NEDC



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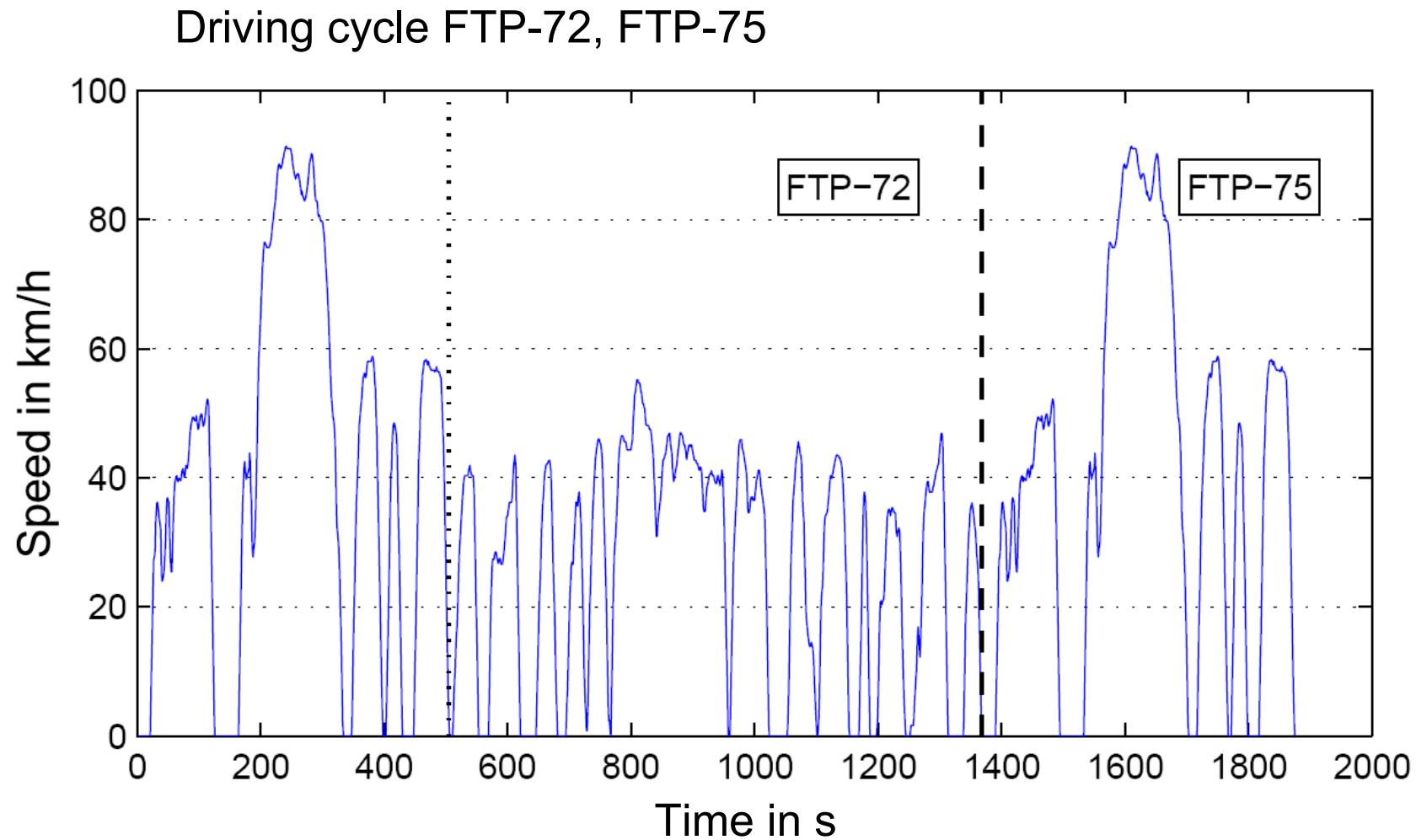
Driving cycle: NEDC: New European driving cycle



# Driving cycle FTP-72, FTP-75

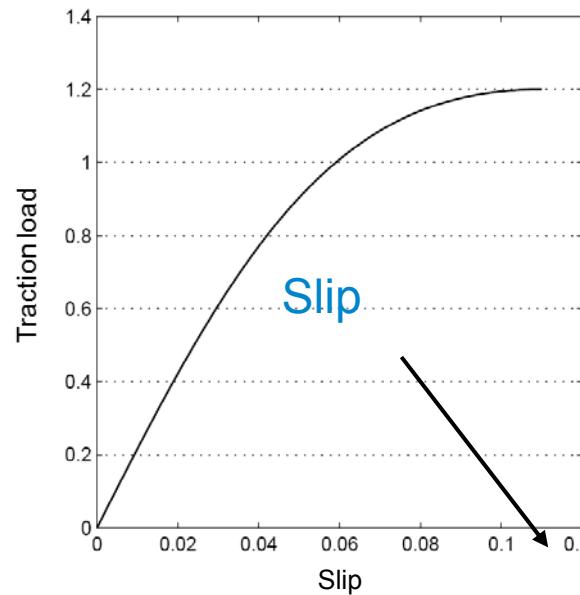


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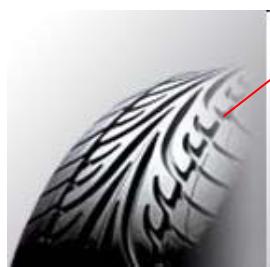
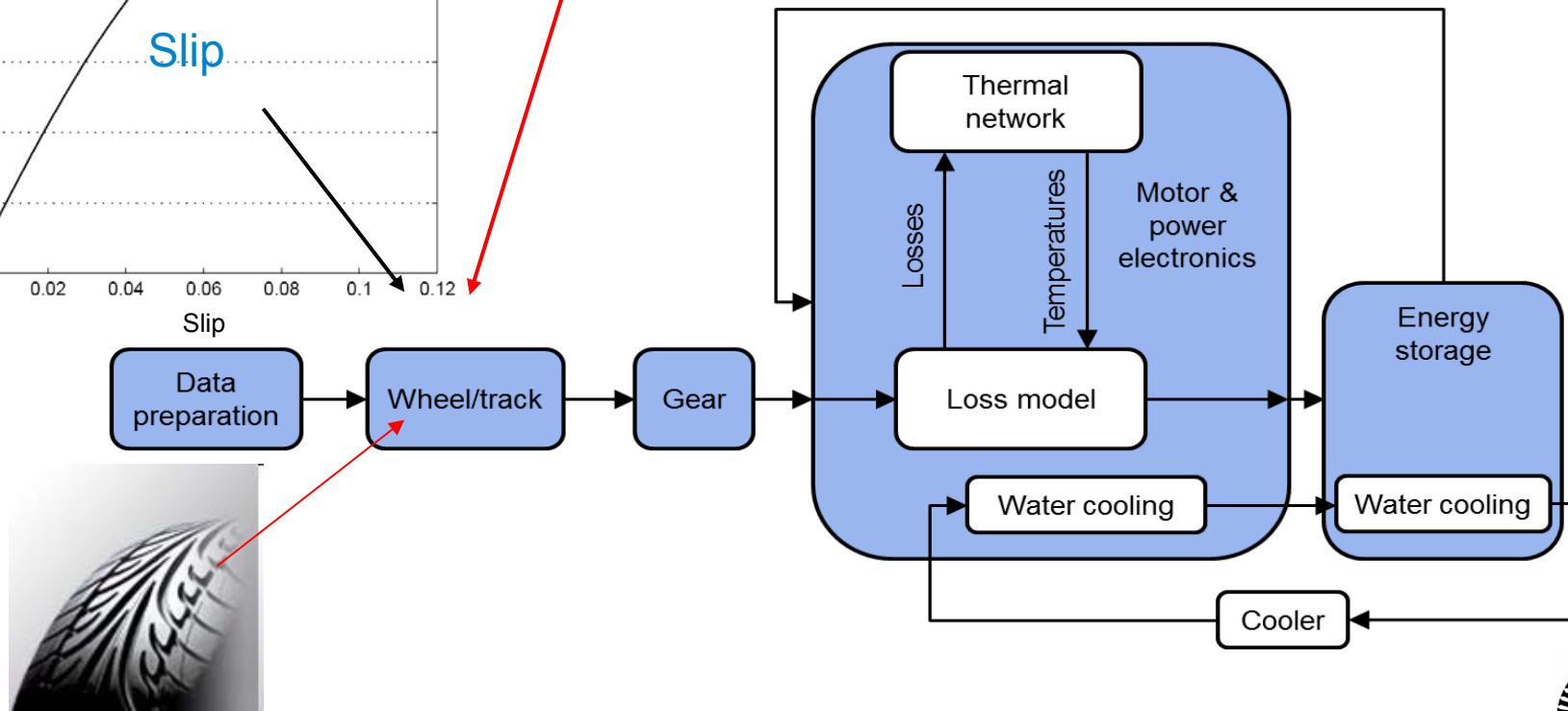


# Driving resistances

## Simulation – Wheel / track



- Driving resistance:
  - Rolling resistance
  - Air resistance
  - Acceleration resistance
  - Slope resistance



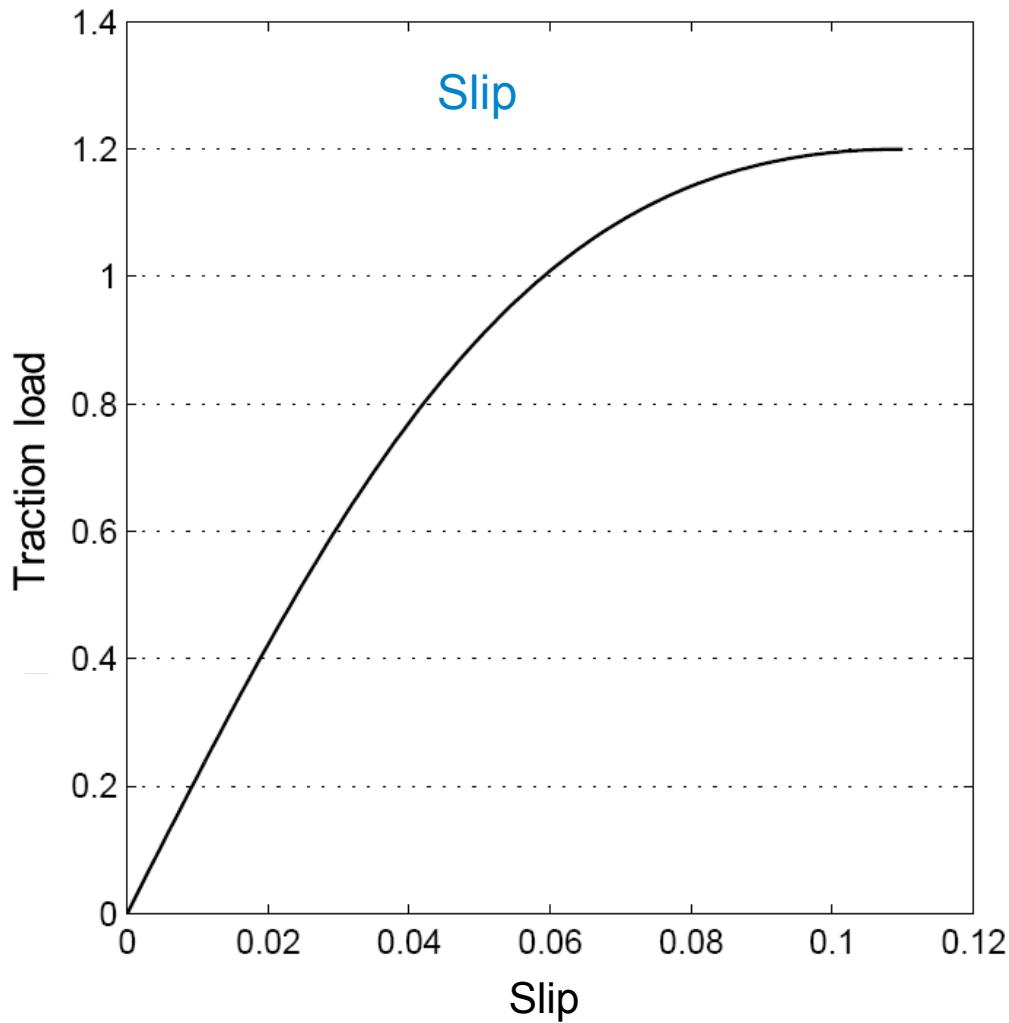
# Slip between wheel and track

## Simulation – Wheel / track



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- Without slip, there is no tractive force transmission to the track, but only „pure“ rolling!

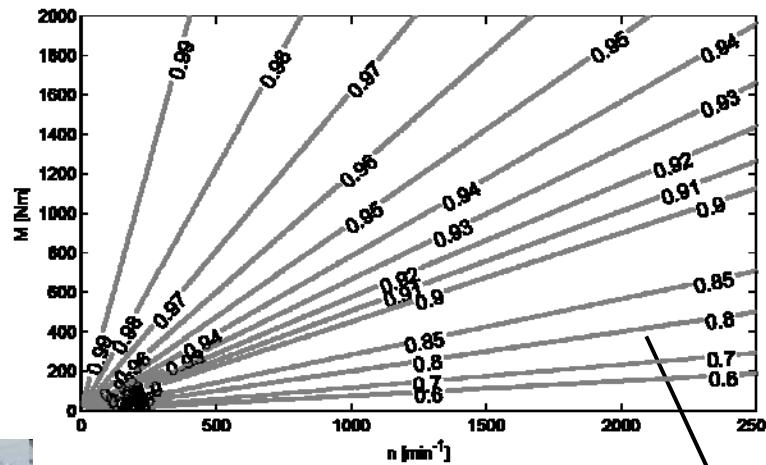


# Single-stage gear between wheel and E-motor



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- Efficiency of gear

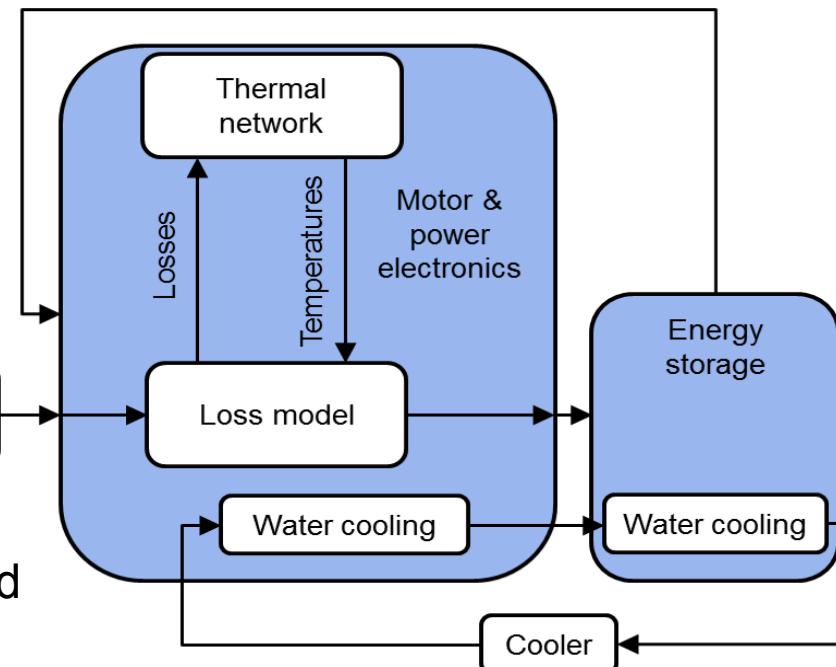


- Low wheel speed  $\rightarrow$  high E-Motor speed
- High E-Motor speed  $\rightarrow$  small E-Motor

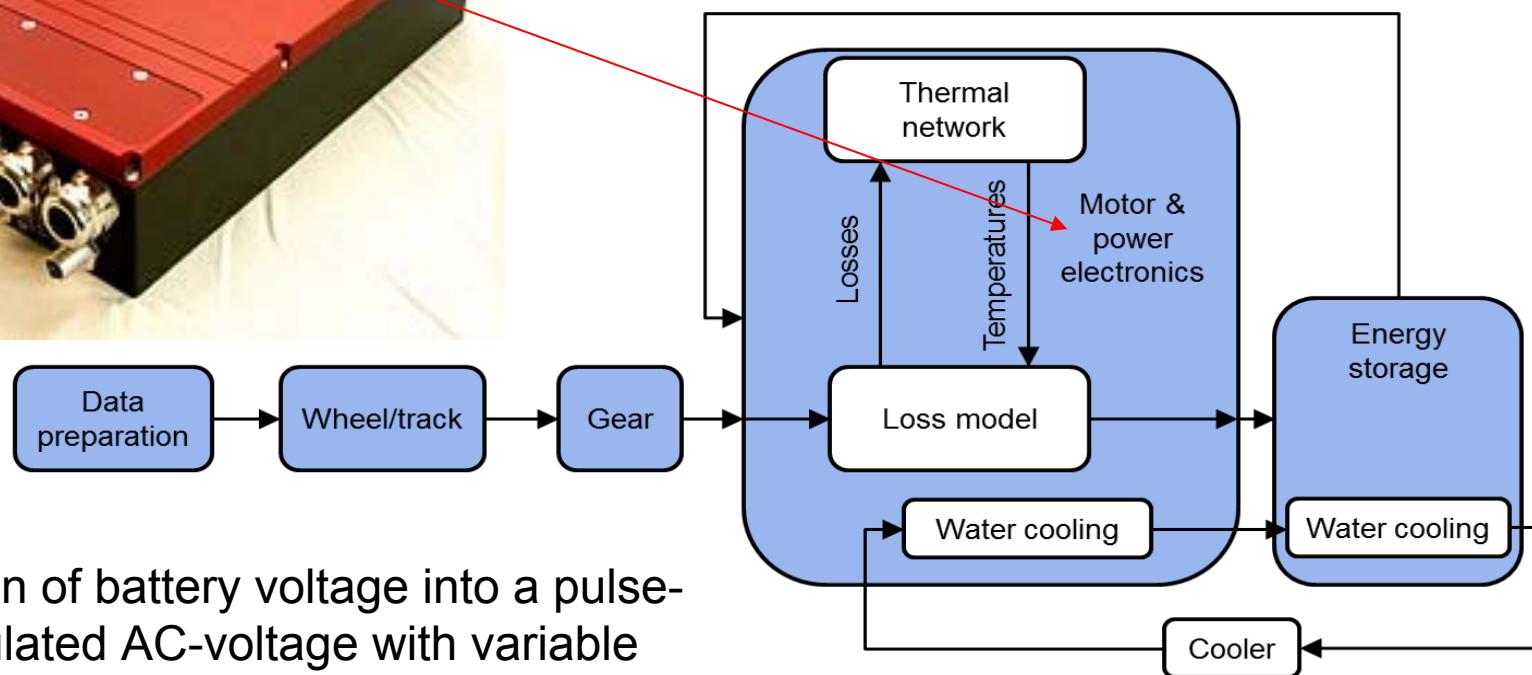
Single stage reduction gear

$$i = 8$$

Above approx.  $i = 10$  double-stage gear necessary!



# Power electronic chopper (Inverter)



- Conversion of battery voltage into a pulse-width-modulated AC-voltage with variable frequency
- Variable frequency = variable motor speed

## Example: Inverter Brusa



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- *Brusa DMC524* 3-phase-inverter for automobile applications
  - 480 V DC-link voltage
  - 600 V IGBTs
  - 80kW continuous power
- Model for calculation of switching- and conduction losses for diodes and transistors
- For Simulation: e. g.  
board grid power = 150 W constant power



# Example: Inverter Brusa



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Electric properties	
Minimal supply voltage for full output current in V	200
Maximum operating supply voltage in V	480
Over voltage cutoff in V	500
Maximum permitted over voltage in V	520
Continuous current, RMS in A	225
Repetitive maximum current, RMS, 30s 100%, 90s 50% in A	300
Continuous power in kW	80
Maximum power in kW	106
PWM frequency symmetric modulation in kHz	24
Mechanic properties	
Height in mm	88
Width mm	240
Length in mm	360
Volume in cm <sup>2</sup>	7600
Weight (without cooling water) in kg	9.5
Ambient operating temperature in °C	-40...+85



## Example: Inverter – Conti Temic



### ▪ Technical data IGBT-Inverter

Maximum current $I_{\max}$	250 A
DC-link voltage $U_{\text{DC}}$	110 - 370 V
Switching frequency $f_{\text{switching}}$	8 kHz
Weight $m_{\text{inverter}}$	10 kg
Coolant flow $\dot{V}$	8 l/min
Coolant-supply temperature $\vartheta_{\text{CS}}$	85 °C
DC-link capacitance $C_{\text{DC-link}}$	2 mF
DC-link resistance $R_{\text{DC-link}}$	1 mΩ



### ▪ Loss groups

Losses	IGBT	Diode
<b>Static losses</b> Conduction losses $P_C$ Blocking losses $P_{\text{block}}$	X (X)	X (X)
<b>Switching losses</b> Switch-on losses $P_{\text{ON}}$ Switch-off losses $P_{\text{OFF}}$	X X	(x) X
<b>Trigger losses <math>P_{\text{trigger}}</math></b>	X	X



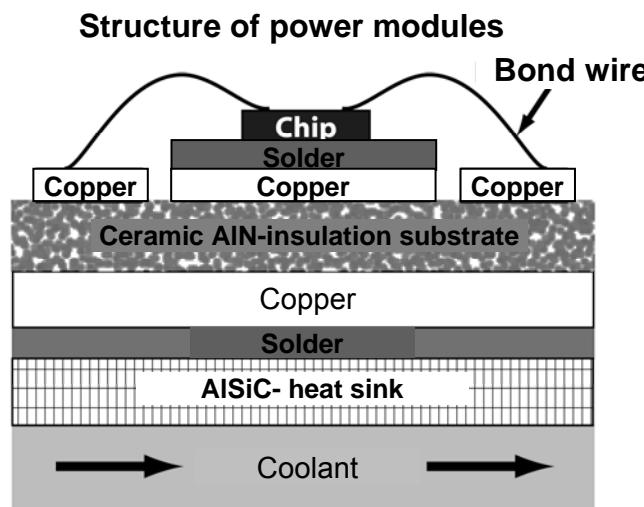
# Inverter – Heating



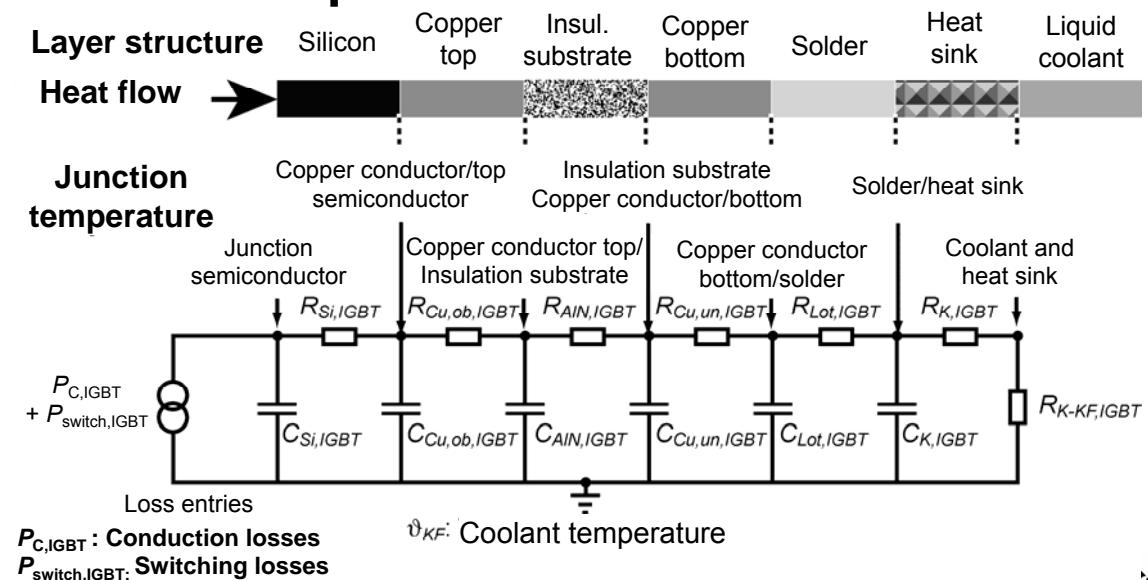
## ■ Modeling

- RC-network ( $R$ : heat resistance,  $C$ : heat capacity)
  - Dynamic calculation temperatures
- 6-body-model
- Analytic calculation  $R$ ,  $C$  on the basis of structure geometry
- No thermal coupling to neighboring power electronic semi conductors

## ■ Structure technology



## ■ Thermal equivalent circuit IGBT



# Example: PM-synchronous machine

## *Brusa*



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- *Brusa Hybrid Synchronous Machine*  
6.17.12
  - 40 kW rated power, 85 Nm rated torque
  - Available on the market
  - Used in E-cars by hobbyists



# Example: PM-synchronous machine

## *Brusa - Data*



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Mechanic properties	
Number of slots Q	36
Pole count	6
Number of turns per pole and phase q	2

Electric properties	
Rated power in kW	40
Rated speed in 1/min	4500
Rated torque in Nm	85
Rated current in A, phase	96
Rated voltage in V, phase	164
$\cos\varphi$	0,885
Efficiency in %	95,7
Losses in W	1800

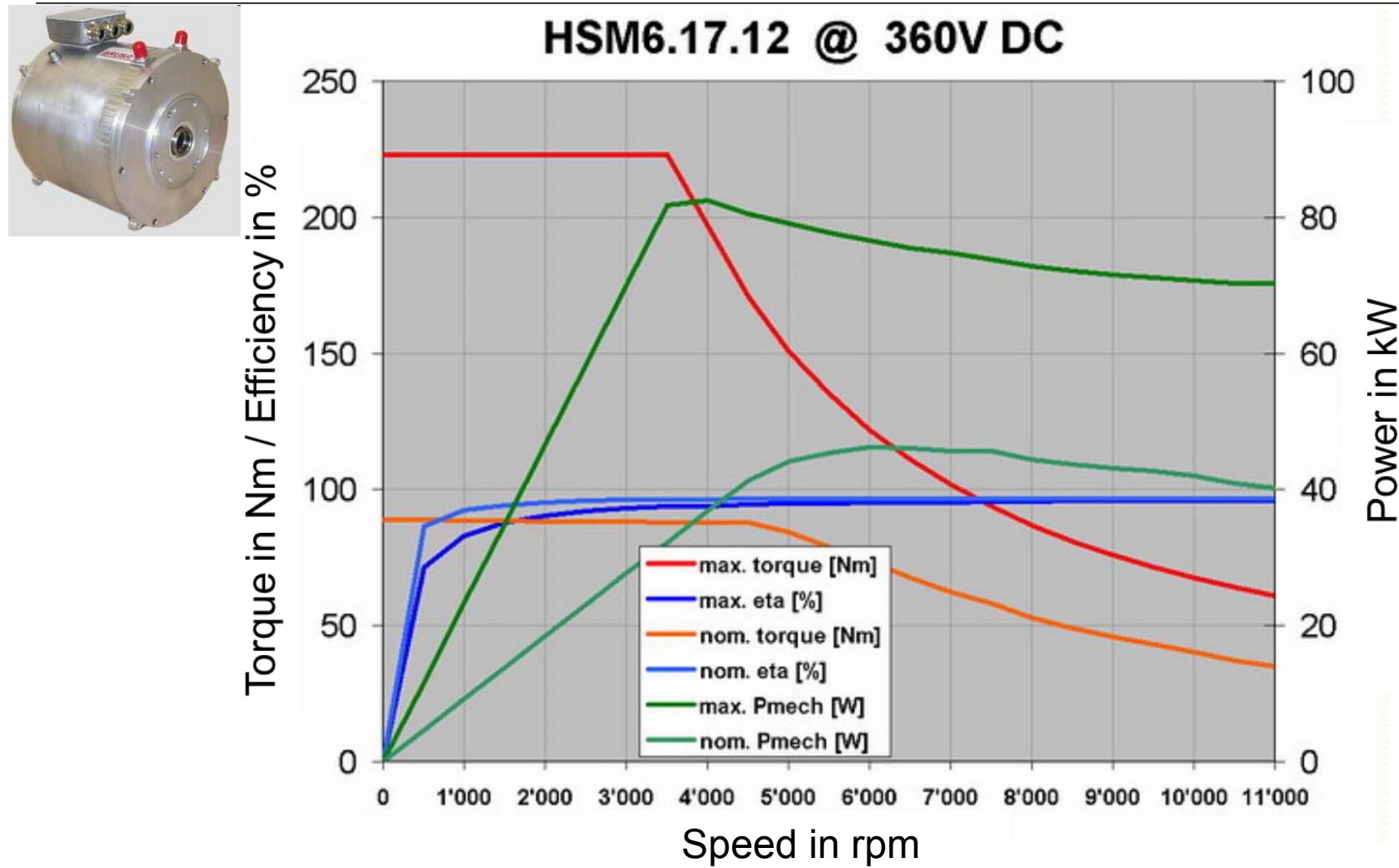


# Example: PM-synchronous machine

## Brusa - Torque-power curves



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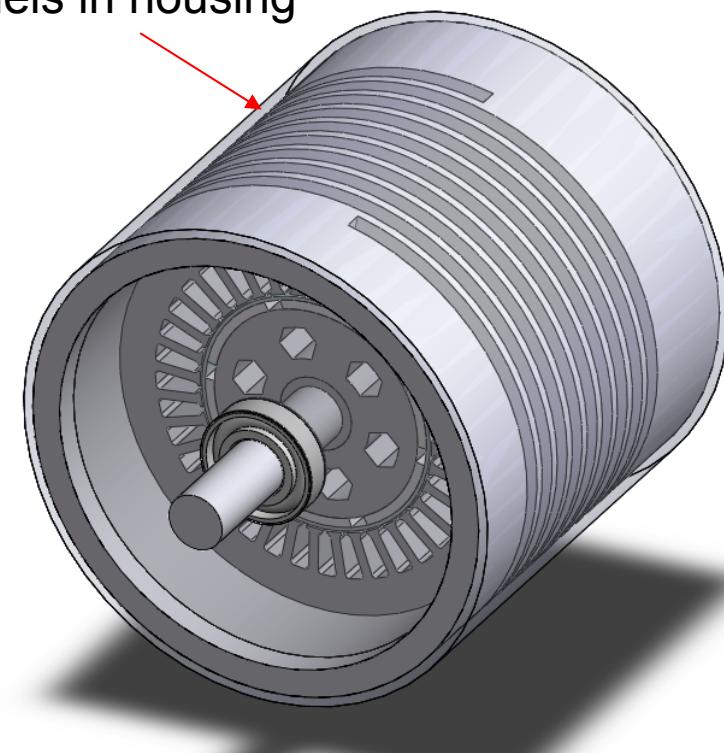
# Example: PM-synchronous machine **Brusa – Main dimensions (recalculated)**



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Geometric properties	
Outer length in mm	240
Diameter in mm	260
Rotor diameter in mm	114
Iron length in mm	120
Air gap length in mm	1
Bandage height mm	2
Magnet height in mm	5
Pole coverage ratio in %	0,85

Water jacket cooling in spiral  
channels in housing

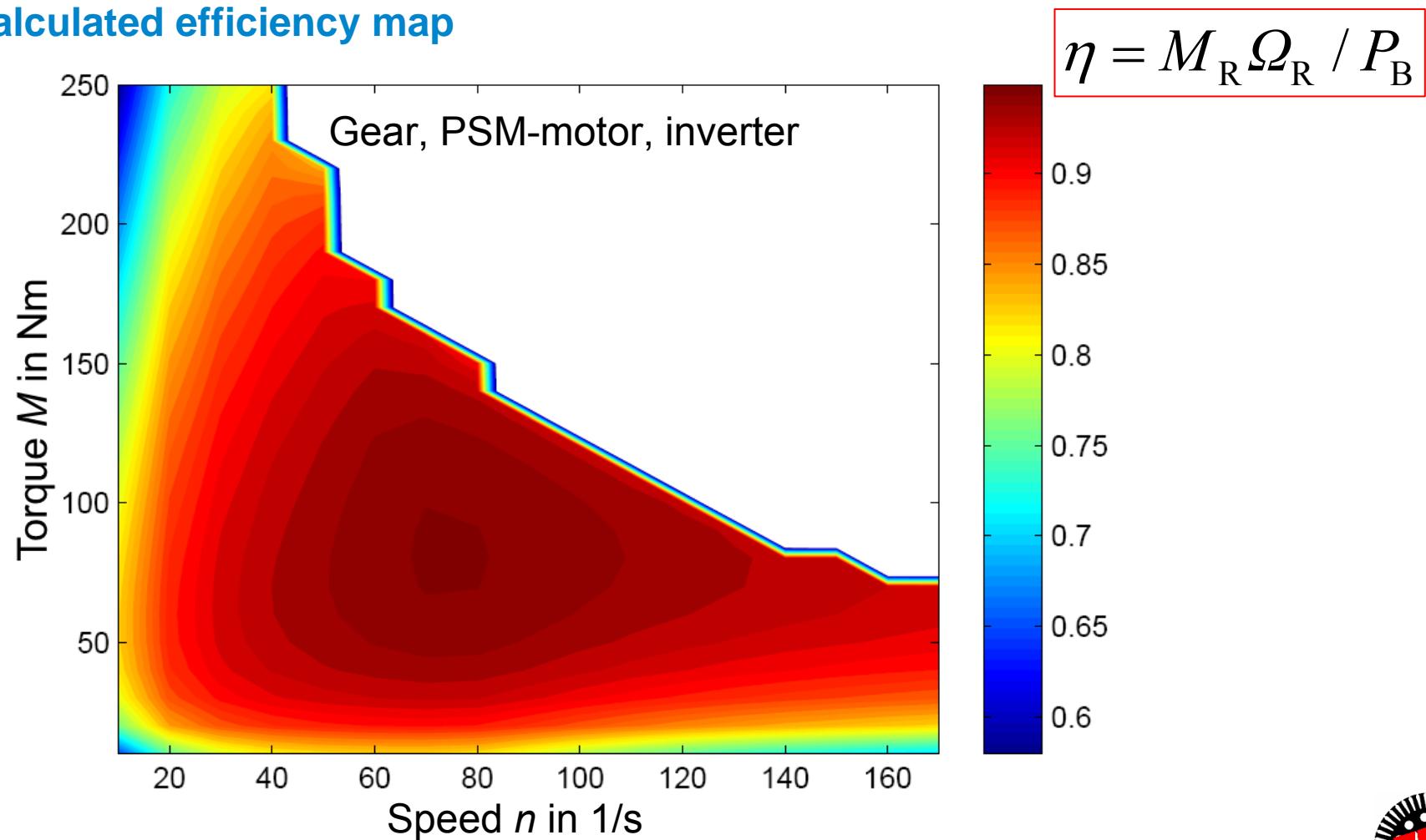


## Example: Efficiency of drive train – E-Motor + Inverter + Gear, Brusa



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Calculated efficiency map

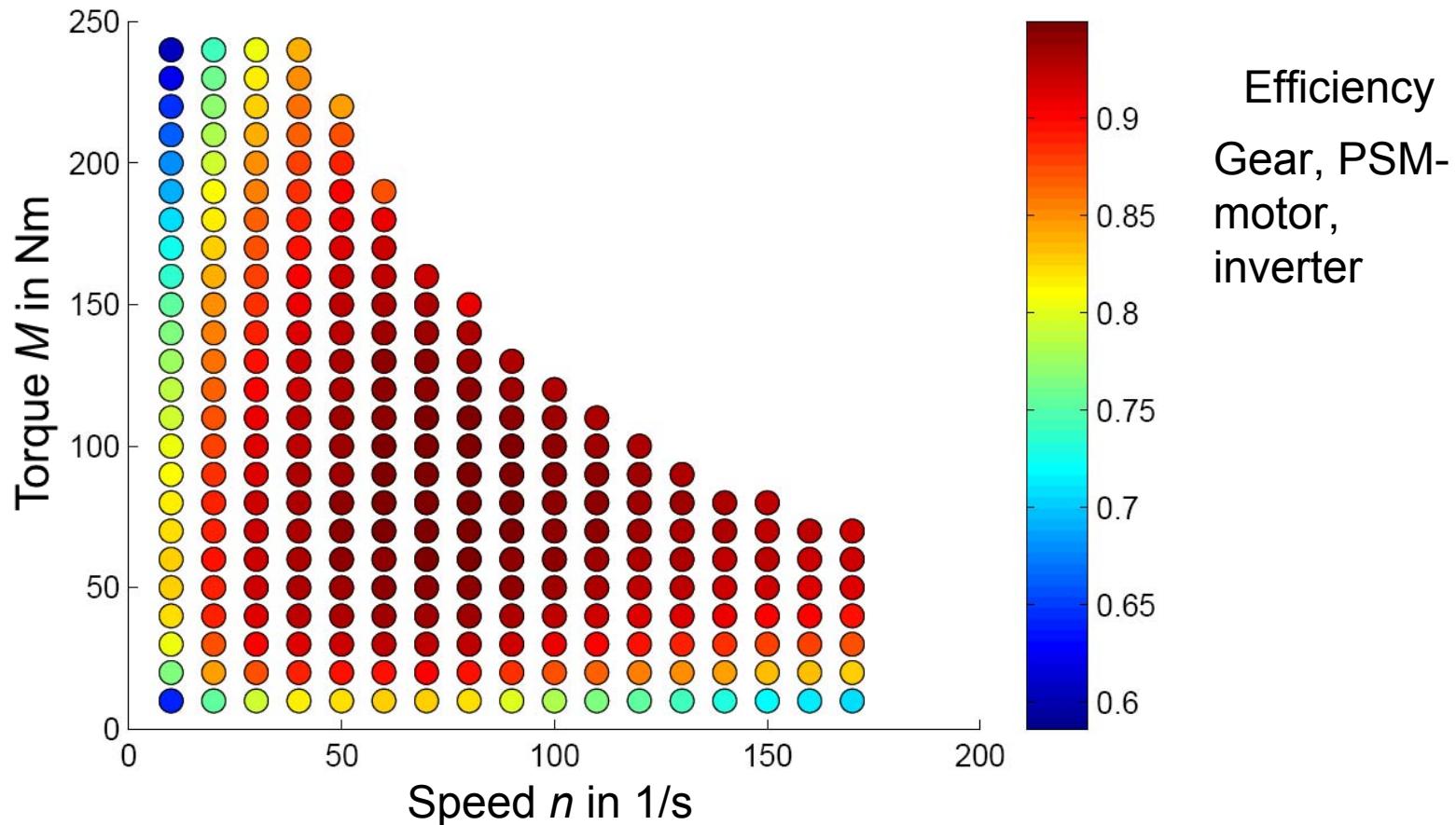


## Example: Efficiency of drive train – E-Motor + Inverter + Gear, Brusa



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- Screened efficiency map
- Steps of in 10 Nm and 10 1/s distances



# Example: PM-synchronous- and squirrel cage induction machines (Daimler)



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## PM-synchronous machine

### ■ Technical data electric machines

	PSM	ASM
Rated power $P_N$	20,5 kW	15 kW
Maximum power $P_{\max}$	42 kW	35 kW
Rated speed $n_N$	1500 min <sup>-1</sup>	2765 min <sup>-1</sup>
Maximum speed $n_{\max}$	6000 min <sup>-1</sup>	12500 min <sup>-1</sup>
Rated torque $M_N$	130 Nm	52 Nm
Maximum torque $M_{\max}$	270 Nm	120 Nm
Outer diameter $d_{sa}$	286 mm	150 mm
Iron length $l_{Fe}$	95 mm	180 mm
Coolant flow	8 l/min	8 l/min
Coolant supply temperature	85 °C	85 °C
Thermal class	H	H



Squirrel cage  
induction machine



# Loss groups for PM-synchronous - and squirrel cage induction machines



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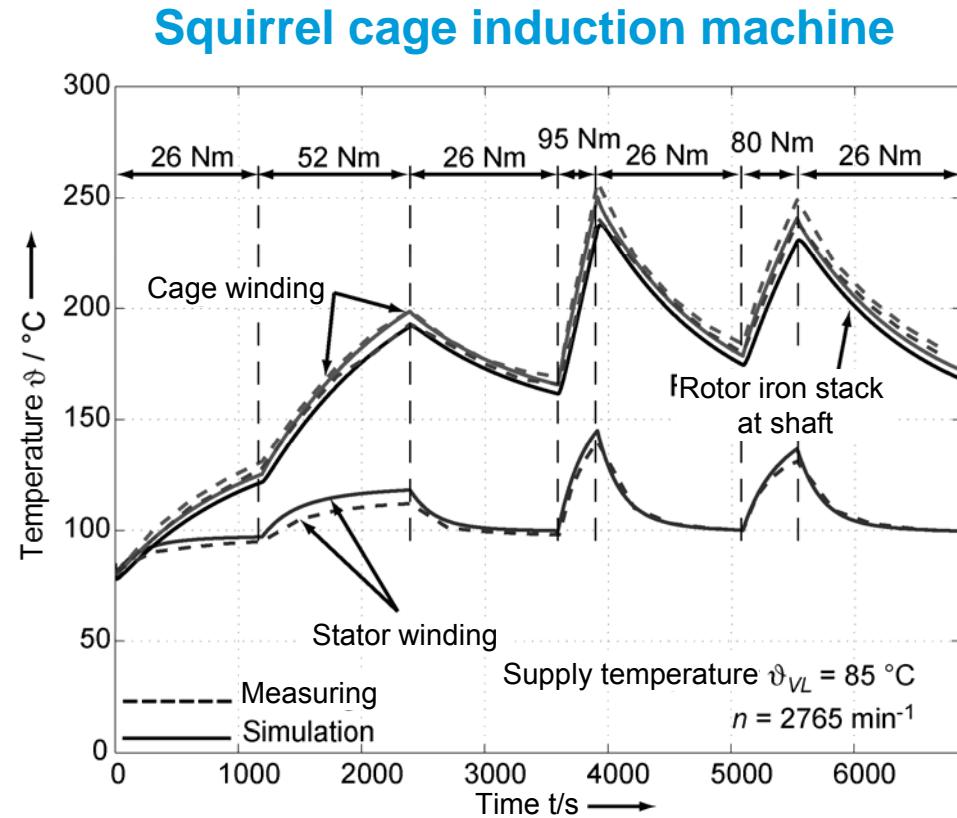
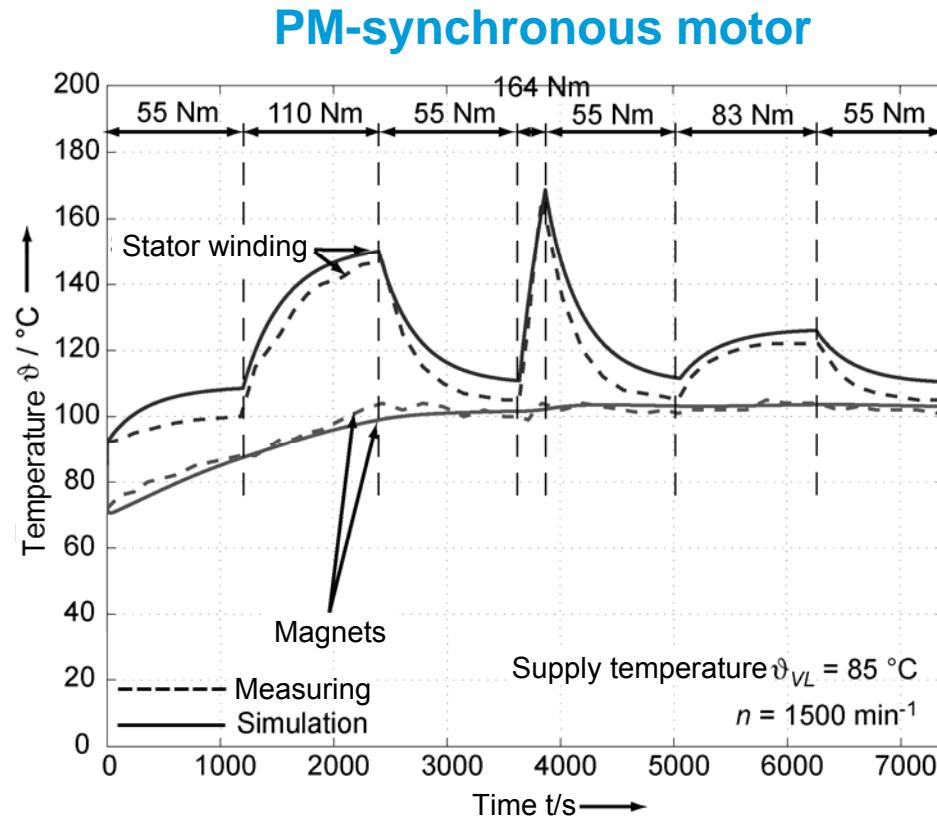
PM-synchronous machine	Squirrel cage induction machine
Stator ohmic losses	Stator ohmic losses
Iron losses	Iron losses
Losses in magnets and rotor	Rotor ohmic losses
	Additional losses for sinusoidal current operation
Ventilation- and bearing- friction losses	Ventilation- and bearing- friction losses
Additional losses in inverter	Additional losses in inverter

# Heating of PM-synchronous- and squirrel cage induction machines



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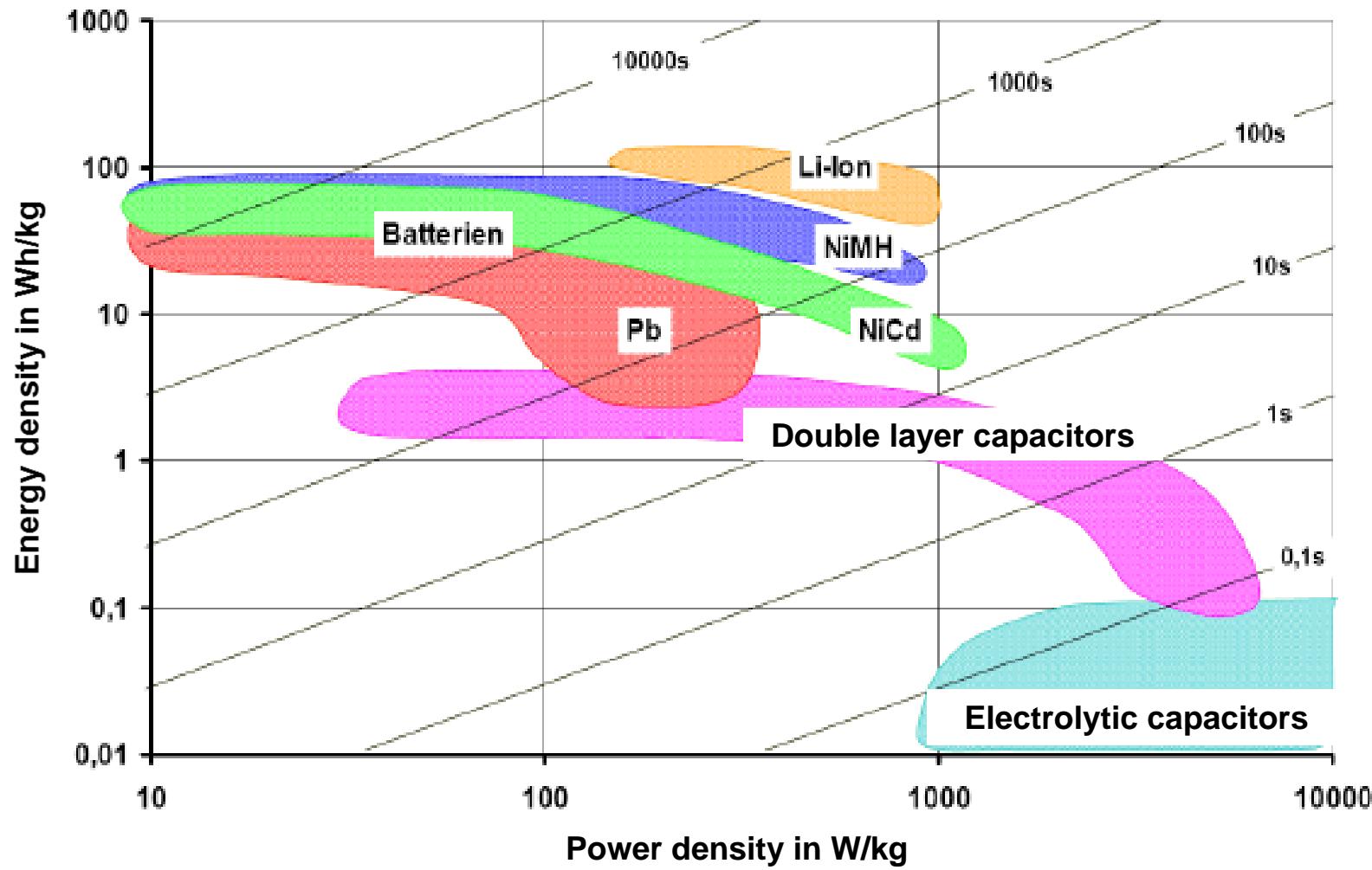
- Comparison calculation – Measuring (test rig) for driving example: constant speed, variable load



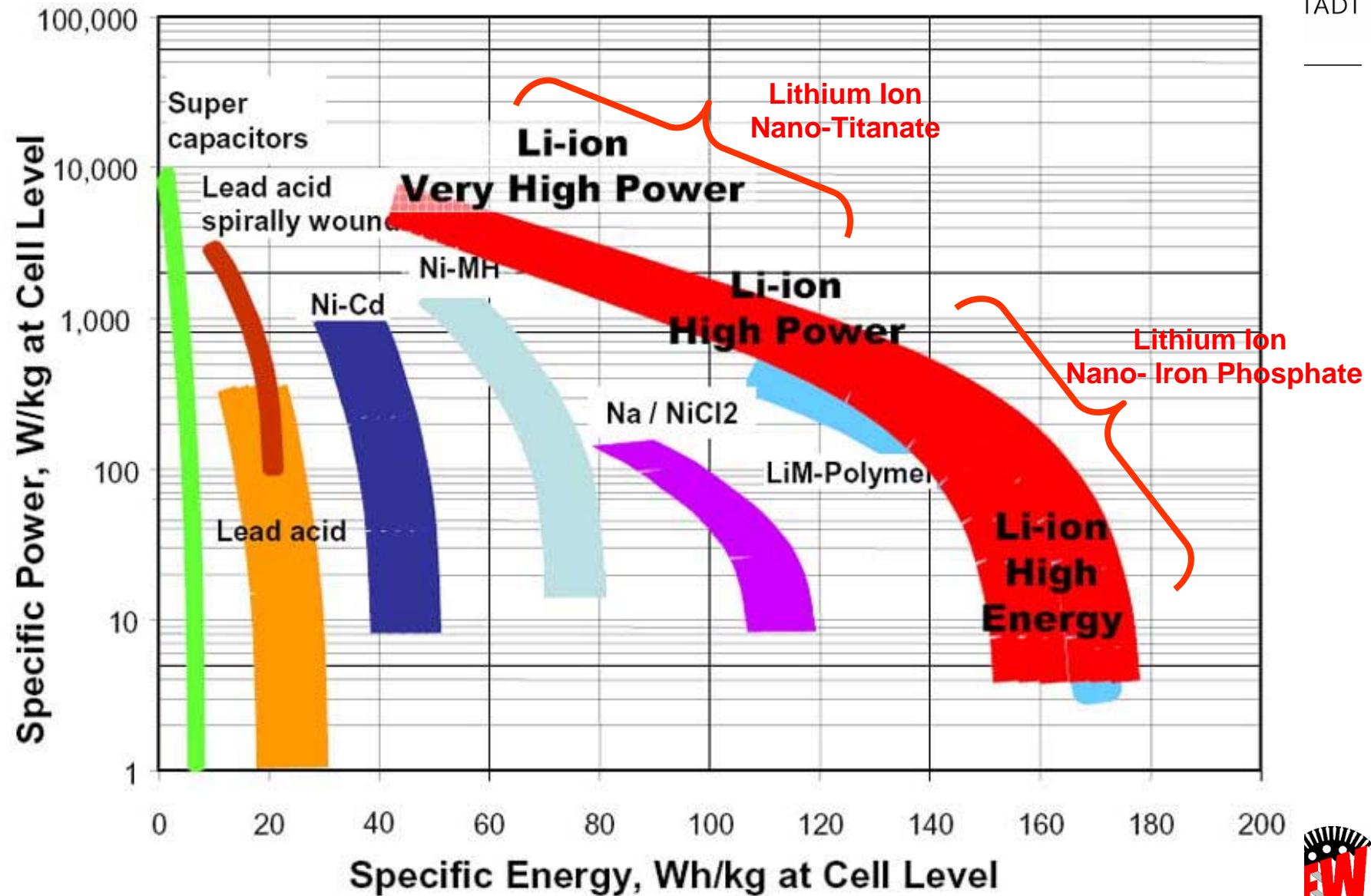
# Battery variants: *Ragone*-diagram



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# Battery variants: Energy & power density



# Lead batteries: VRLA (Valve-regulated lead acid)



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- designation for ‘maintenance-free lead-acid batteries’
- not really “sealed”, but vented for overpressure
- 2 types: Absorbed Glass Mat (AGM) or Gel battery
- use less electrolyte, less space than flooded designs
- high-rate power capacity (short duration)
- cost-effective, deep discharge, used in UPS systems
- 3-5 year life in heavy-duty vehicle service

Traditional choice  
for hybrid Electric  
transit vehicle  
designs

Low cost, rugged  
and field-proven



Typical VRLA batteries



VRLA Vehicle battery pack string

Can be combined  
with UltraCaps  
for greater power  
cycling capacity

# Lithium-ion (Li-ion)-batteries



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- compact, light weight, highest power density
- safety issues with older tech: cell phone/laptop types
- new nano-titanate cells handle 20,000 recharging cycles
- fast charge – up to 80% in one minute
- long life claims – 10+ years;
- new technology – cost is 4-to-5 x VRLA cost, for same power
- price will decrease as technology matures

High power, mid-energy density



Li-ion nano-titanate battery



“flat” wound cell  
2.3 V 11 A-h

High energy, mid-power cycling



Li-ion nano-iron phosphate battery



Spiral-wound cell  
3.3 V 2.3 A-h



# Data of Li-ion-batteries



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Properties	Lithium-ion	Lithium-polymer	Kokam
Conductance (20 °C) in mS/cm	2 – 5	0.05 – 0.5	0.05 – 0.5
No-load voltage in V	4.2	4.2	4.2
Rated voltage in V	3.7	3.7	3.7
Discharge lower limit voltage in V	2.5	2.7	2.7
Energy density (weight) in Wh/kg	90 – 160	130 – 144	136
Energy density (volume) in Wh/l	200 – 300	230 – 410	276
Power density in W/kg		300 – 1500	2700
Self discharge at 20 °C in %/month	5 – 10	2 – 8	2 – 8
Possible cycles	500 – 1200	500 – 1000	500 – 1000
Storage capability in a	5 – 10	5 – 10	5 – 10



# Example: Lithium-polymer-cells

## Kokam SLPB 98188216



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	1 cell	116-pack
Rated voltage in V	3.7	429.2
Rated discharge capacity in Ah	30	30
Rated charge current in A	30	30
Maximum discharge current in A	600	600
Cut-off voltage in V	2.7	313
Weight in kg	~ 0.82	~ 95



- 116-pack: 116 cells in series for height DC-link voltage
- Limitation of recuperation power to maximum 14,6 kW
- Weight is being increased by packaging, cooling, sensors and control devices

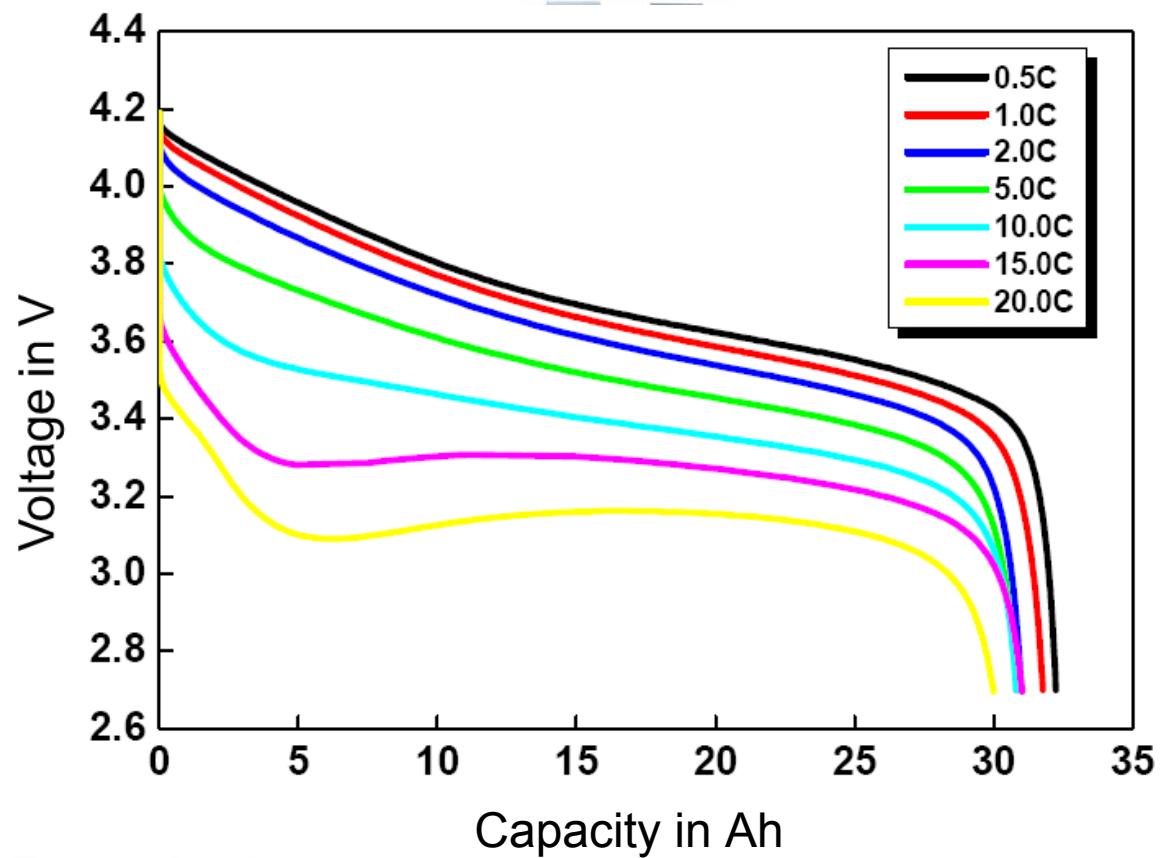
# Li-ion-batteries: Discharge characteristics



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## Calculation approach:

1. Determination of battery voltage and battery current
2. Calculation of losses
3. Change of SOC
4. Feed-back of DC-link voltage to power electronics

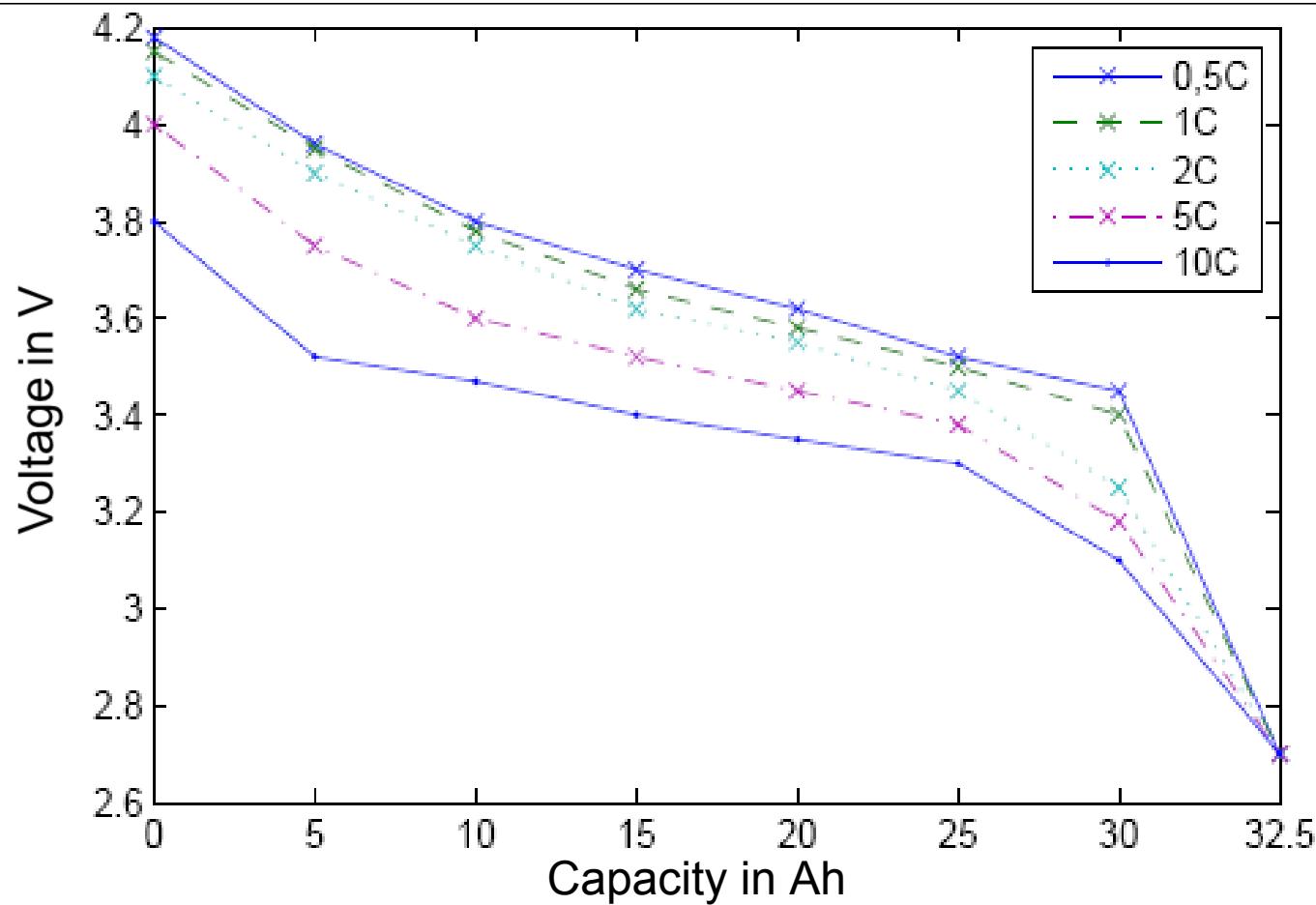


- Discharging rate of 1.0C equals to 30 A

# Li-ion-batteries *Kokam SLPB 98188216*: Discharge characteristics



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- Discharge rate of 1.0C equals to 30 A





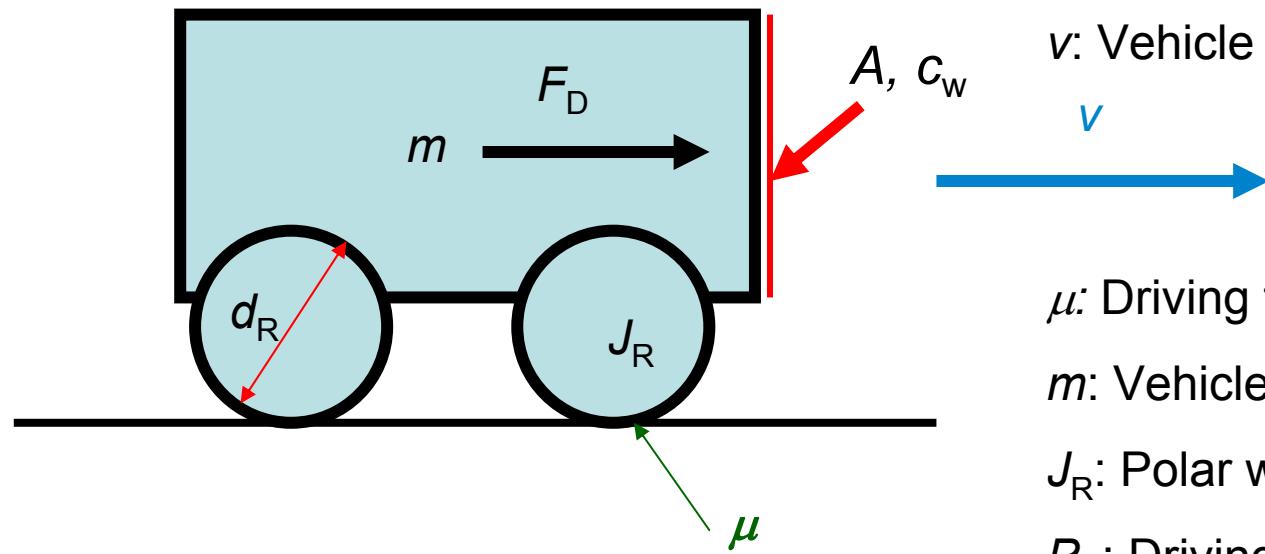
## **Electric vehicles – Simulation**

### **Vehicle - Track**

# Modeling of the vehicle



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$$P_D = F_D \cdot v$$

$A$ : Reference area

$c_w$ : Drag coefficient

$d_R$ : Wheel diameter

$v$ : Vehicle speed

$v$

$\mu$ : Driving traction coefficient

$m$ : Vehicle weight

$J_R$ : Polar wheel moment of inertia

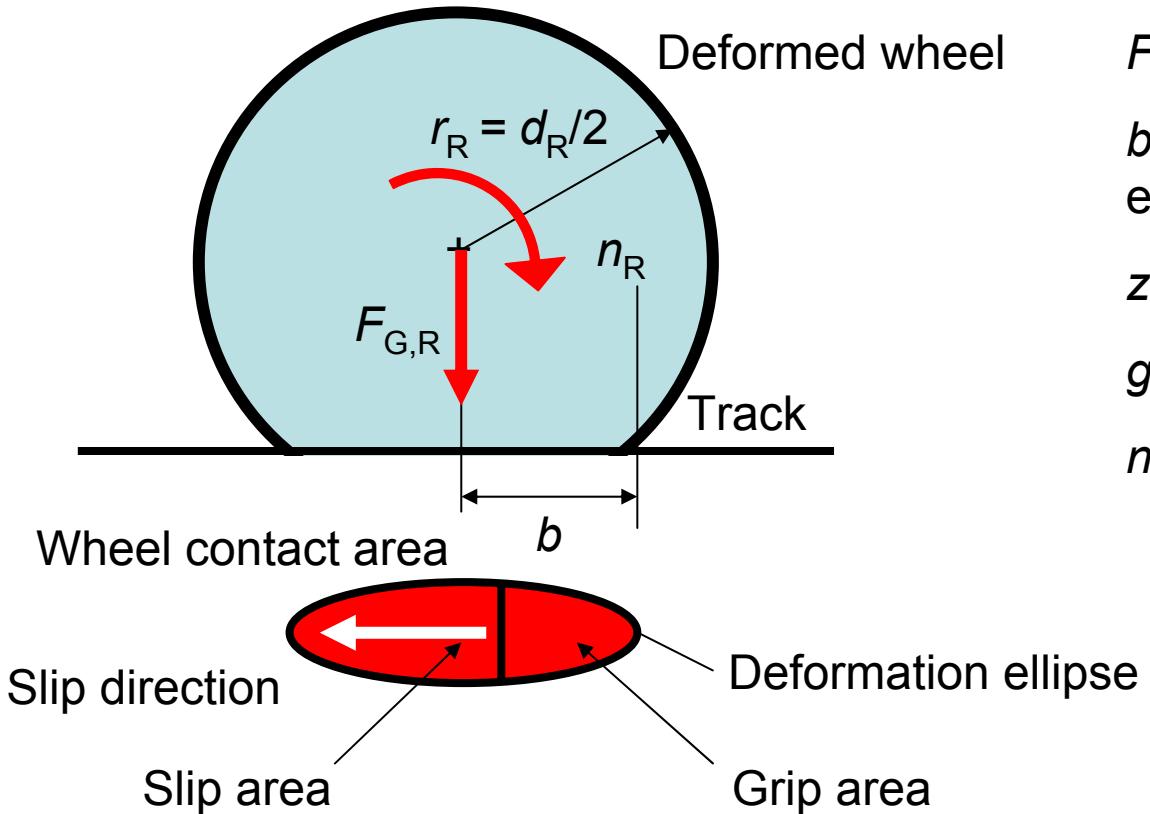
$P_D$ : Driving power

$F_D$ : Driving force in centroid of vehicle

# Wheel-track-contact



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$F_{G,R}$ : Normal force per wheel

$b$ : Big radius of deformation ellipse

$z_R$ : Number of wheels

$g$ : Gravitational acceleration

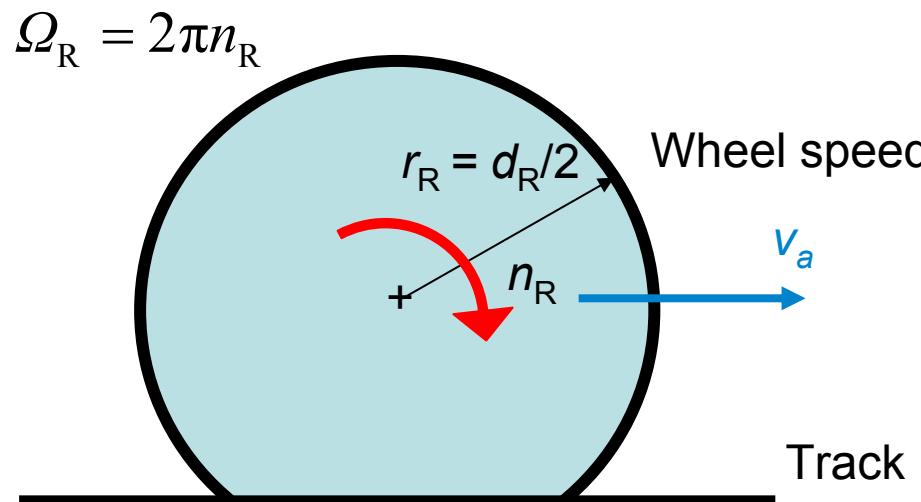
$n_R$ : Wheel speed

$$F_{G,R} = m \cdot g / z_R$$

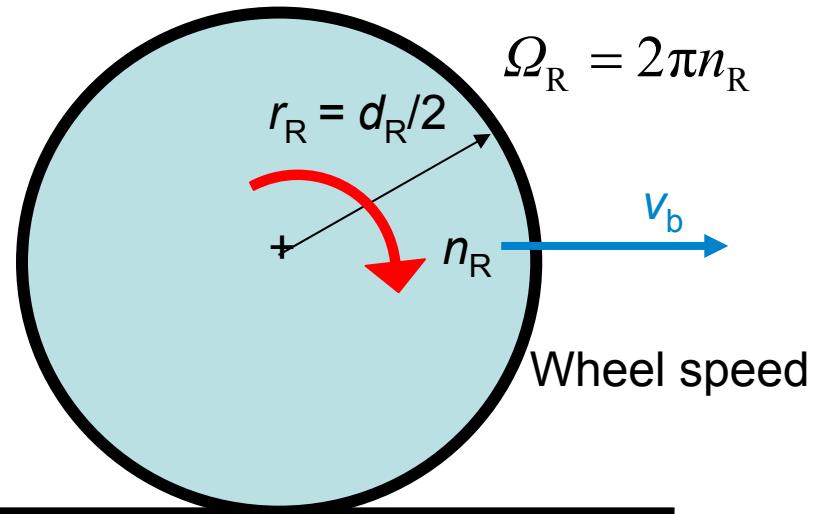
# Wheel slip s



Wheel WITH force transmission  
slip s between wheel and track



Wheel WITHOUT force transmission  
„purely rolling“ wheel, slip s = 0



$$\Omega = v_a / r_R$$

$$s = (\Omega_R - \Omega) / \Omega_R$$

Wheel speed  $v_a$  is SMALLER than the circumferential speed of wheel  $v_U$

$$v_a < v_U = d_R \pi n_R$$

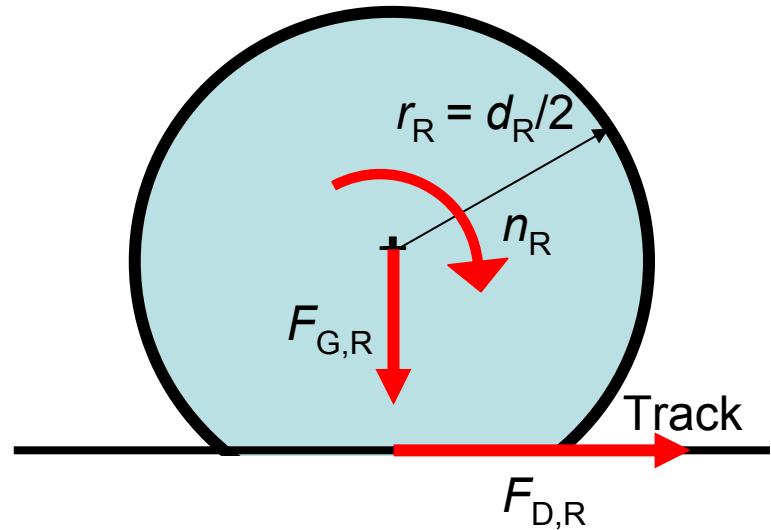
Wheel speed  $v_b$  = circumferential speed of wheel  $v_U$

$$v_b = v_U = d_R \pi n_R$$

# Transmittable Force $F_D$ from wheel to track



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DARMSTADT



Slope  $\tan \alpha$ :

$$F_{N,R} = F_{G,R} \cdot \cos \alpha$$

Maximum transmittable driving force per wheel:

$$F_{D,R,\max} = \mu(s) \cdot F_{N,R}$$

$\mu$ : Traction force coefficient

So that the wheels do not spin  
(„wheelspin“):

$$F_{D,R} \leq F_{A,R,\max}$$

$z_{R,D}$ : Number of driven wheels

Maximum transmittable driving force to the track:

Condition against wheel spin:  $F_D \leq F_{D,\max}$

$$F_{D,\max} = z_{R,D} \cdot F_{D,R,\max}$$

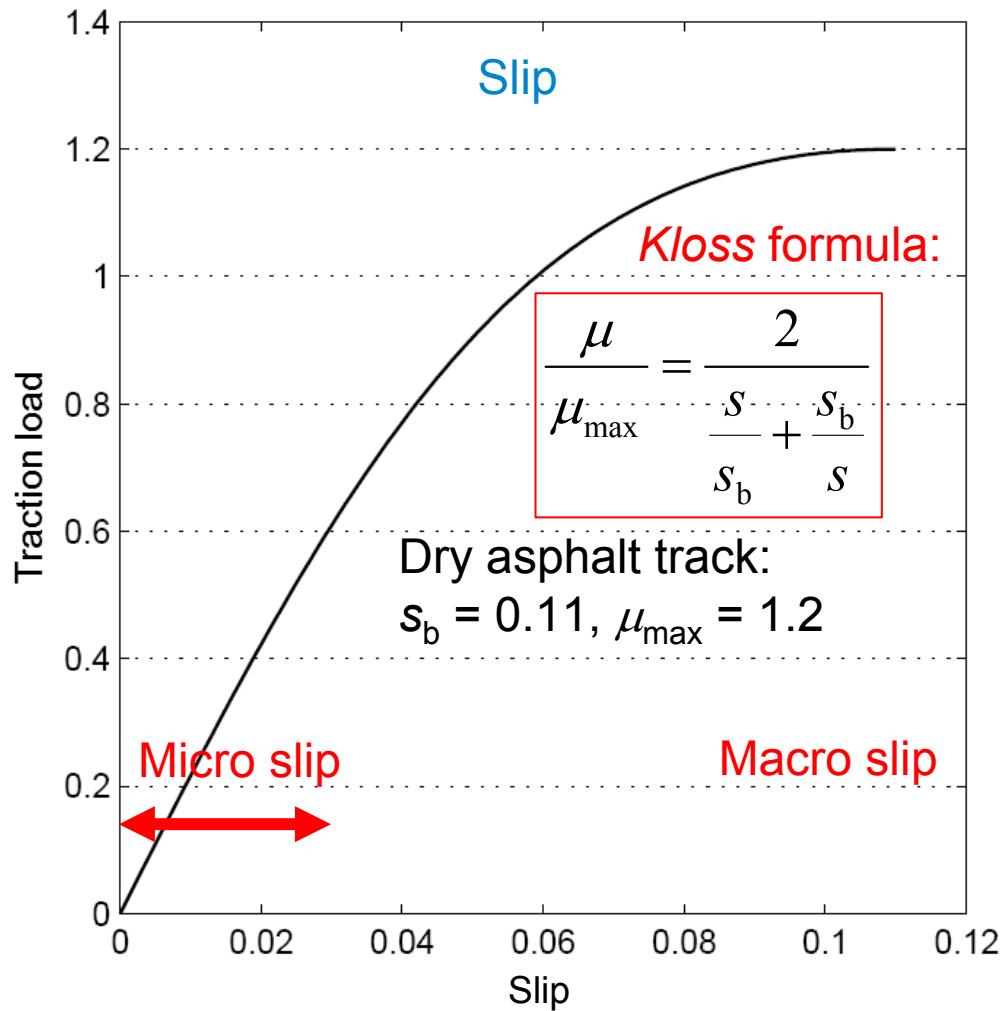


# Slip between wheel and track

## Simulation – Wheel / Track



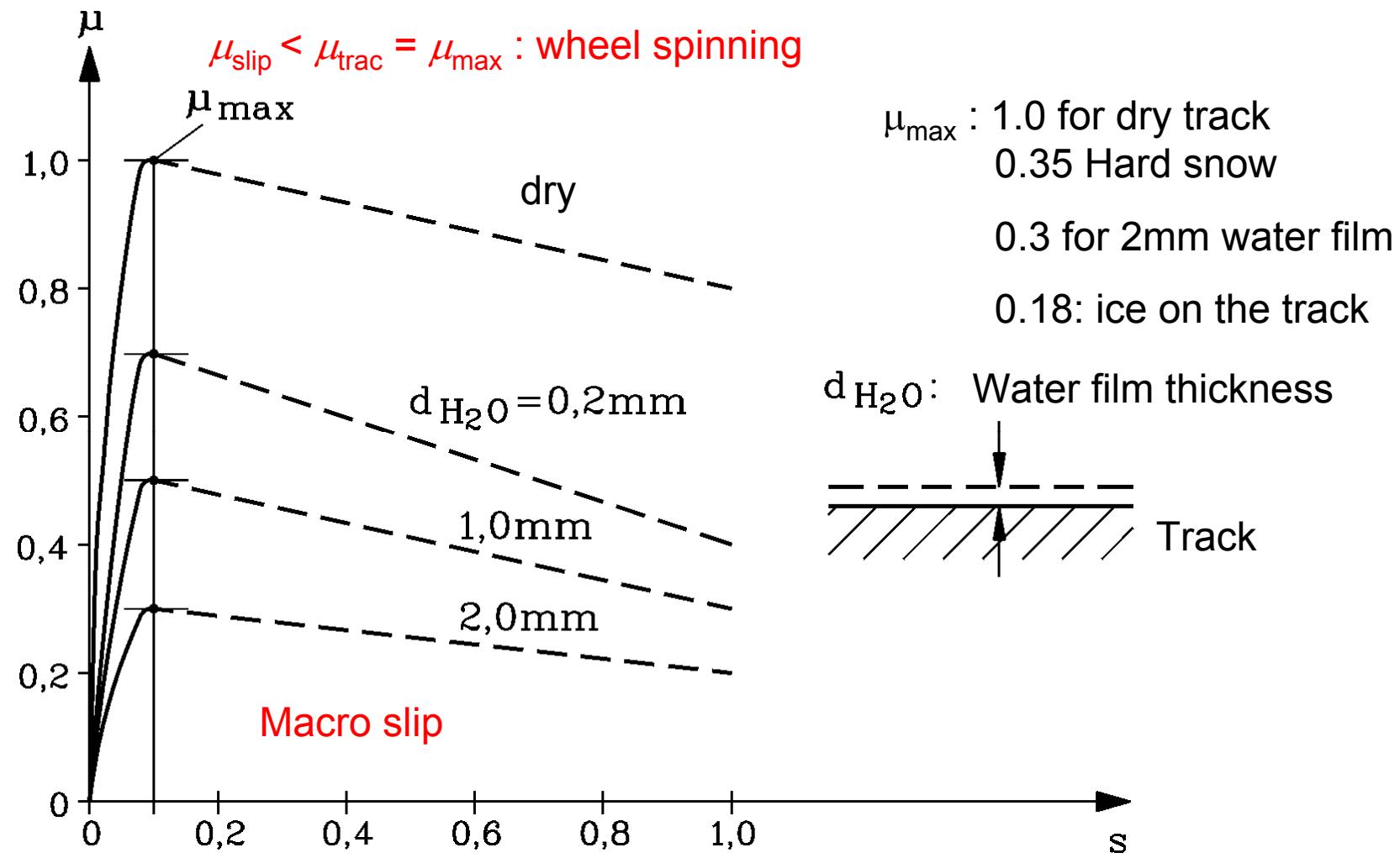
- Without slip → no transmission of force to track, only „pure“ rolling!
- With dry asphalt and good traction (summer wheels) at a slip of approx. 0.1 the maximum of **traction force coefficient  $\mu$**  of approx. 1.2 is reached.
- **Micro slip** up to approx. 3%: driving with constant speed
- **Macro slip:** > 10%: acceleration



# Traction coefficient $\mu$ and wheel slip $s$



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# Traction coefficient vs. slip



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## Kloss formula

$$\frac{\mu}{\mu_{\max}} = \frac{2}{\frac{s}{s_b} + \frac{s_b}{s}}$$

Dry asphalt track:  
 $s_b = 0.11, \mu_{\max} = 1.2$

## Empiric, more exact formula:

$$\mu = \mu_{\max} \cdot \left(1 - e^{-S_t \cdot s}\right) - \frac{A_b \cdot e^{W \cdot s}}{100 A_b + e^{W \cdot s} - 1} + 0.01 \quad 0 \leq s \leq 1$$

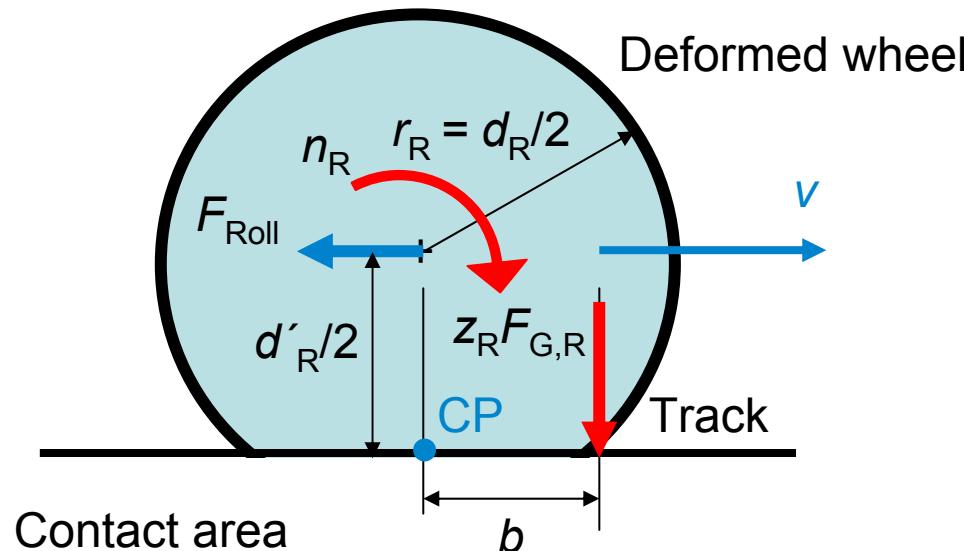
$S_t$ : slope of  $\mu(s)$ -curve for  $s = 0$                           (Value range: 10 ... 50)

$A_b$ : depression of  $\mu(s)$ -curve for  $s = 1$                           (Value range : 0 ...  $\mu_{\max}$ )

$W$ : inflection point    (Value range : 10 ... 100)

Dry asphalt track:  $S_t = 30, A_b = 0.3, W = 10$

# Rolling resistance $F_{\text{Roll}}$ of all wheels



$F_G$ : Normal force on all wheels

$b$ : Big radius of deformed ellipsis

$g$ : Gravitational acceleration

$n_R$ : Wheel speed

CP: Contact point

$\alpha$ : Slope angle of track

Torque balance:  $d'_R < d_R$

$$F_{\text{Roll}} \cdot d'_R / 2 = z_R F_{G,R} \cdot b_R$$

$$F_G = m \cdot g \quad F_N = F_G \cdot \cos \alpha$$

$$d'_R \approx d_R :$$

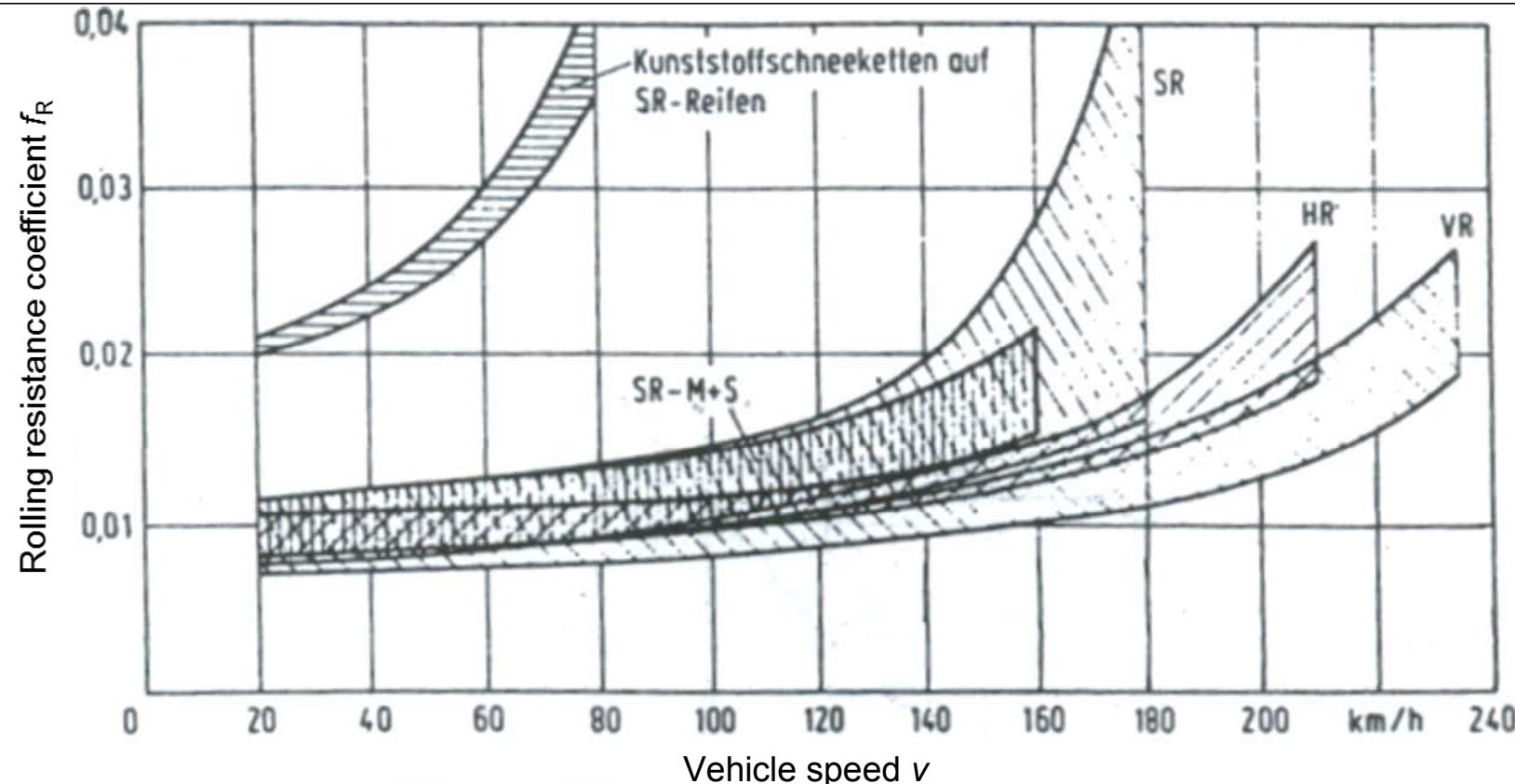
$$F_{\text{Roll}} = (2b / d_R) \cdot F_N = f_R \cdot F_N$$

Rolling resistance coefficient  $f_R = f_R(v)$  due to deformation work of wheels :

Depends on vehicle speed and wheel property



# Rolling resistance coefficient of tyres

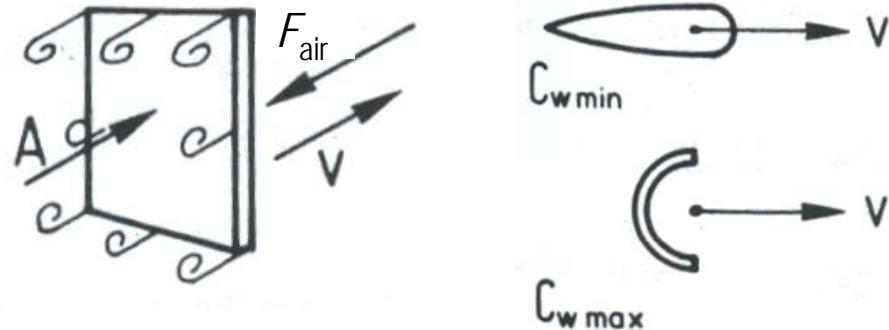


Example: no slope:  $F_G = 8000 \text{ N}$  (weight: 800 kg),  $f_R = b/r_R = 0.01$ ,  $F_{\text{Roll}} = 80 \text{ N}$

$$f_R = f_{R0} + f_{R1} \cdot (v/v_0) + f_{R4} \cdot (v/v_0)^4 \quad v_0 = 27.8 \text{ m/s} = 100 \text{ km/h}$$
$$f_{R0} = 0.009, f_{R1} = 0.0015, f_{R4} = 0.0012$$



# Air resistance $F_{\text{air}}$



A: Reference area

$\rho_{\text{Air}}$ : Density of air

v: Vehicle speed

$c_w$ : Drag coefficient

$c_w$ -values person cars: 0.2 ... 0.5

$$\rho_{\text{Air}, 20^\circ C} = 1.202 \text{ kg/m}^3$$

Vehicle speed  $v$  equals the negative air speed for non-moving air

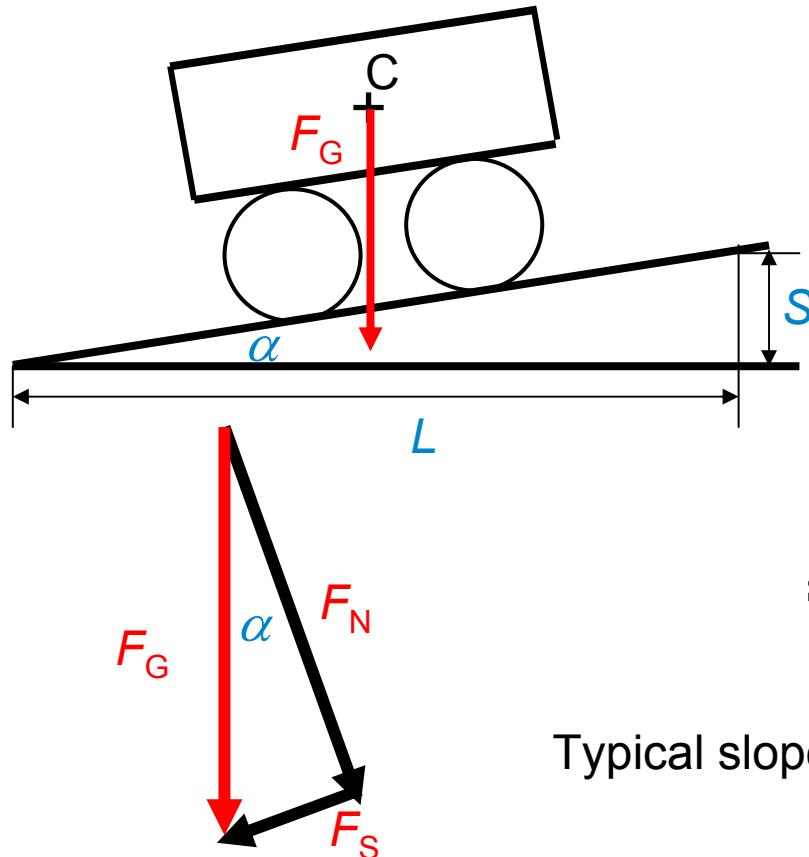
Ram pressure:  $p_{\text{Ram}} = \rho_{\text{Air}} v^2 / 2$

Air resistance force:

$$F_{\text{Air}} = (c_w A) \rho_{\text{Air}} v^2 / 2$$

Example: VW-Golf:  $c_w A = 0.56 \text{ m}^2$ ,  $c_w = 0.4$

# Slope resistance $F_S$



$$\text{Slope: } \tan \alpha = S / L$$

C: Centroid

$$F_N: \text{Normal force } F_N = F_G \cdot \cos \alpha$$

$F_S$ : Downhill force =  
slope resistance:

$$F_S = F_G \cdot \sin \alpha$$

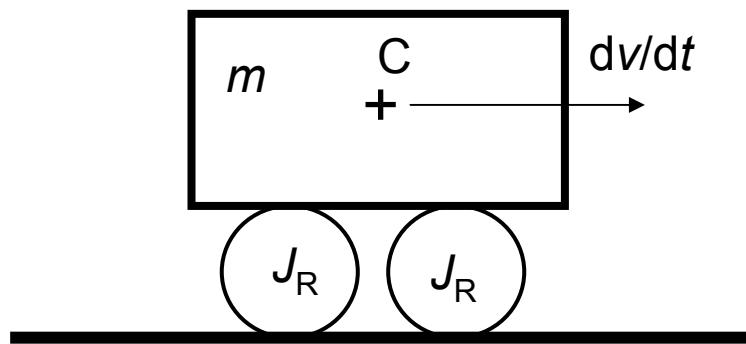
$$\sin \alpha = \frac{S}{\sqrt{S^2 + L^2}} \approx \frac{S}{L} = \tan \alpha, \quad S \ll L$$

Typical slope of track:  $S/L = 0 \dots 25\%$

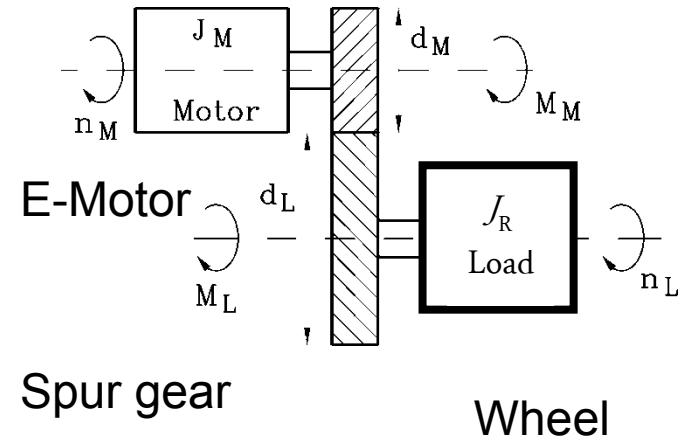
Example: Slope Turracher Höhe (Carinthia, Austria):  $\tan \alpha = 0.22 = 22\%$

# Vehicle acceleration force $dv/dt$

Vehicle:



Drive:



Vehicle acceleration:  $dv/dt$

Acceleration of linearly moved masses:  $F_a = m \cdot dv / dt$

Acceleration of rotating masses (wheels, gear, E-motor):  $M_a = J \cdot d\Omega / dt$   
(torque  $M$  necessary)

Maximum permitted acceleration („comfort“):  $(dv/dt)_{max} = 2m/s^2 \approx 0.2 g$

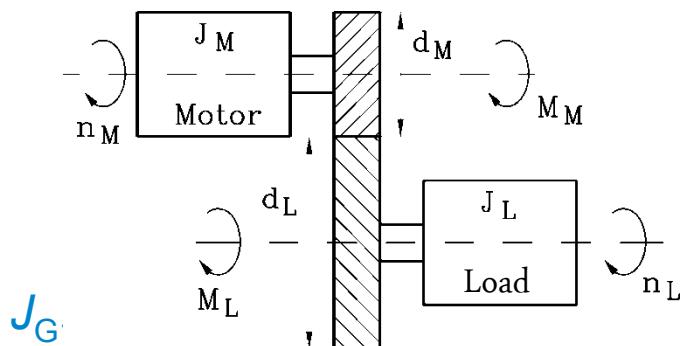
# Rotating mass adding factor $\Delta$



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Total kinetic energy:

$$W_{\text{kin}} = \frac{mv^2}{2} + \frac{(z_R J_R + J_{G1})\Omega_R^2}{2} + \frac{(J_M + J_{G2})\Omega_M^2}{2} = \frac{m' \cdot v^2}{2}$$



$n_L = n_R$ , „load“ = driven wheels of driven axle

Equivalent linear accelerated mass  $m'$ :

$$m' = m \cdot (1 + \Delta)$$

Typical value for the share of the rotating masses to be accelerated by kinetic energy:  $\Delta = 0.2$

Acceleration force  $F_a$ :

$$F_a = m' \cdot (\text{d}v / \text{dt})$$



## Bearing friction $F_{Bg}$

Per wheel:  $F_{Bg,R} = F_{G,R} \cdot k_{Bg}$

Per vehicle:  $F_{Bg} = z_R F_{G,R} \cdot k_{Bg} = m \cdot g \cdot k_{Bg}$

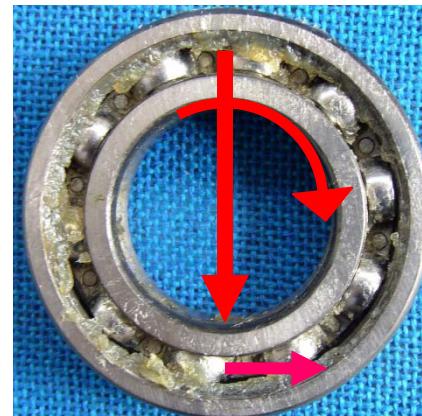
Example:

$$m = 1500 \text{ kg}$$

$$F_{Bg} = 73.5 \text{ N}$$

**Per wheel: Bearing force**

$$F_{G,R}$$



**Wheel speed  $n_R$**

Example:

Ball bearing

**Braking bearing friction  
force  $F_{Bg,R}$**

Friction coefficient  $k_{Bg} = 0.005$  as an estimation !

Depending on type of bearing, state of lubrication, age, bearing load, and wheel speed this value is varying and can be calculated according to exact formulas!



# Demanded driving force $F_D$ and power $P_D$



1) Steady state operation:  $dv/dt = 0$ :  $F_{D,\text{steady}} = F_{\text{Roll}} + F_{\text{Air}} + F_S + F_{\text{Bg}}$

2) Non-steady-state:  $dv/dt \neq 0$ :  $F_{D,\text{non-steady}} = m' \cdot (dv / dt) + F_{\text{Roll}} + F_{\text{Air}} + F_S + F_{\text{Bg}}$

Accelerating:  $dv / dt > 0$

Braking:  $dv / dt < 0$

3) Driving power  $P_D = F_D v$ : steady state:  $P_{D,\text{steady}} = F_{D,\text{stat}} v = (F_{\text{Roll}} + F_{\text{Air}} + F_S + F_{\text{Bg}}) \cdot v$

$$P_{D,\text{stat}} = [(f_R + \tan \alpha) \cdot F_N + F_{\text{Bg}}] \cdot v + c_w A \frac{\rho_L}{2} v^3$$

Dominating at:

low speed

high speed

4) Driving energy in driving example (time period  $t_2 - t_1$ ):

$$W_D = \int_{t_1}^{t_2} P_D(t) \cdot dt$$



## Example: Driving force $F_A$



Data:  $m = 1500 \text{ kg}$ ,  $v = 80 \text{ km/h}$ ,  $f_R = 0.01$ ,  $c_w A = 0.56 \text{ m}^2$

- a) Rain-wet asphalt:  $\mu_{\max} = 0.5$  at  $s_b = 0.11$ ,  
Acceleration:  $dv/dt = 1 \text{ m/s}^2$ ,  $\Delta = 0.2$ ,  
Slope 10%
- b) Dry asphalt:  $\mu_{\max} = 1.2$  at  $s_b = 0.11$ ,  
No acceleration:  $dv/dt = 0$   
No slope

$$F_G = 14700 \text{ N}, F_{Bg} = 73.5 \text{ N}, F_{Air} = 166 \text{ N}$$

a)  $F_N = 14627 \text{ N}, F_{Roll} = 146 \text{ N}, F_S = 1463 \text{ N}, F_B = 1800 \text{ N}$

$$F_D = F_B + F_S + F_{Roll} + F_{Air} + F_{Bg} = 3648 \text{ N}$$

b)  $F_N = 14700 \text{ N}, F_{Roll} = 147 \text{ N}, F_S = 0, F_B = 0$

$$F_D = F_{Roll} + F_{Air} + F_{Bg} = 386.5 \text{ N}$$



# Slip losses



- $\mu_{\max}$  at  $s_b$  result for a given **state of track**.
- For demanded driving force and vehicle weight resp. slope a **needed traction force coefficient  $\mu$**  concludes. For sym. Centroid location and two axles:

$$F_{N,\text{axle}} = m \cdot g \cdot \cos \alpha / 2$$

$$\text{1 driven axle: } \mu = F_D / F_{N,\text{axle}}$$

- From above the **wheel slip** is determined with the aid of  $\mu(s)$ -curve or from der **Kloss function**:

$$\frac{s}{s_b} = \frac{\mu_{\max}}{\mu} - \sqrt{\left(\frac{\mu_{\max}}{\mu}\right)^2 - 1}$$

- Due to the wheel slip the friction power occurs as **slip power  $P_{\text{sl}}$** . Hence the driving power equals the mechanic power  $P_m$  at the driving wheels reduced by this slip power  $P_{\text{sl}}$ .

$$P_{\text{sl}} = s \cdot P_m \quad P_D = (1-s) \cdot P_m$$

**Slip losses = friction heat = slip power  $P_{\text{sl}}$ :**

**Braking slip force:**  $F_{\text{sl}} = P_{\text{sl}} / v$

$$P_{\text{sl}} = \frac{s}{1-s} \cdot P_D$$



# Example: Slip losses



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Data:  $m = 1500 \text{ kg}$ ,  $v = 80 \text{ km/h}$ ,  $f_R = 0.01$ ,  $c_w A = 0.56 \text{ m}^2$

- a) Rain-wet asphalt:  $\mu_{\max} = 0.5$  at  $s_b = 0.11$ , acceleration:  $dv/dt = 1 \text{ m/s}^2$ ,  $\Delta = 0.2$ , slope 10%,  $F_D = 3648 \text{ N}$
- b) Dry asphalt:  $\mu_{\max} = 1.2$  at  $s_b = 0.11$ , no acceleration:  $dv/dt = 0$  no slope,  $F_D = 386.5 \text{ N}$

- a)  $F_{N,\text{axle}} = 14641 \text{ N}$ ,  $\mu = 3648/14641 = 0.249$ ,  $s = 0.0292$ ,  
 $P_D = F_D v = 81067 \text{ W}$ ,  $P_{sl} = 2438 \text{ W}$ , braking force:  $F_{sl} = 109.7 \text{ N} = 3\% \text{ von } F_D$
- b)  $F_{N,\text{axle}} = 14700 \text{ N}$ ,  $\mu = 386.5/14700 = 0.0263$ ,  $s = 0.011$ ,  
 $P_D = F_D v = 8589 \text{ W}$ ,  $P_{sl} = 94 \text{ W}$ , braking force:  $F_{sl} = 4.2 \text{ N} = 1.1\% \text{ von } F_D$

## **Conclusion:**

*Slip losses can be neglected for normal driving conditions in the range of micro slip!*





## **Electric vehicles – Simulation of the drive components**

# Single-stage gear



$$v_{U,Gr} = d_M \pi n_M = d_R \pi n_R$$

$$i = n_M / n_R = d_R / d_M$$

$$F_{Gt} = 2M_M / d_M = 2M_R / d_R$$

$$i = M_R / M_M \quad M_M = M_R / i$$

Speed-dependent loss torque due to oil viscosity:  $M_{d0} = p_0 M_N$

Load-dependent loss torque due to tooth meshing:  $M_{d1} = p_1 M_N$

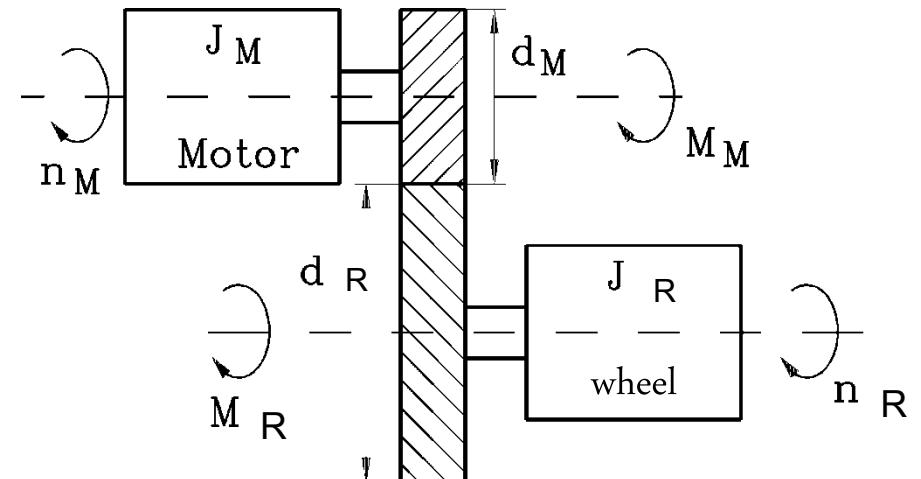
$m$  = torque/rated torque =  $M/M_N$

$v$  = speed/rated speed =  $n/n_N$

$$\eta_G = \frac{P_{out}}{P_{in}} = \frac{M_{out} 2\pi n_M}{M_{in} 2\pi n_M} = \frac{M}{M + v \cdot M_{d0} + m \cdot M_{d1}} = \frac{m}{m + v \cdot p_0 + m \cdot p_1}$$

Single-stage reduction gear (spur gear)

$i = n_M / n_R$  : transmission ratio



Example:  $p_0 = 0.011$ ,  $p_1 = 0.0043$ ,  $\eta_{GN} = 0.9849$

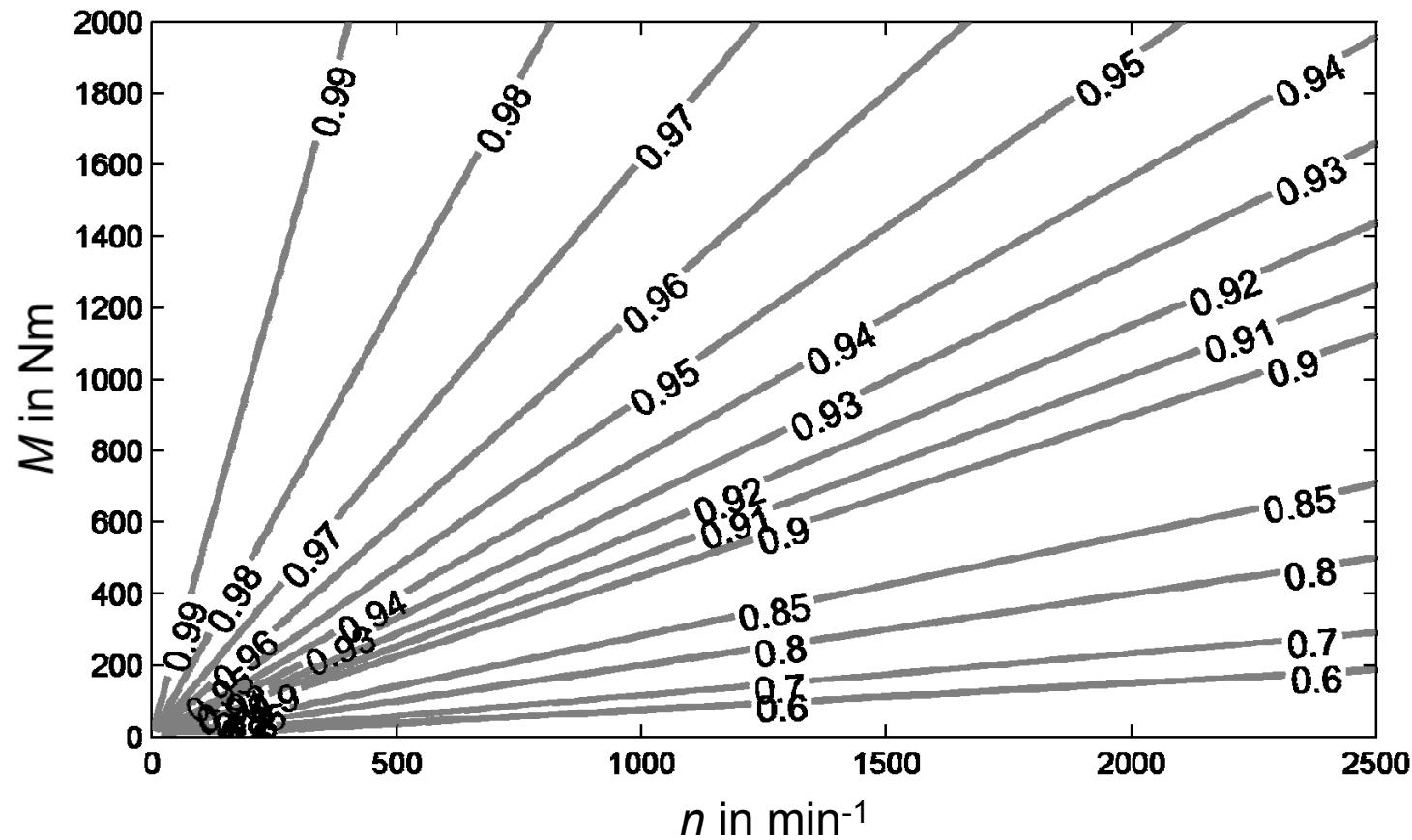


# Gear efficiency



- Gear efficiency

Single-stage reduction gear  
 $i = 1/8$ , spur gear (helical gear)



# Power requirement to the driving motor



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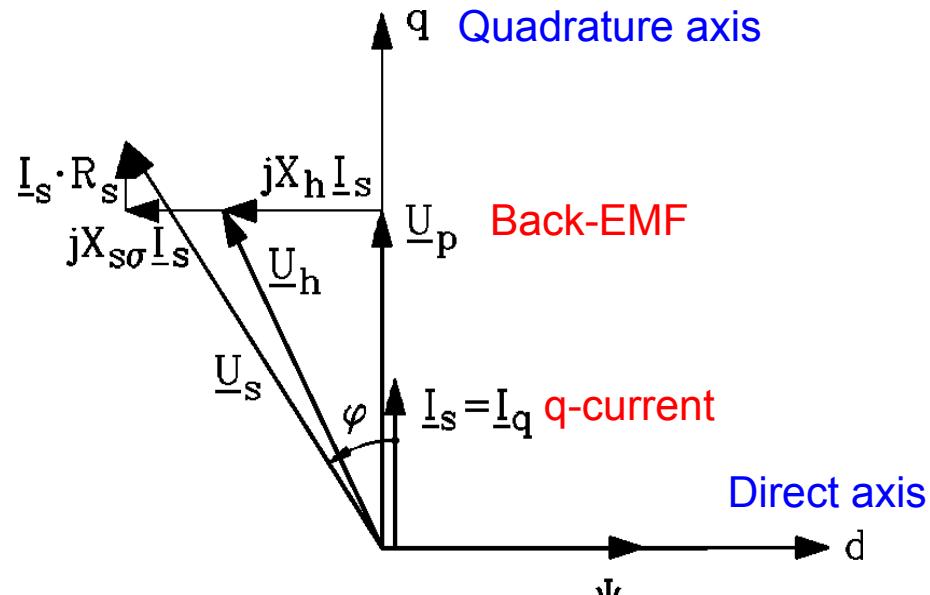
Wheel torque from driving force:  $F_D = M_R / (d_R / 2)$

Wheel speed from vehicle speed and wheel slip:  $n_R = \frac{v}{d_R \pi \cdot (1-s)}$

Motor torque over gear and its loss torque:  $M_M = M_R / (i \cdot \eta_G)$

Motor speed over gear:  $n_M = n_R \cdot i$

# PM-synchronous motor – Field oriented operation



$R_s$ : Stator resistance

$X_h, X_{s\sigma}$ : Reactance (main- and stray- ( $h + \sigma$ ))

$U_s = U_{s1}$ : Phase voltage (RMS, fundamental)

- Stator current is **DIRECTLY** proportional to torque  $M_e$

- Speed is proportional to stator frequency

$$M_e = \frac{P_\delta}{\Omega_{\text{syn}}} = m \cdot p \cdot \frac{\Psi_p}{\sqrt{2}} \cdot I_s$$

$M_e$ : El. torque

$P_\delta$ : Internal power

$\Omega_{\text{syn}}$ : Synchronous speed

$m = 3$ : Number of phases

$p$ : Number of pole pairs

$\Psi_p$ : Flux linkage (peak)

$I_s = I_{s1}$ : Stator phase current (RMS)

$U_p$ : back-EMF (RMS)

$$n = f_s / p$$

# PM-synchronous motor – Operation at full flux



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$$M_e = \frac{P_\delta}{\Omega_{\text{syn}}} = m \cdot p \cdot \frac{\Psi_p}{\sqrt{2}} \cdot I_s = k_T I_s \quad k_T = m \cdot p \cdot \frac{\Psi_p}{\sqrt{2}}$$

Torque constant: Nm/A

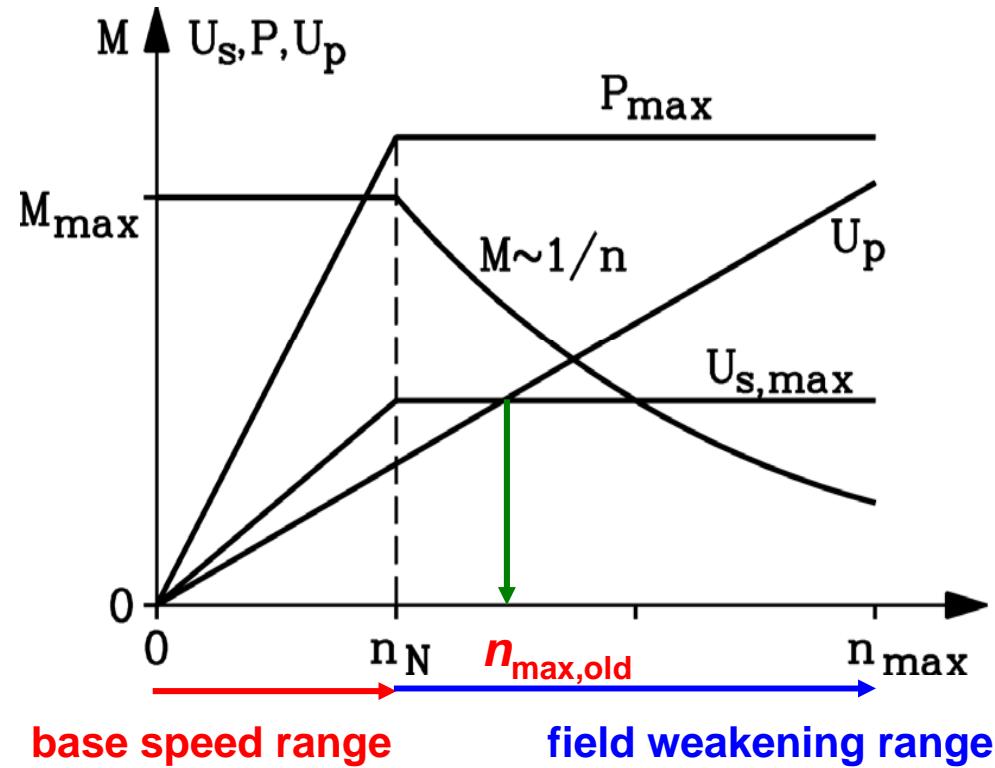
$$k_T = m \cdot p \cdot \frac{\Psi_p}{\sqrt{2}}$$

Field oriented operation: PM-synchronous motor with  $I_q$  impressing:

- a) Thermal continuous torque: Rated torque  $M_N$  at  $n_N$ 
  - Ohmic losses  $P_{Cu}$
  - Iron losses  $P_{Fe,s+r}$ ,
  - Magnet- and friction losses  $P_M, P_R$
- b) Demagnetization/inverter current limit:
  - Stator field influences magnets: Inverter current limit has to be beneath demagnetization limit.
- c) Short time operation:
  - Maximum torque at inverter current limit
  - Motor operated at short time, utilization of thermal time constant of motors.
- d) Maximum operating speed:  $n_{\max} = n_{\text{sl}}/1.2$
- e) Voltage limit: Maximum inverter output voltage.



# Field weakening for PM-synchronous machines

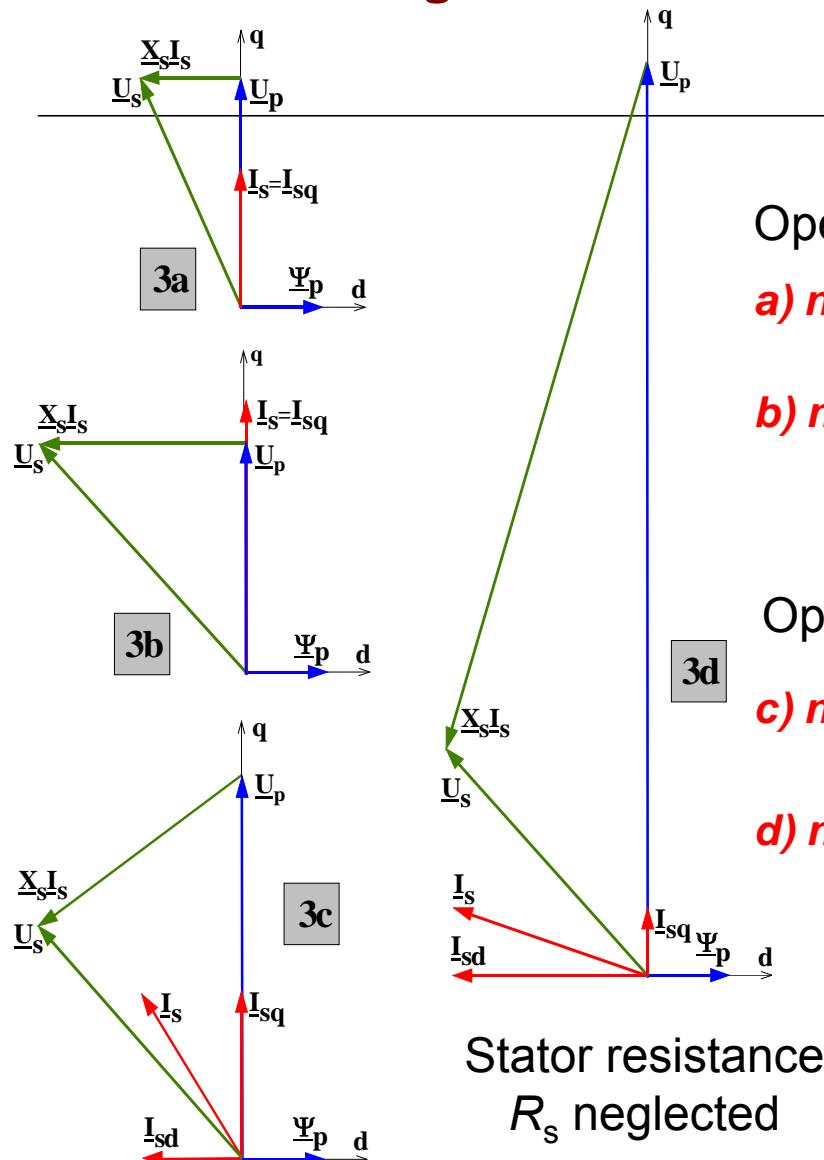


- From **rated speed  $n_N$**  on voltage limit  $U_{s,\max}$  is reached.
- By impressing a **negative  $d$ -current** a voltage opposing  $U_p$  is induced into the stator winding, so that  $U_s$  remains constant.
- $d$ -current generates with rotor flux **no torque!**
- At constant total current  $q$ -current has to be reduced due to the required  $d$ -current, so that **torque  $M$  is also being reduced!** („Field weakening range“)

Instead of  $n_{\max,\text{old}}$  (at  $U_s = U_p$ ) a higher  $n_{\max}$  is reached, but with reduced torque, which is not proportional to  $I_s$  anymore.



# Field weakening for PM-machines with negative d-current



Operation with full flux:

a)  $n = n_N$ : Rated current, rated torque,  $I_q$ -control,  $M \sim I_s$

b)  $n = n_N$ : 2x rated current, 2x rated torque,  $I_q$ -control,  $M \sim I_s$

Operation at field weakening:

c)  $n = 1.7n_N$ : 1.5x rated current, 1.3x rated torque

d)  $n = 4n_N$ : 1.7x rated current, 0.5x rated torque

**Current pilot control:**  $I_s$  is in front of  $U_p$ ,  $M$  is proportional to  $I_s$ , but higher speed than  $n_{max}$  (at  $U_s = U_p$ ) possible!



# Condition for good capability of field weakening



	Voltage $u_s$	Current $i_s$	<i>d</i> -axis $i_{sd}$	<i>q</i> -axis $i_{sq}$	Power	Speed $n$	$\cos\varphi$
a)	0.8	1.0	0	1.0	$P_N$	$n_N$	0.89 ind
b)	1.0	2.0	0	2.0	$2P_N$	$n_N$	0.7 ind
c)	1.0	1.5	-0.8	1.27	$2P_N$	$1.7n_N$	0.98 ind
d)	1.0	1.7	-1.6	0.5	$2P_N$	$4n_N$	0.89 cap

High field weakening range:  $U_p \gg U_{s,\max}$ ,  $U_{s,\max}$  and  $R_s$  neglected

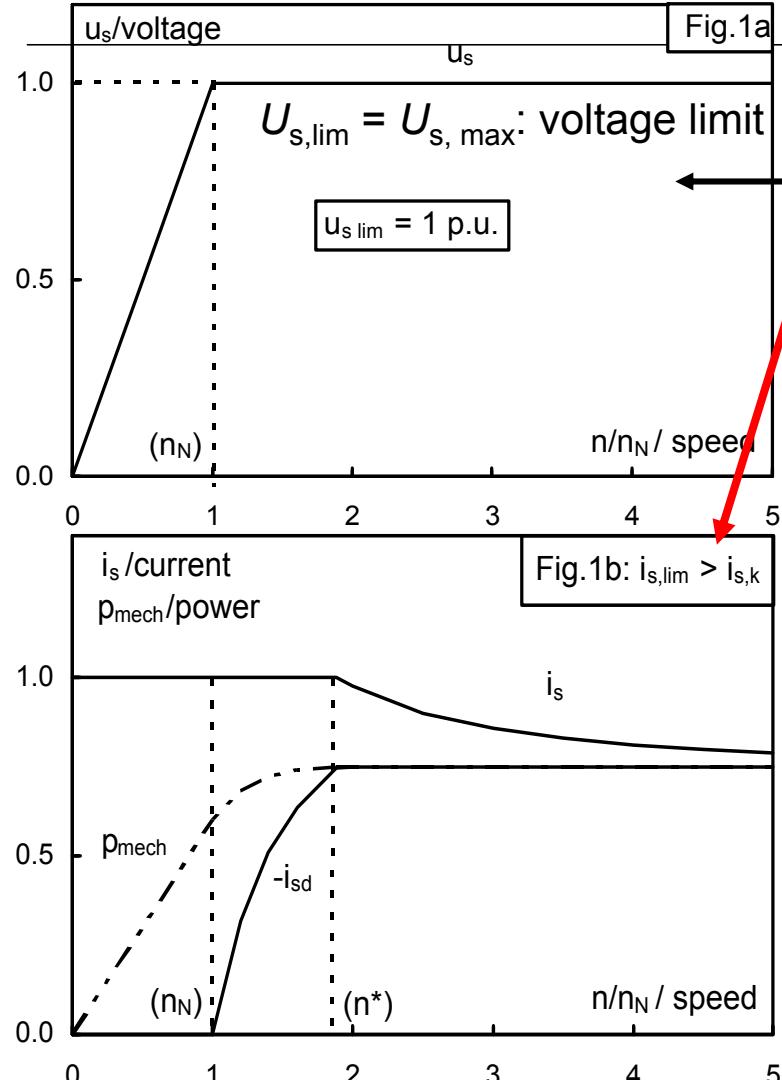
$$I_{s,d} \cong U_p / X_s = \Psi_p / L_s = \Psi_p / L_d$$

The required field weakening current  $I_d$  is approximately the generator short circuit current. The short circuit current has to be smaller than the inverter current limit for infinite field weakening!

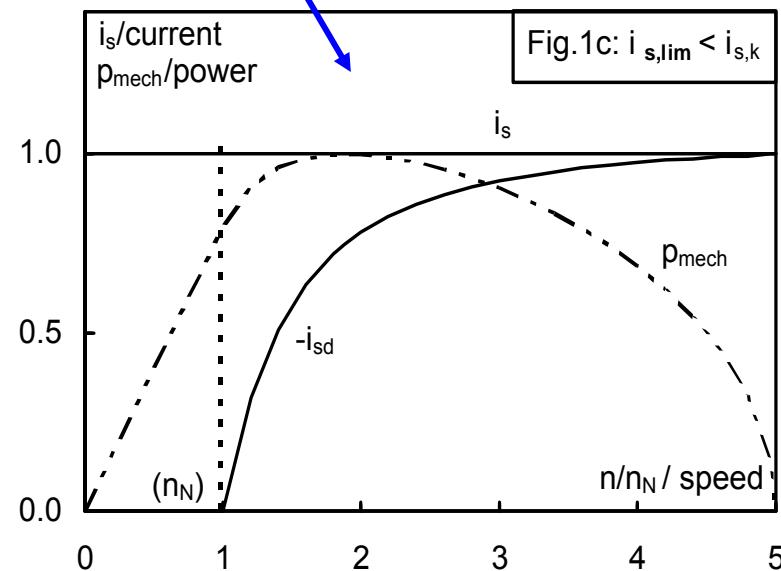
$$I_{s,d,\max} < I_{s,\max}$$



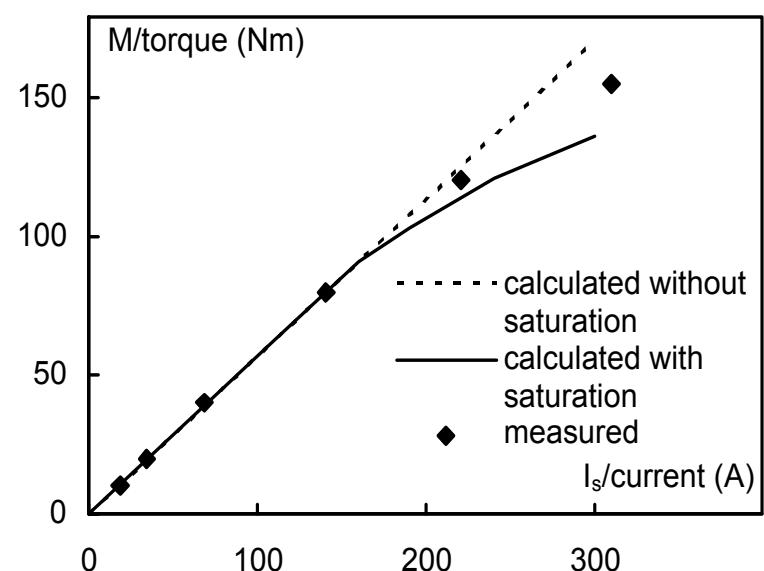
# Comparison of a well (A) and a badly (B) field weakable PM-synchronous motor



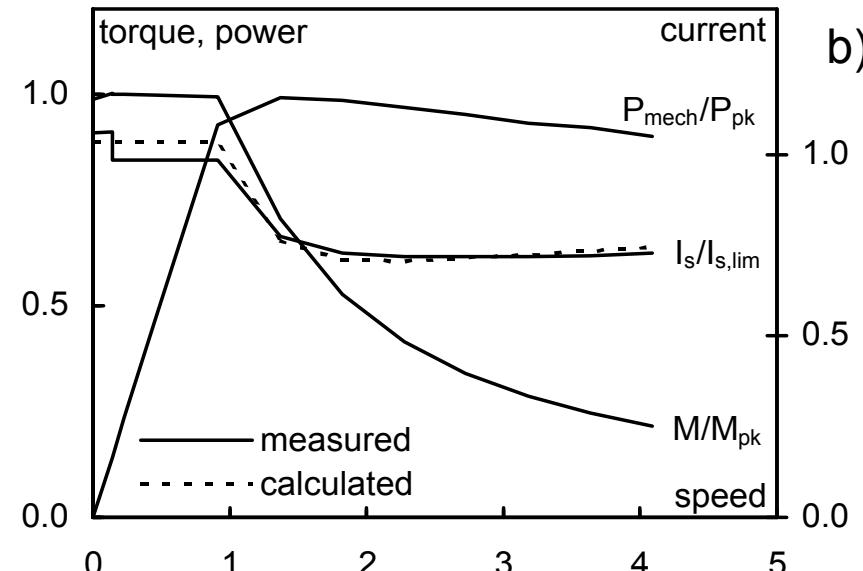
- $I_{s,lim} = I_{s, max}$ : Current limit
- a) Inverter output voltage for maximum motor power
  - b) Motor A: Inverter current limit high  $i_{s,lim} > i_{s,k}$
  - c) Motor B: Inverter current limit small  $i_{s,lim} < i_{s,k}$



## Example: PM-synchronous motor for E-car drive



a)



b)

- a) Torque-current-curve at low speed (full flux)
- b) Measured Torque-speed characteristic at 132V DC-link voltage = battery voltage,

Source: Ackva, A. et al.:  
EPE 1997, Trondheim

$$M_{\text{pk}} = 156 \text{ Nm}, P_{\text{pk}} = 35 \text{ kW}, I_{s,\text{lim}} = 315 \text{ A}$$

( $I_{s,\text{lim}} = I_{s,\text{max}}$ : Current limit)

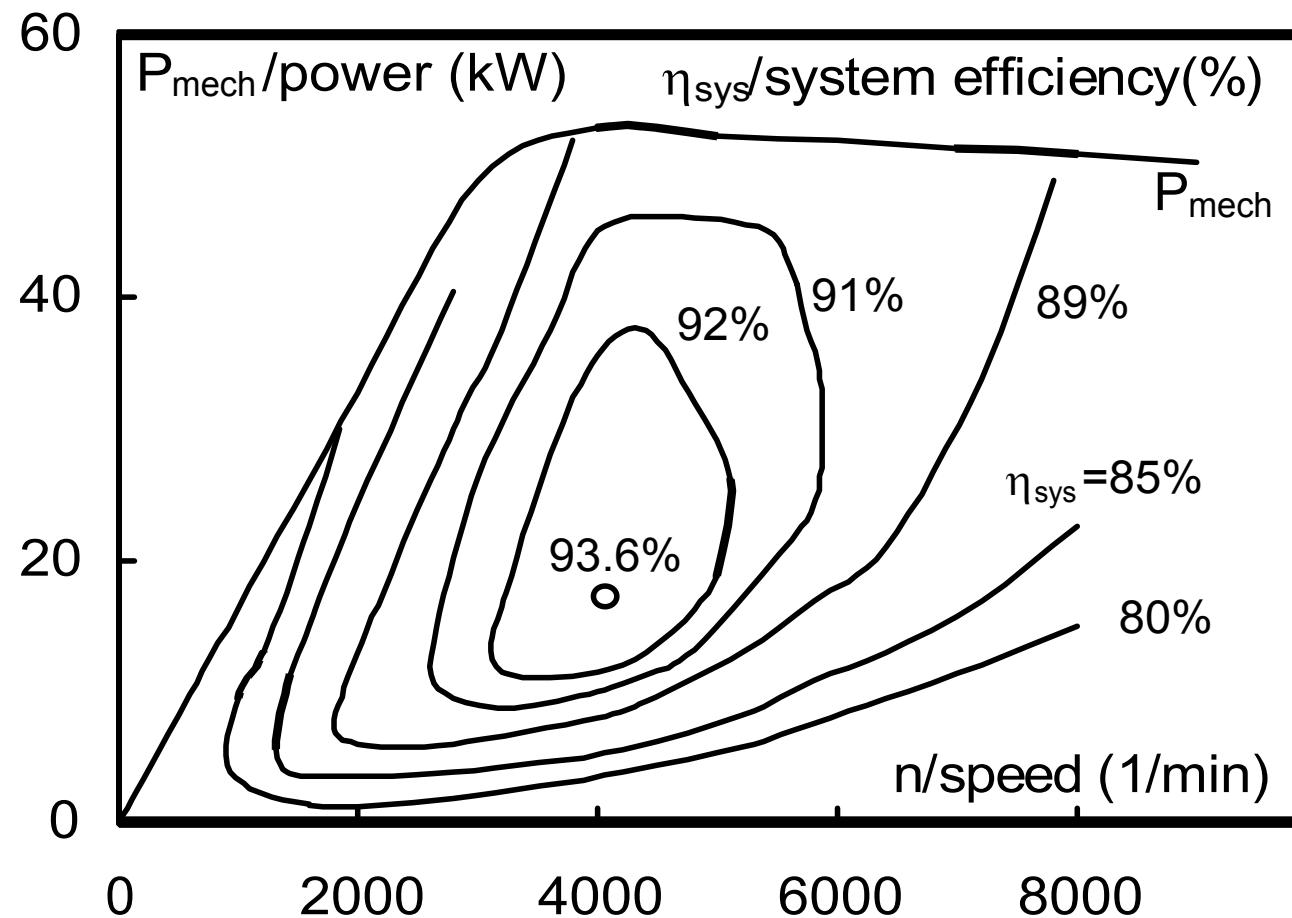


## Example: PM-synchronous motor + inverter: Efficiency map



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Measured motor output power and system efficiency (PM-synchronous motor + inverter) at 190V DC-link voltage = battery voltage



Source: Ackva, A. et al.:  
EPE 1997, Trondheim

## Example: PM-Synchronous motor efficiency



Measured operating parameters in continuous operation at

a) 132V , b) 160 V DC-link voltage = battery voltage

Speed in 1/min	$n$	2200	9000
Motor output power in kW	$P_M$	26	15
Battery voltage in V	$U_B$	132	160
Battery current in A	$I_B$	227.5	119
Shaft torque in Nm	$M$	113	16
Motor fundam. voltage in V	$U_{s1}$ (rms)	52	68.5
Motor fundam. current in A	$I_{s1}$ (rms)	213	164
Power factor	$\cos\varphi_s$	0.87	0.52
Motor ohmic losses in W	$P_{Cu}$	2180	1260
Winding temperature in °C	$\vartheta_{Cu}$	148	142
Motor efficiency in %	$\eta_M$	90.2	85.9
System efficiency in %	$\eta_{sys}$	86.6	78.9

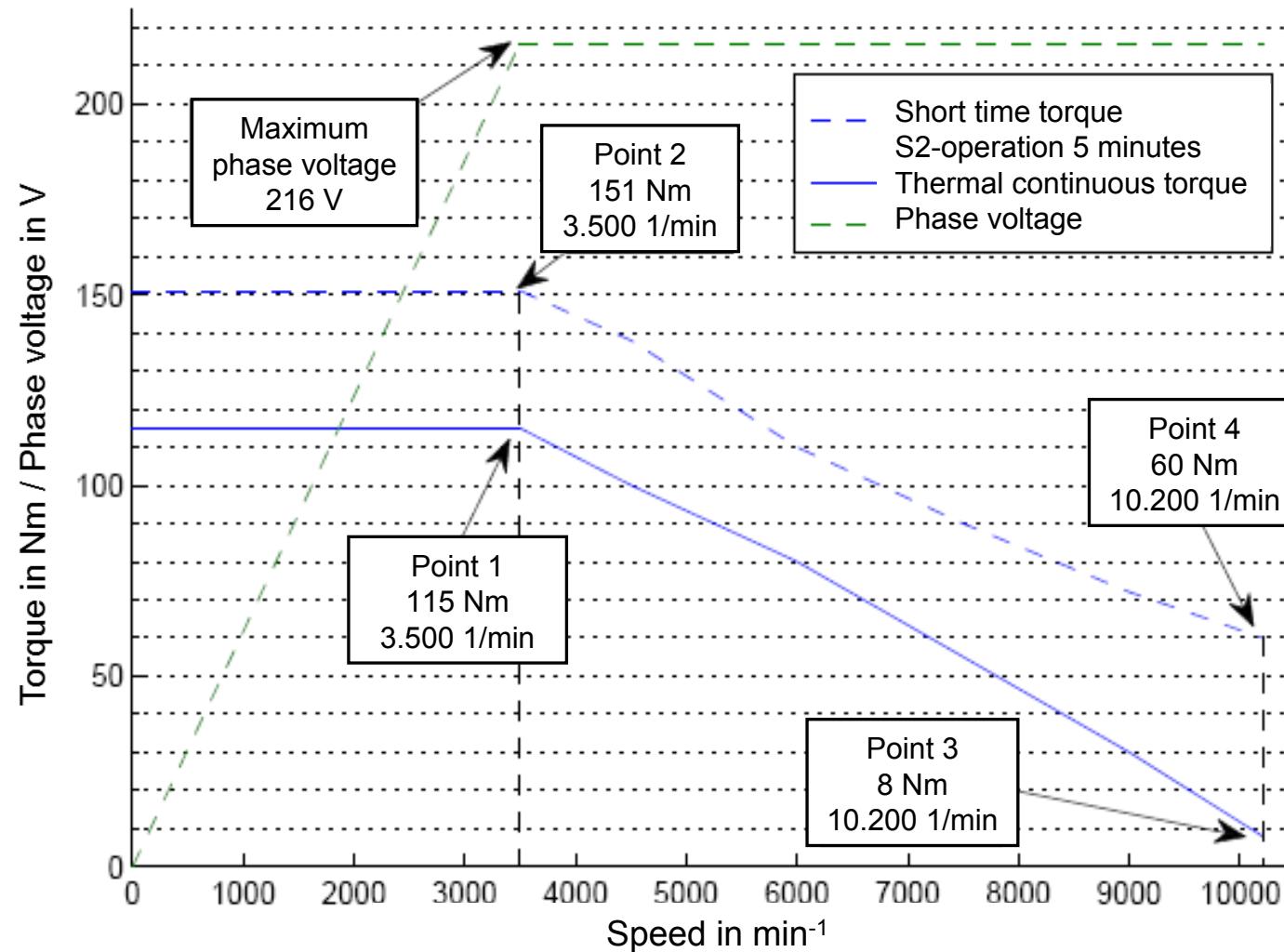
Source: Ackva, A. et al.:  
EPE 1997, Trondheim



# Example: Characteristics of a PM-synchronous motor (*Brusa*)



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# Loss groups of the PM-machine



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## 1. Stator:

1.a) Ohmic losses inclusive current harmonics  $P_{\text{Cu,s}}$

1.b) Iron losses in stator iron stack (teeth and yoke)

$$P_{\text{Fe,s}} = P_{\text{Fe,d}} + P_{\text{Fe,ys}}$$

## 2. Rotor:

2.a) Eddy current losses in magnets  $P_M$  due to stator current ripple (of inverter supply) and flux pulsation due to slot openings

2.b) Iron losses in rotor iron stack  $P_{\text{Fe,r}}$  due to stator current ripple

2.c) Friction losses: Bearing- and air friction  $P_{\text{bg+fr}}$

# Determination of the motor operating values for the required torque $M_M$ and speed $n_M$



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Motor shaft torque approx. as big as air gap torque:  $M_M \approx M_e$

Required q-current:  $I_q = \frac{M_M}{3p\Psi_p / \sqrt{2}} < I_{s,\max}$

at  $f_s = n_M \cdot p$ ,  $\omega_s = 2\pi f_s$

Required voltage without field weakening:

$$U_{s1} = \sqrt{(\omega_s \Psi_p / \sqrt{2} + R_s I_q)^2 + (\omega_s L_q I_q)^2} \leq U_{s,\max}$$

In case  $U_{s1} > U_{s,\max}$ : Required field weakening current  $I_d$  (negative):  
( $R_s$  neglected!)

$$I_d = \frac{\sqrt{U_{s,\max}^2 - (\omega_s L_q I_q)^2} - \omega_s \Psi_p / \sqrt{2}}{\omega_s L_d} \leq \sqrt{I_{s,\max}^2 - I_q^2}$$

Motor current:  $I_{s1} = \sqrt{I_d^2 + I_q^2} \leq I_{s,\max}$

In case  $I_d$  is too big  $\rightarrow I_q$  and therefore torque has to be reduced!



# Loss calculation in the PM-synchronous motor



Ohmic losses (stator):  $P_{\text{Cu,s}} = 3R_s(\vartheta) \cdot I_{s1}^2$

Iron losses:  $P_{\text{Fe}} = P_{\text{Fe0}} \cdot \left( \frac{\omega_s}{\omega_N} \right)^{1.8} \cdot \left( \frac{U_{s1}}{\omega_s \Psi_p / \sqrt{2}} \right)^2$

Friction losses:  $P_{\text{fr}} = 2\pi n_M M_{\text{fr}}(n_M)$

Additional losses (eddy current losses in magnets, rotor parts, winding) at sinusoidal current:

$$P_{\text{ad}} = P_{\text{ad,N}} \cdot \left( \frac{\omega_s}{\omega_N} \right)^{1.5} \cdot \left( \frac{I_{s1}}{I_{sN}} \right)^2$$

Additional losses due to current ripple with switching frequency (about constant value, a. o. depending on modulation degree  $m$ ):  $P_{\text{ad,inv}}$

Total losses of motor:  $P_{d,M} = P_{\text{Cu,s}} + P_{\text{Fe}} + P_{\text{ad}} + P_{\text{fr}} + P_{\text{ad,inv}}$

Motor efficiency:  $\eta_M = P_M / (P_M + P_{d,M}) = P_M / P_e \quad \cos \varphi_s = P_e / (3U_{s1}I_{s1})$

## Example: Motor losses



### Rated data:

6-pole PM-synchronous motor,  $M_N = 95.5 \text{ Nm}$ ,  $n_N = 2200/\text{min}$ ,  $P_N = 22 \text{ kW}$   
 $f_N = 110 \text{ Hz}$ ,  $L_d = 0.186 \text{ mH}$ ,  $L_q = 0.219 \text{ mH}$ ,  $R_{s, 20^\circ\text{C}} / R_{s, 155^\circ\text{C}} = 10.5/16.0 \text{ mOhm}$   
 $\Psi_p = 98 \text{ mVs (20°C)}$ ,  $P_{Fe0} = 248 \text{ W}$ ,  $P_{adN} = 110 \text{ W}$ ,  $P_{ad,inv} = 56 \text{ W}$ ,  $M_{fr} = 0.05 \text{ Nm}$   
 $I_{sN} = 174 \text{ A}$ ,  $U_{sN} = 50 \text{ V}$ , motor weight 45 kg, water jacket cooling

Ohmic losses,  $155^\circ\text{C}$ : 1453 W

Iron losses: 270 W

Friction losses: 11.5 W

Additional losses: 110 W

Additional losses due to current ripple: 56 W

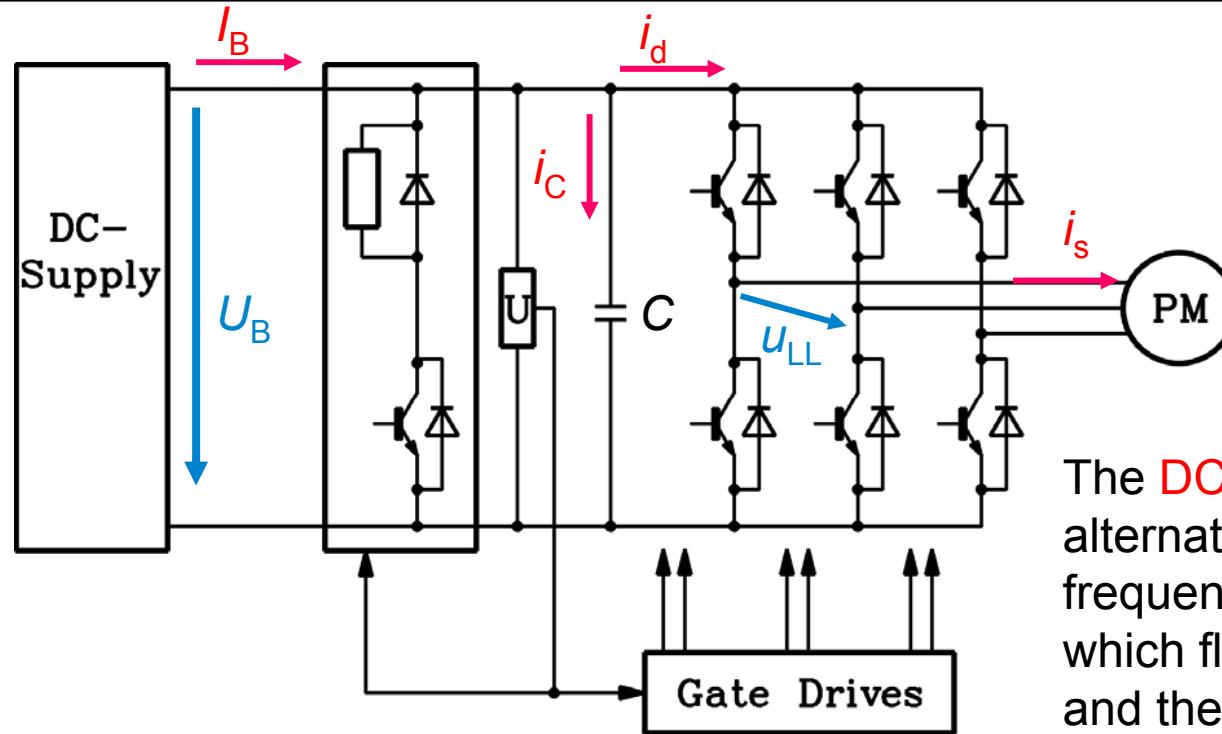
Source: Ackva, A. et al.:  
EPE 1997, Trondheim

Total losses: 1900 W

$\cos\varphi_s = 0.916$

Motor efficiency: 92.05%

# Modeling of the inverter



The line-to-line pulsed stator voltage  $u_{LL}$  has a fundamental  $U_{LL1}$  with  $f_s$ . Its rectification is mainly the battery voltage  $U_B$ .

$I_B$ : Battery current

$i_d$ : DC-link current

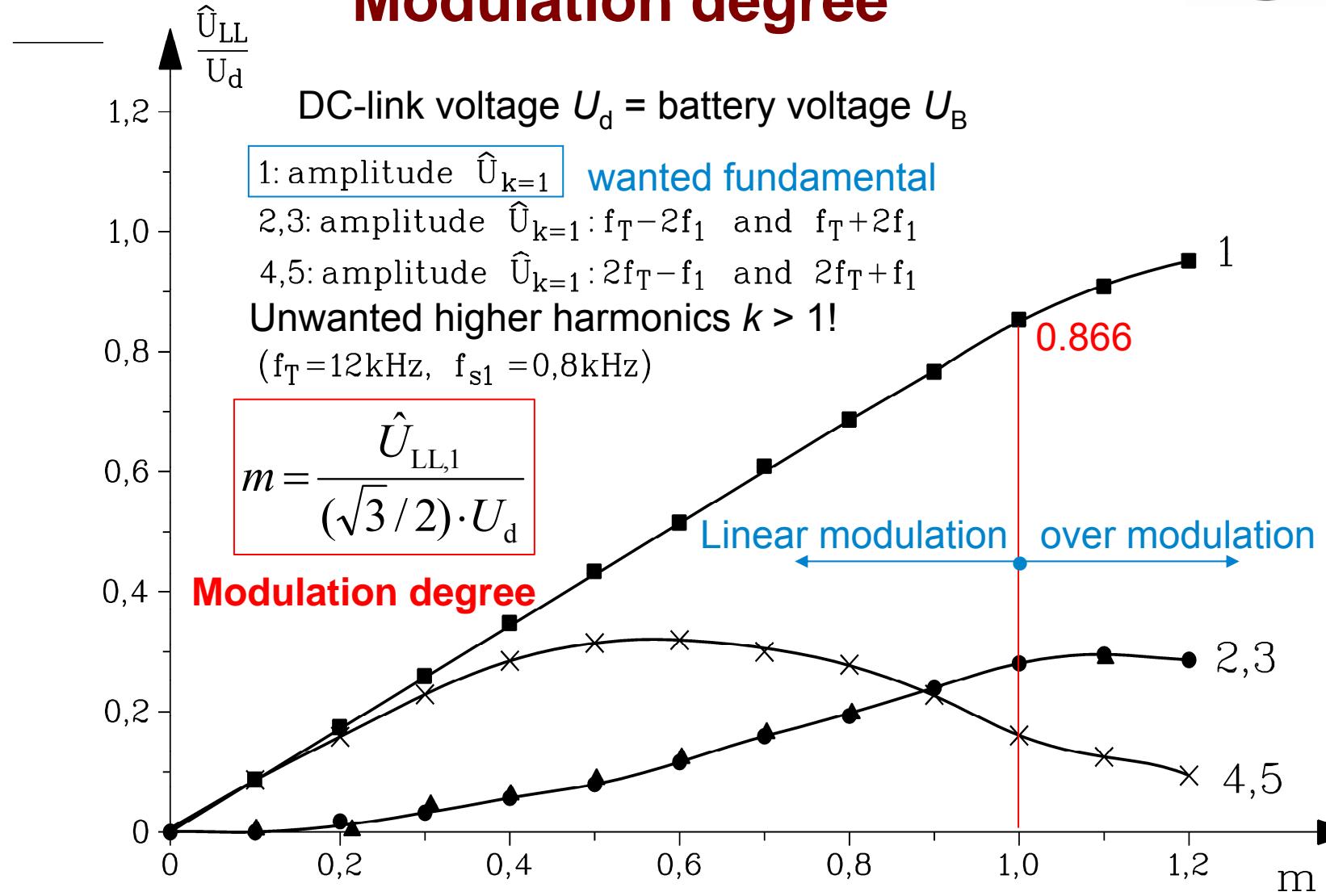
$i_C$ : capacitor current

C: DC-link capacity

The DC-link current  $i_d$  contains the alternating part from the switching frequency  $f_T$  of the transistors, which flows as capacitor current  $i_C$  and therefore hardly loading the battery. The DC-part is the battery current, which is being distributed on the three phases with the fundamental frequency  $f_s$  as stator frequency.

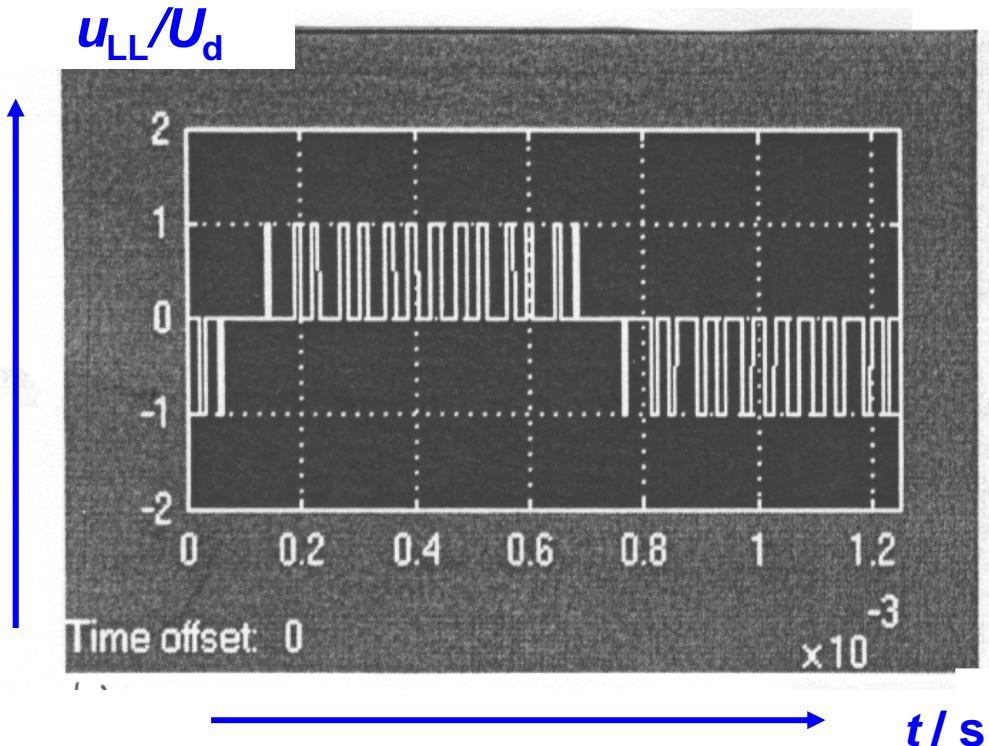


# Pulse width modulation – Modulation degree

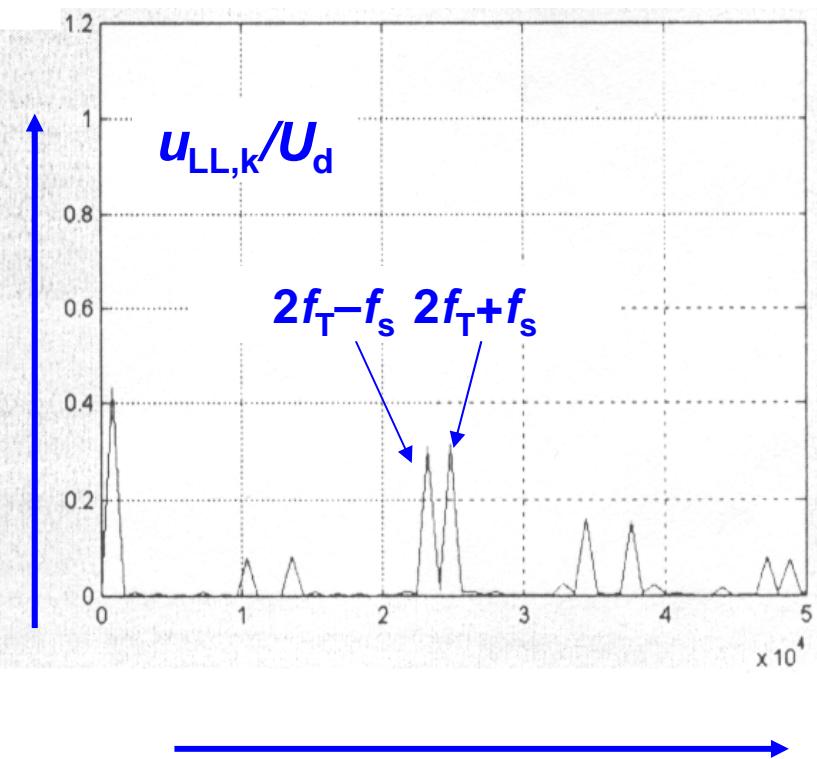


# Line-to-line inverter output voltage: $m = 0.5$

Pulse width modulated output voltage



Fourier-spectrum of  $U$ -harmonics



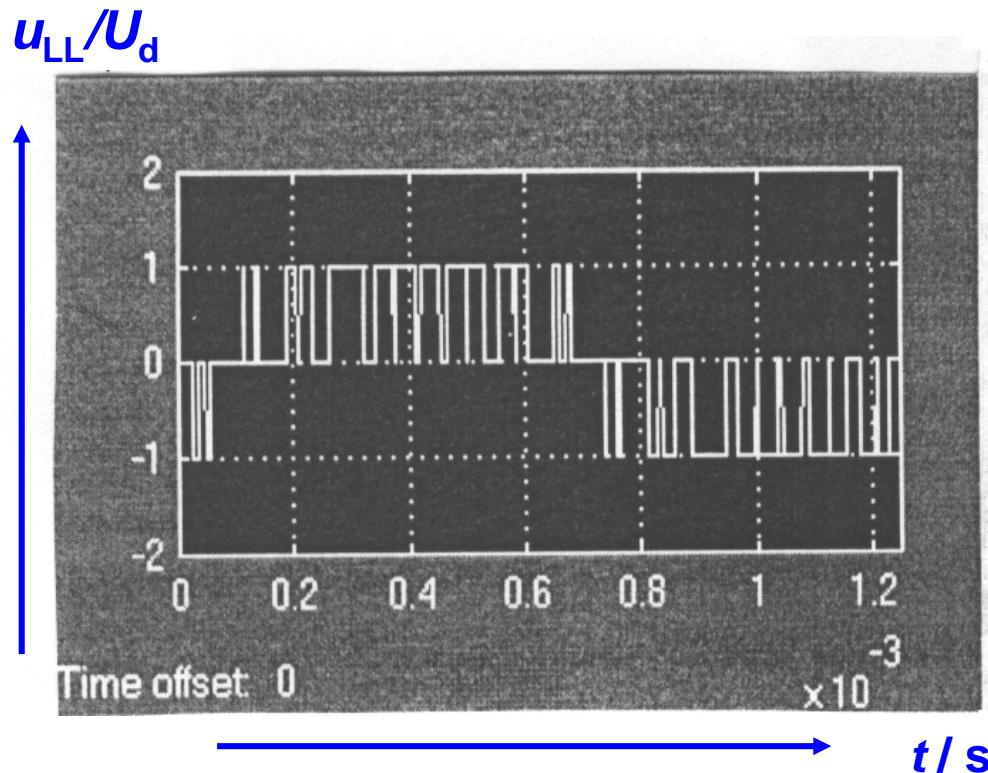
Example: Fundamental  $f_s = 800$  Hz

Switching frequency  $f_T = 12000$  Hz =  $15f_s$

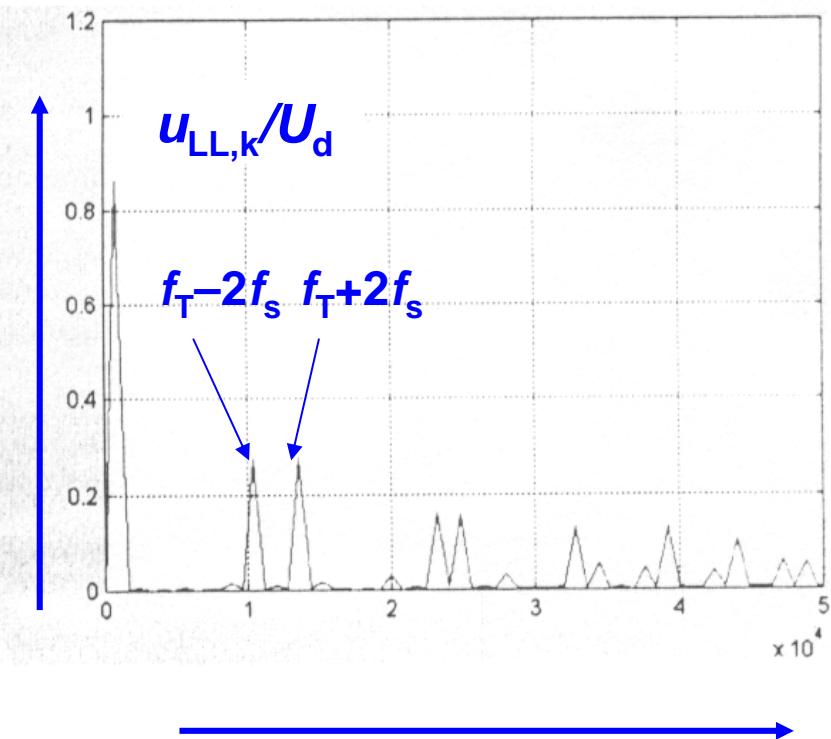
$f/Hz$   
Voltage fundamental:  
amplitude  $0.43U_d$

# Line-to-line inverter output voltage: $m = 1.0$

Pulse width modulated output voltage



Fourier-spectrum of  $U$ -harmonics



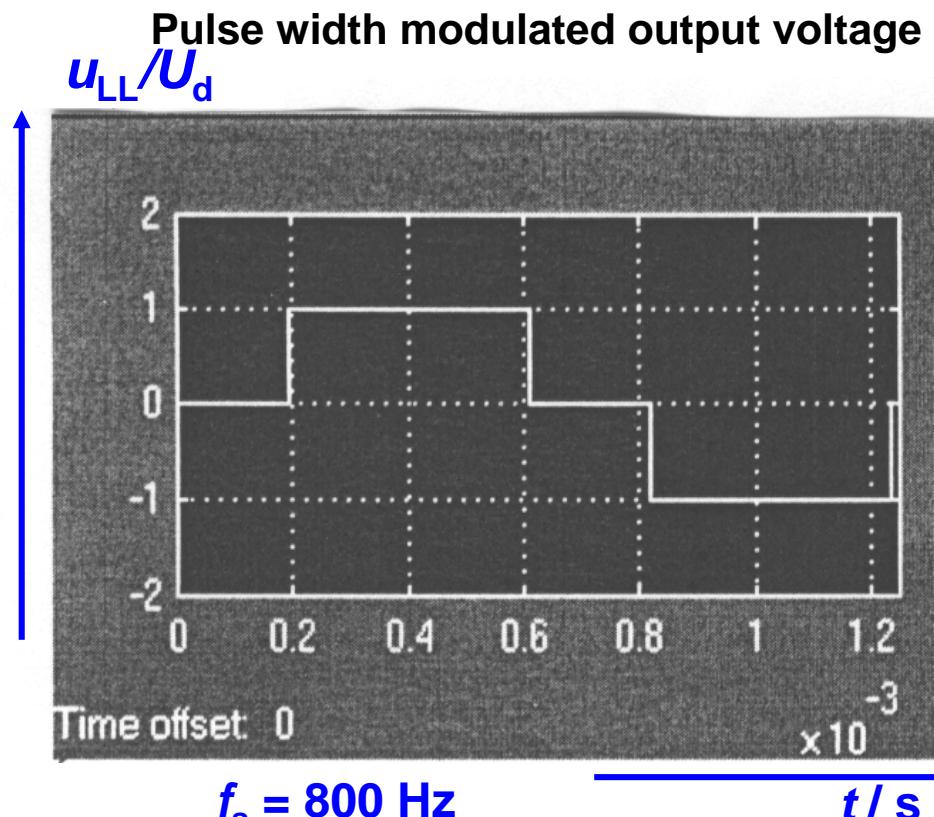
Example: Fundamental  $f_s = 800 \text{ Hz}$

Switching frequency  $f_T = 12000 \text{ Hz} = 15f_s$

Voltage fundamental:  
amplitude  $0.86U_d$

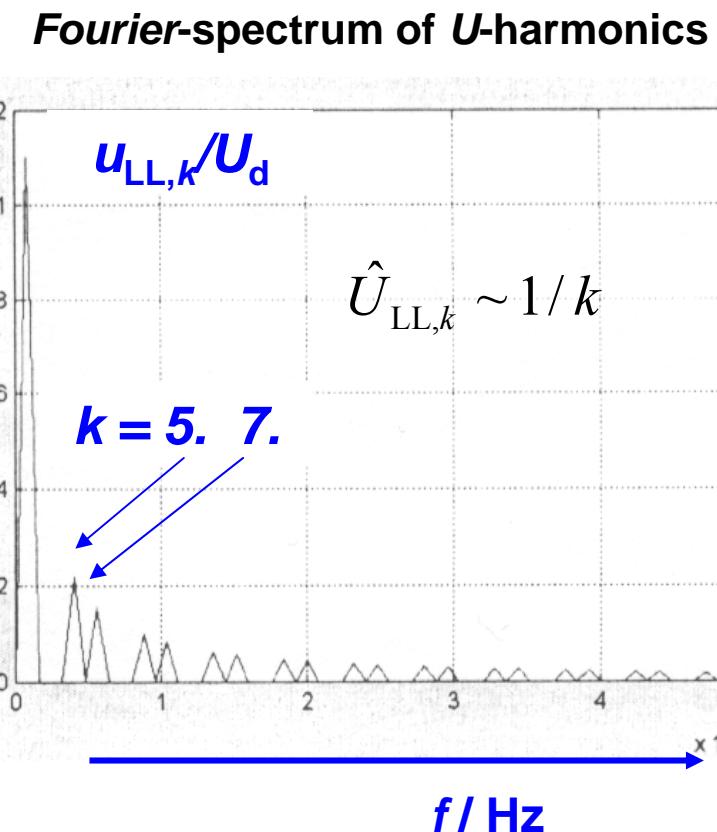


# Square wave operation: Over modulation $m = \infty$



Example: Fundamental frequency  $f_s = 800 \text{ Hz}$

Switching frequency  $f_T = f_s$  “six step operation”



Voltage fundamental:  
amplitude  $1.1U_d$



# Estimation of max. inverter output voltage



Maximum inverter fundamental output voltage at:

a) Square wave operation:

Line-to-line voltage peak value:

$$\hat{U}_{LL1} = \frac{4}{\pi} \cdot \sin\left(\frac{2}{3} \cdot \frac{\pi}{2}\right) \cdot U_d = \frac{2\sqrt{3}}{\pi} \cdot U_d$$

Phase voltage, RMS-value:  $U_{s1} = \hat{U}_{LL1} / (\sqrt{2} \cdot \sqrt{3}) = \frac{\sqrt{2}}{\pi} \cdot U_d$

b) At linear limit of modulation  $m = 1$ :  $\hat{U}_{LL1} = \frac{\sqrt{3}}{2} \cdot U_d$        $U_{s1} = \frac{U_d}{2\sqrt{2}}$

Example:

Battery voltage  $U_B = U_d = 480$  V:

a)  $\hat{U}_{LL1} = 529$  V       $U_{s1} = 216$  V

b)  $\hat{U}_{LL1} = 415$  V       $U_{s1} = 170$  V



# Modeling of the inverter



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$I_{s1}$ : Fundamental of stator phase current

$U_{s1}$ : Fundamental of stator phase voltage       $U_{s1} = U_{LL1} / \sqrt{3}$

$\varphi_{s1}$ : Phase angle between  $I_{s1}$  and  $U_{s1}$

$P_{d,inv}$ : Inverter losses

Power balance

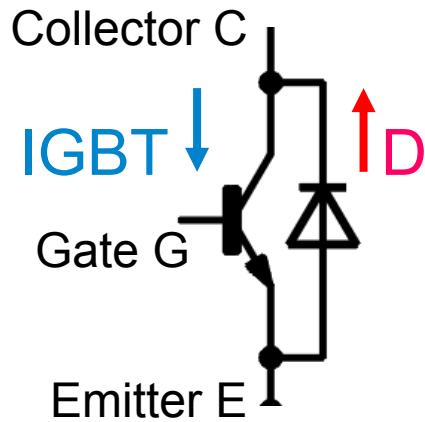
$$P_B = 3U_{s1}I_{s1} \cos \varphi_{s1} + P_{d,inv}$$

Inverter losses:

- Conduction losses  $P_{inv,C}$
- Switching losses  $P_{inv,S}$
- Base supply  $P_{inv,0} = \text{approx. } 50 \text{ W}$

$P_{d,inv}$

# Modeling of the inverter



IGBT: Insulated Gate Bipolar Transistor = switching transistor

D: Free wheeling diode (antiparallel): Conducts current during voltage brake

Example: IGBT a. Diode FS200 R06KE3, Fa. Infineon

Blocking voltage:  $U_{CE,\text{sperr}} = 600 \text{ V}$ , battery voltage should not exceed 500 V

## IGBT:

Collector continuous-/peak current:  $I_{C,N} = 200 \text{ A}$ ,  $I_{C,pk} 400 \text{ A (1 ms)}$ ,  $U_{CE,N} = 300 \text{ V}$

Continuous junction temperature 125°C:  $U_{CE,\text{sat}} = 1.6 \text{ V}$  at 200 A

Conducting voltage  $U_{CE0} = 0.8 \text{ V}$ , conducting resistance  $R_{TD} = 4 \text{ m}\Omega$

Switch-on/-off losses at  $U_{CE,N}$ ,  $I_{C,N}$ : 1.7 mJ/6.7 mJ per switching process

## Free wheeling diode:

Continuous-/peak current:  $I_{F,N} = 200 \text{ A}$ ,  $I_{F,pk} 400 \text{ A (1 ms)}$ ,  $U_{F,N} = 300 \text{ V}$

Continuous junction temperature 125°C: conducting voltage  $U_{F0} = 0.8 \text{ V}$ , Conducting resistance  $R_{FD} = 2.5 \text{ m}\Omega$

Cut-off losses at  $U_{F,N}$ ,  $I_{F,N}$ : 5.2 mJ per switching process



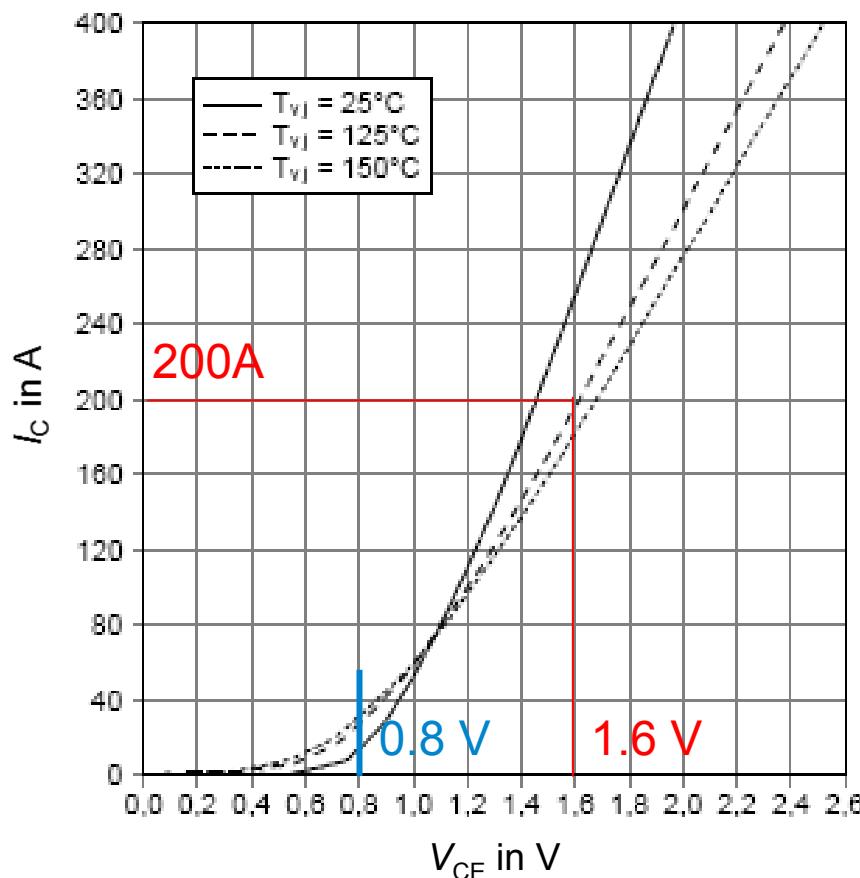
# Power switch IGBT (inverter)

FS200 R06KE3, Fa. Infineon



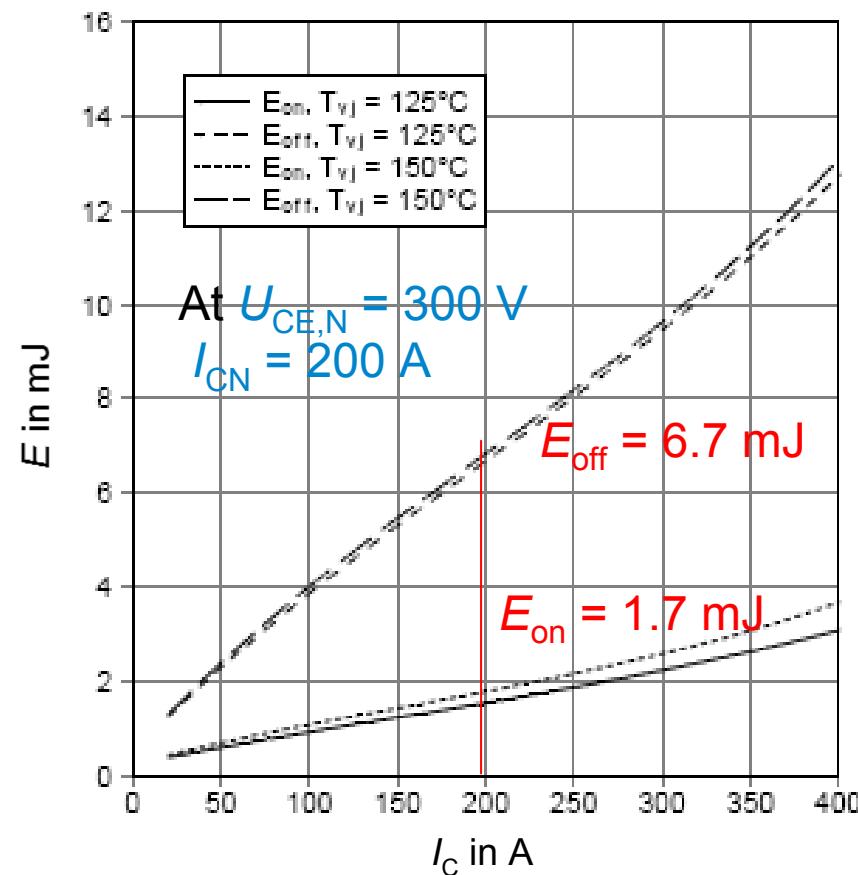
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Conduction characteristics



$$R_{TD} = (2.4 - 0.8) / 400 = 4 \text{ m}\Omega$$

Switching losses ( $t_{\text{on}} = 40 \text{ ns}$ ,  $t_{\text{off}} = 70 \text{ ns}$ )



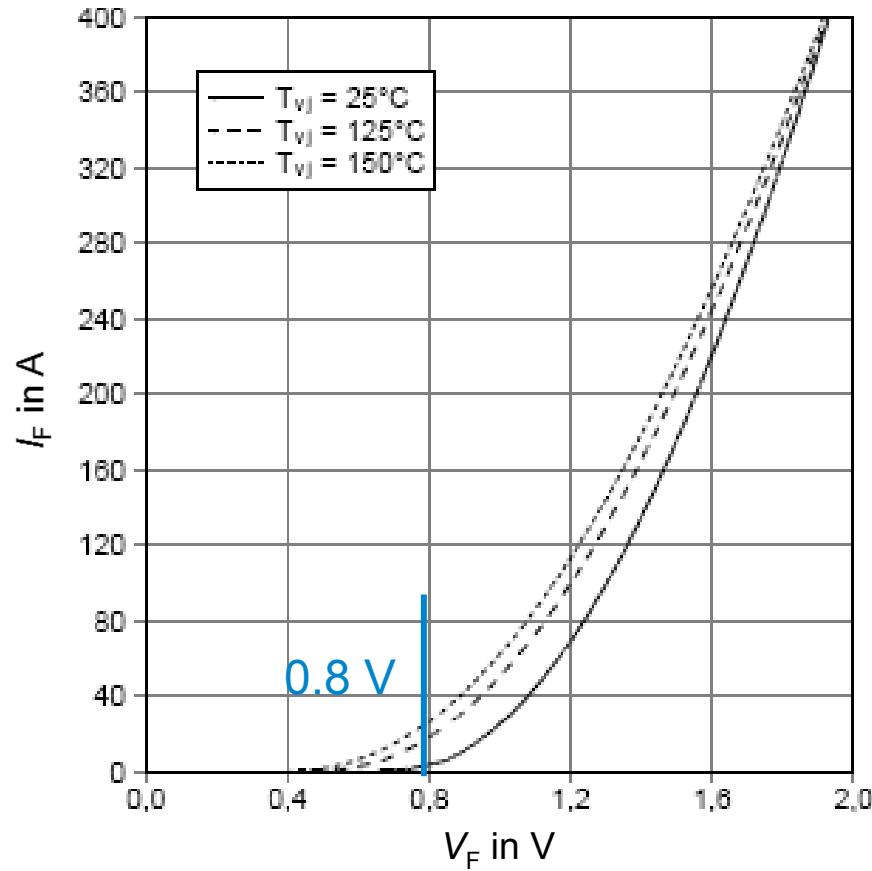
# Free wheeling diode (inverter)

FS200 R06KE3, Fa. Infineon



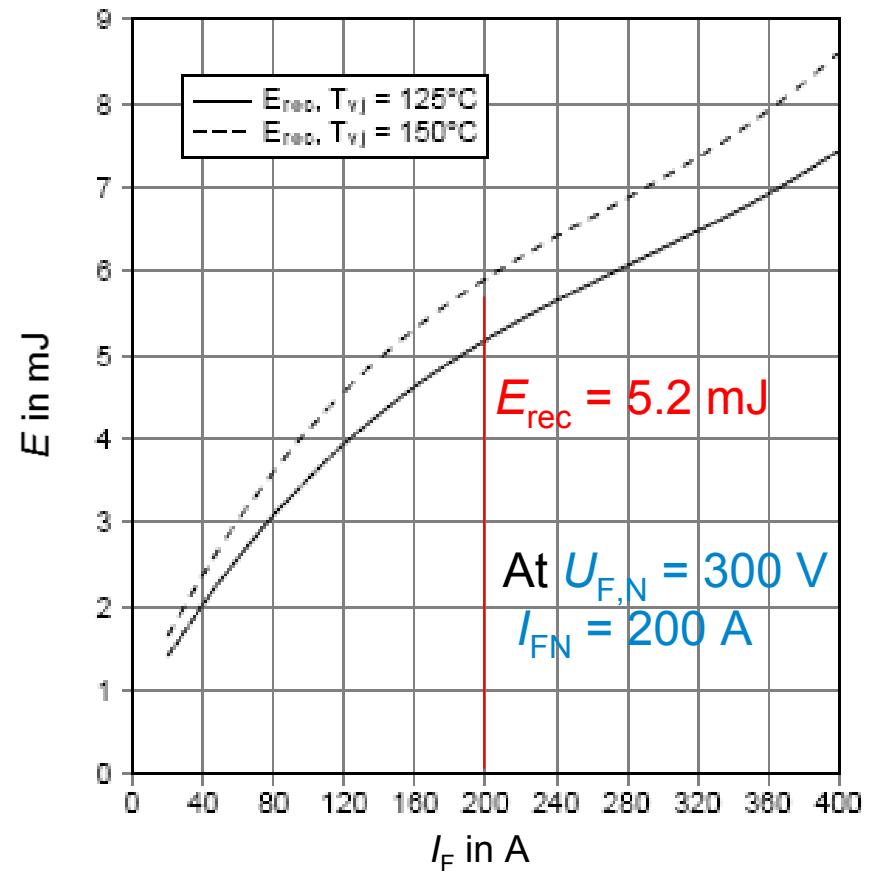
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Conduction characteristics



$$R_{FD} = (1.8 - 0.8) / 400 = 2.5 \text{ m}\Omega$$

Switching losses  $E_{\text{rec}}$  (very small)



# Estimation of losses of the inverter

for modulation degree  $0 \leq m \leq 1$



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- Conduction losses per IGBT:

$$P_{T,D} = U_{CE0} \hat{I}_s \cdot \left( \frac{1}{2\pi} + \frac{m \cdot \cos \varphi_s}{8} \right) + R_{TD} \hat{I}_s^2 \cdot \left( \frac{1}{8} + \frac{m \cdot \cos \varphi_s}{3\pi} \right)$$

- Switching losses per IGBT:

$$P_{T,S} = \frac{f_T}{\pi} \cdot \frac{\hat{I}_s}{I_{C,N}} \cdot \frac{U_d}{U_{CE,N}} \cdot (E_{on} + E_{off})$$

- Conduction losses per Diode:

$$P_{D,D} = U_{F0} \hat{I}_s \cdot \left( \frac{1}{2\pi} - \frac{m \cdot \cos \varphi_s}{8} \right) + R_{FD} \hat{I}_s^2 \cdot \left( \frac{1}{8} - \frac{m \cdot \cos \varphi_s}{3\pi} \right)$$

- Cut-off losses per Diode:

$$P_{D,S} = \frac{f_T}{\pi} \cdot \left( 0.55 + 0.45 \cdot \frac{\hat{I}_s}{I_{F,N}} \right) \cdot \frac{U_d}{U_{F,N}} \cdot E_{rec}$$

For higher modulation degree  $m$  the IGBTs conduct more often and the diodes less, hence the IGBT losses increase with increasing  $m$ !

- Conduction- and switching losses for 6 IGBTs and Diodes:

$$P_{inv,S+D} = 6 \cdot (P_{T,D} + P_{T,S} + P_{D,D} + P_{D,S})$$



# Example: Losses of the inverter



$$m = 1, \cos\varphi_s = 0.8, U_d = 480 \text{ V}, f_T = 12 \text{ kHz}, I_{s1} = 100 \text{ A}, U_{s1} = 170 \text{ V}$$

Output fundamental power:

$$P_e = 3U_{s1}I_{s1} \cos\varphi_{s1} = 40.8 \text{ kW}$$

Loss component	Losses in W
Transistor conduction losses	38.8 W
Transistor switching losses	36.3 W
Diode conduction losses	8.7 W
Diode switching losses	27.6 W
Sum per transistor-diode pair	111.4 W
Sum aver all 6 pairs	668.4 W
Efficiency in %	98.27

$$\text{Inverter efficiency: } \eta_{\text{inv}} = P_e / (P_e + P_{d,\text{inv}})$$

# Board grid energy demand (is added as additional losses of the inverter)



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Component	Power consumption in W
Control devices	60
Headlight	90
Vehicle reg. light a. rear light	25
Instrument light	20
Ventilation	50
Power steering	25
Sum	270

Average demand:  
(day/night)  
(warm/cold)  
(rain/dry)  
in minimum 150 W

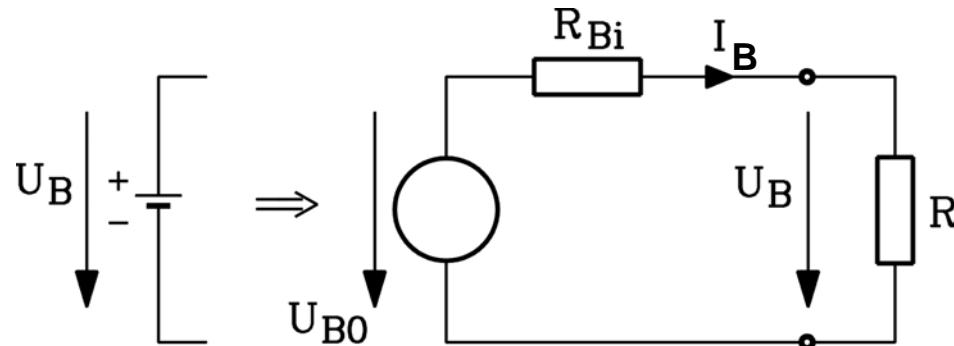
## More electric consumers:

Wiper motor, compressor for air conditioning, radio + DVD-player, navigation, heatable windows and mirrors, electric adjustable chassis (suspension), electric heating

**12 V supply:** From battery (e. g. 400 V DC) by **DC-DC-converter** to 12 V DC step-down



# Modeling of the battery



$U_{B0}$ : No-load voltage

$R_{Bi}$ : Internal battery resistance

$Q$ : Obtained amount of el. charge

$t_B$ : Discharge time for  $Q$  at current  $I = \text{const.}$

$W_B$ : Obtained energy from battery

$Q_N$ : Rated charge (Ah), often also denoted as  $C$

$y = 1 - Q/Q_N$ : State of Charge SOC

$$U_B = U_{B0} - I_B \cdot R_{Bi}$$

$$Q = I_B \cdot t_B$$

$$W_B = Q \cdot U_B$$

$$Q_{\text{Rest}} = y \cdot Q_N$$

Discharging:  $I_B > 0$

Charging:  $I_B < 0$

Consumer  
reference system

*Example:*

Pb-battery:  $U_{B0} = 144 \text{ V}$ ,  
 $R_{Bi} = 0.055 \Omega$ ,  $Q_N = 100 \text{ Ah}$

# Battery current / at obtained power $P_B$



$$U_B = U_{B0} - I_B \cdot R_{Bi}$$

$$P_B = (U_{B0} - I_B \cdot R_{Bi}) I_B$$

For a fixed power the batteries can be charged/discharged with  
a) low current and high voltage

b) High current and low voltage (unfavorable).

a) 
$$I_B = \frac{U_{B0}}{2R_{Bi}} - \sqrt{\left(\frac{U_{B0}}{2R_{Bi}}\right)^2 - \frac{P_B}{R_{Bi}}} \leq I_{B,\max}$$

b) 
$$I_B = \frac{U_{B0}}{2R_{Bi}} + \sqrt{\left(\frac{U_{B0}}{2R_{Bi}}\right)^2 - \frac{P_B}{R_{Bi}}} \leq I_{B,\max}$$

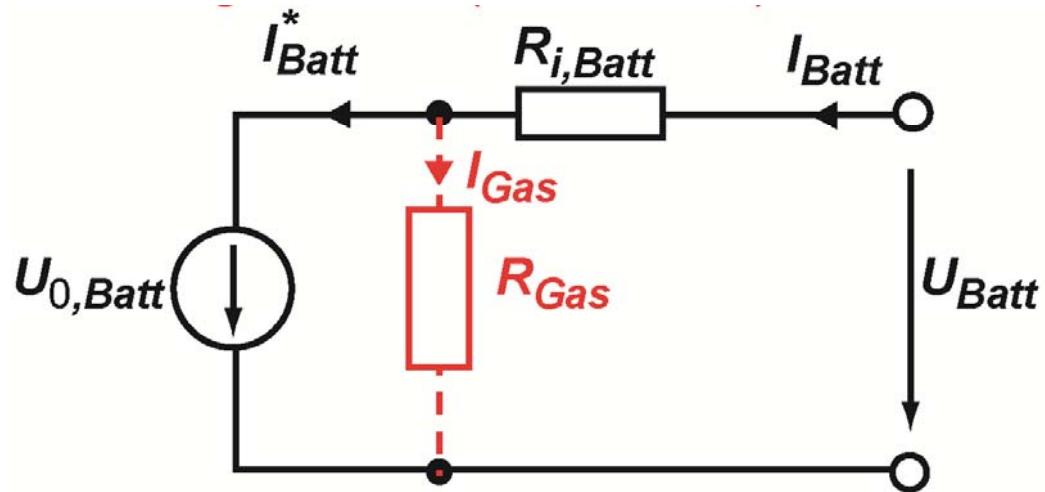
# Modeling: Traction battery



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## ▪ Equivalent circuit

- Discharging of battery and charging without gassing reaction ( $SOC \leq 80\%$ )
- For charging of battery with gassing reaction  $> 80\%$



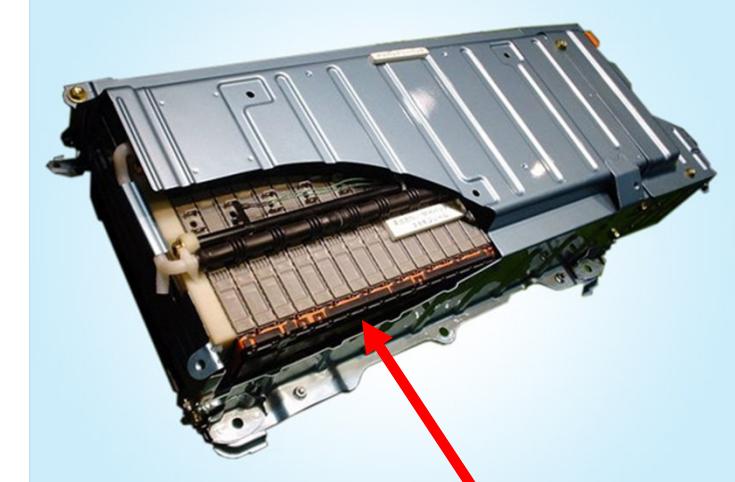
## ▪ Modeling

- EC-parameters: characteristics
- $U_{0,Batt} = f(SOC)$
- $R_{i,Batt} = f(SOC)$
- $R_{Gas} = f(SOC)$
- SOC: Ah-balance

# Example: Modeling of the Ni-metal-hydride-battery



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## ▪ Technical data

Battery parameter	Data
Number of cells in series	$n_{\text{cell}} = 228$
min./max. cells voltage	$U_{\text{cell,min/Max}} = 0,9 \text{ V} / 1,6 \text{ V}$
Min./max. battery-no-load voltage	$U_{\text{batt,min/max}} = 273 \text{ V} / 330 \text{ V}$
Battery rated capacity	$Q_{\text{batt,N}} = 6,5 \text{ Ah}$
Number of parallel battery branches	$a_{\text{batt}} = 1$
Internal resistance $R_{\text{Bi}} = f(\text{SOC})$	$R_{\text{Bi}} = 0,85 \dots 1,2 \Omega$

NiMH-Battery  
*Toyota Prius II*

# Batteries for hybrid- vs. E - car



## Ni-Me-hydride-battery (Comp. Ovonics) for hybrid vehicle

- Battery voltage (no-load): 160 V
- 10.5 Ah
- Battery internal resistance: at -5°C: 0.05 Ohm, at 40°C: 0.01 Ohm
- Battery maximum current: For 10 s: 292 A; for 1 s: 365 A

## Lead-gel-battery for E-car:

- Battery voltage (no-load): 144 V = 12 x 12 V-cells
- 100 Ah
- Battery internal resistance: 0.055 Ohm
- Battery maximum current: 300 A

In [hybrid vehicles](#) the necessary amount of energy storage is much smaller than in [E-cars \(range!\)](#), but the power peaks due to recuperation during braking or due to high power consumption during „boosting“ are much higher. Hence a protection of the batteries with an additional [super cap-storage](#) is recommended, as they have high power densities.

# Battery cells in comparison



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	Lead-gel	Ni-metal-hydride	Li-ion
Cell voltage	2 V	1.2 V	3.5 V
Energy density	30 Wh/kg	80 Wh/kg	100 Wh/kg
Efficiency	70 ... 85 %	85 %	90%
Operating temp.	0 ... 55°C	-20 ... 55°C	-20...60°C



## **Electric vehicles**

### **– Simulation examples**



## a) Example:

### Constant speed – Range calculation

## Example: Range calculation for $v = \text{const.}$



### Tasks:

No slope:  $\alpha = 0$ ,  $v = \text{const.} = 120 \text{ km/h}$ ,  $m = 1437 \text{ kg}$ ,  $c_w A = 0.56 \text{ m}^2$ ,  $d_R = 0.6 \text{ m}$

$f_R = 0.01$ ,  $\eta_G = 0.9$ ,  $i = 8.02$ ,  $Q = 100 \text{ Ah}$ ,  $U_{B0} = 192 \text{ V}$ ,  $R_{Bi} = 0.055 \Omega$  (Pb-Gel)

SOC: start: 100%, end: 25%, PM-synchronous motor 6-poles and IGBT-inverter  
(efficiency field for  $U_B = 190 \text{ V}$ ), board grid: 400 W

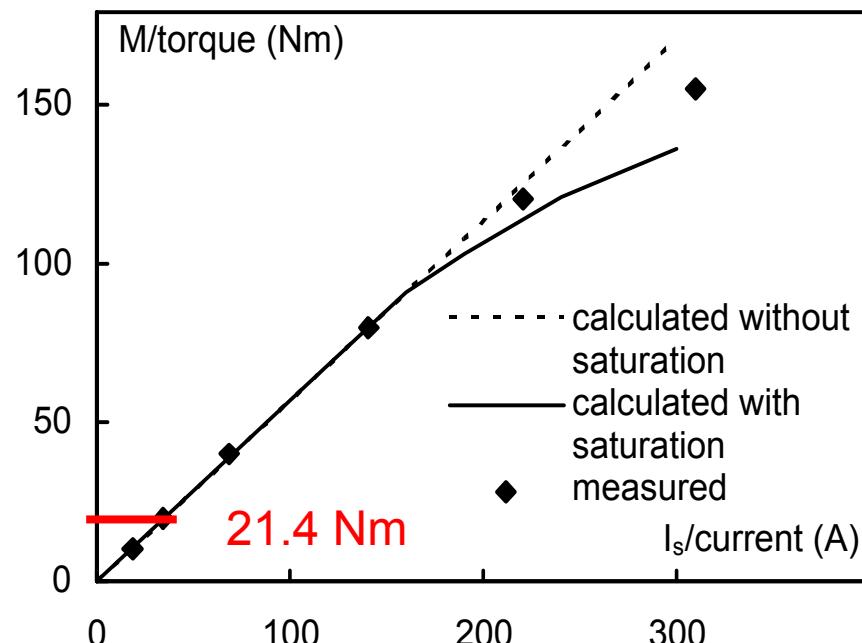
### Results:

- 1) Driving resistances:  $F_{Bg} \approx 0$ ,  $F_{\text{Roll}} = 141 \text{ N}$ ,  $F_L = 375 \text{ N}$ ,  $F_D = 515 \text{ N}$ ,  $P_D = 17.17 \text{ kW}$
- 2) Wheel speed and gear:  $n_W = 1061/\text{min}$ ,  $n_M = 8509/\text{min}$ ,  $P_M = 19.078 \text{ kW}$
- 3) Motor data:  $M_M = 21.4 \text{ Nm}$ , driving system efficiency: 80%  
(inverter: 93%, PM-syn. motor 86%)
- 4) Battery power:  $19.078/0.8 + 400 = 24248 \text{ W} = P_B$ ,  $I_B = \frac{U_{B0}}{2R_{Bi}} - \sqrt{\left(\frac{U_{B0}}{2R_{Bi}}\right)^2 - \frac{P_B}{R_{Bi}}} = 131.2 \text{ A}$
- 5) Range:  $y = 1 - \text{SOC}_{\text{end}} = 0.75$ ,  $t = Q \cdot y / I_B = 2058 \text{ s} = 34.3 \text{ min}$ ,  $s = v \cdot t = 68.6 \text{ km}$

## Example: PM-synchronous drive

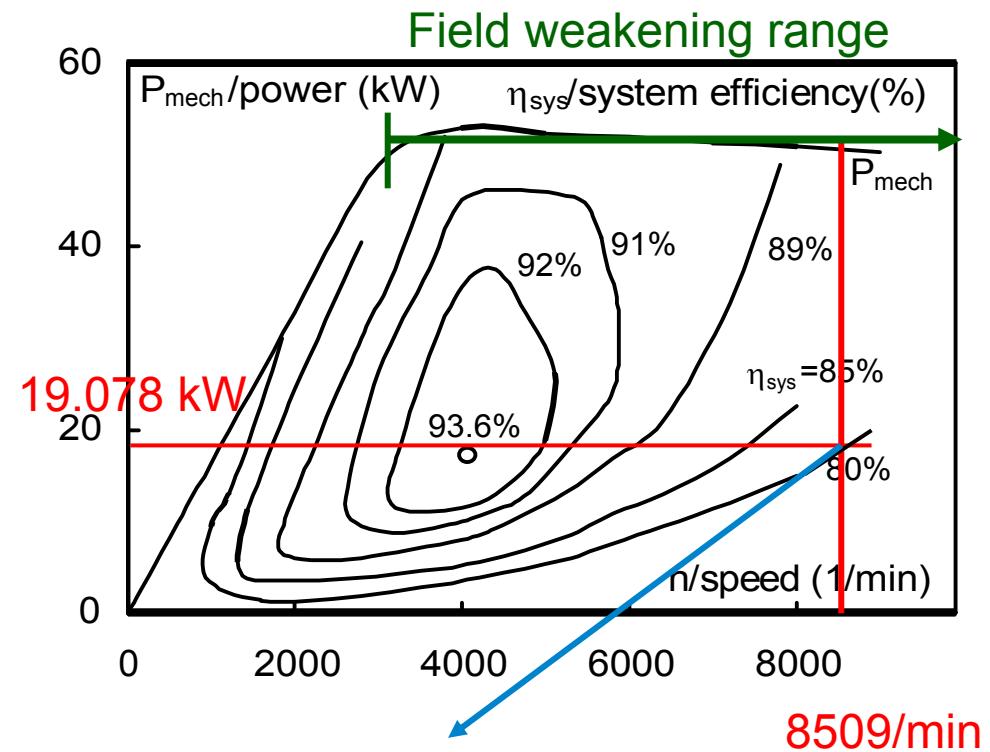


Torque- quadrature current-curve



Source: Ackva, A. et al.:  
EPE 1997, Trondheim

Power+ efficiency (motor + inverter)



System efficiency in high field weakening range and partial load: 80%





## b) Example:

### Speed cycles – Range calculation and capability of acceleration

## Example: Specification for a fictive E-car – during cycle and at max. acceleration



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### Specification:

$m = 900 \text{ kg}$  (empty)  $c_w A = 0.5 \text{ m}^2$ ,  $d_R = 0.623 \text{ m}$ ,  $\Delta = 0.2$  rotating mass adding factor,  
 $f_R = 0.008$ ,  $\eta_G$  accord. Efficiency field,  $i = 8$ ,  $Q = 30 \text{ Ah}$ ,  $U_{B0} = 480 \text{ V}$ ,  $R_{Bi} = 0.0696 \Omega$   
(Li-Ion, comp. Kokam), PM-synchronous motor 6-poles (comp.. Brusa, 6.17.12):  
4500/min, 85 Nm, max. 11000/min, IGBT-inverter: comp.. Brusa, DMC524, 80 kW  
(106 kW short time), 600 V blocking voltage, board grid: 150 W

The vehicle is designed for  $v_{\max} = 150 \text{ km/h}$  : motor speed = 10200/min.

## Example: Driving resistances



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Speed in km/h	Driving resistance in N
0	0
25	85.2
50	128.5
75	201.5
100	302
125	432
138	513
150	591

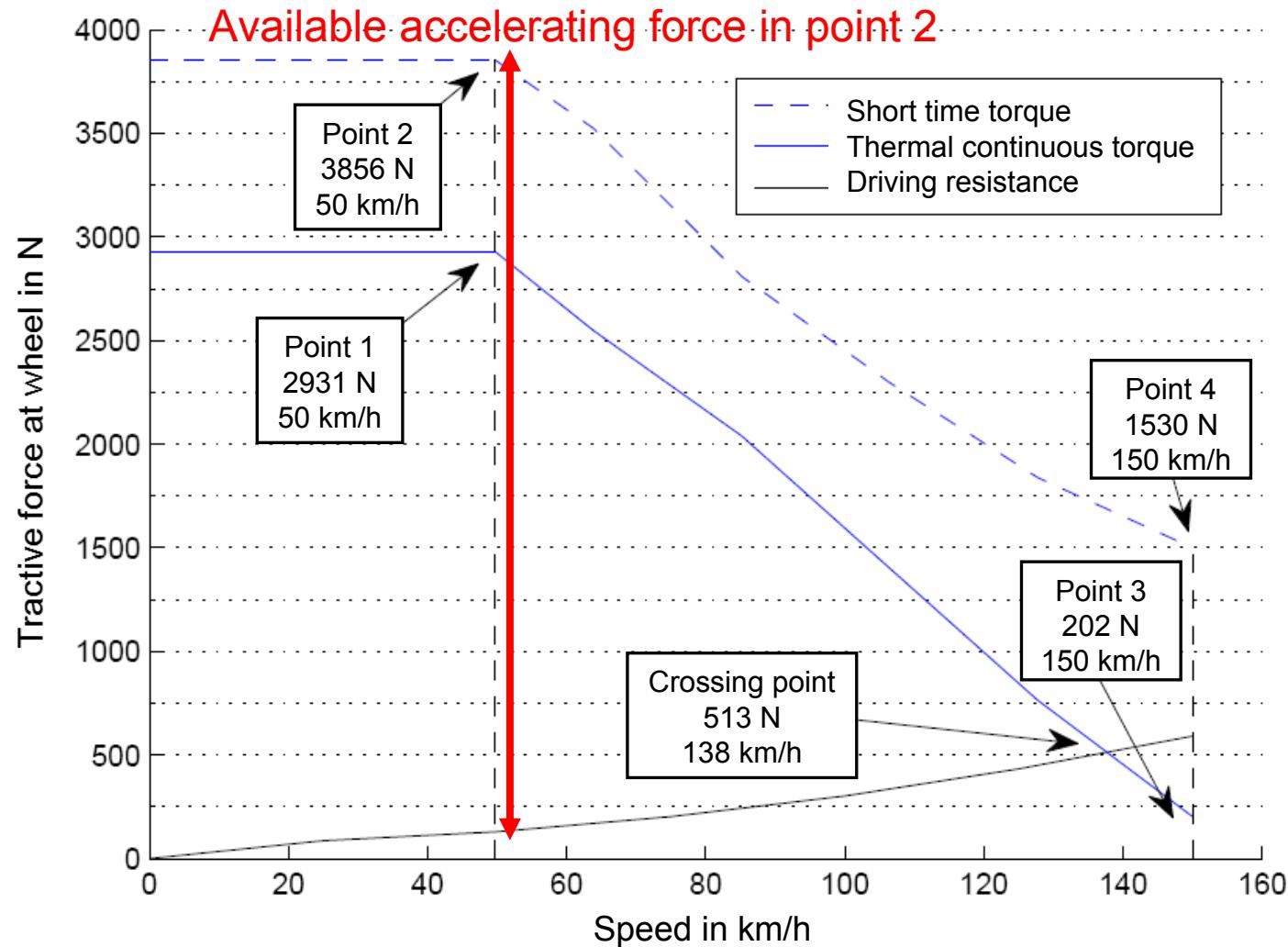
$$\alpha = 0$$



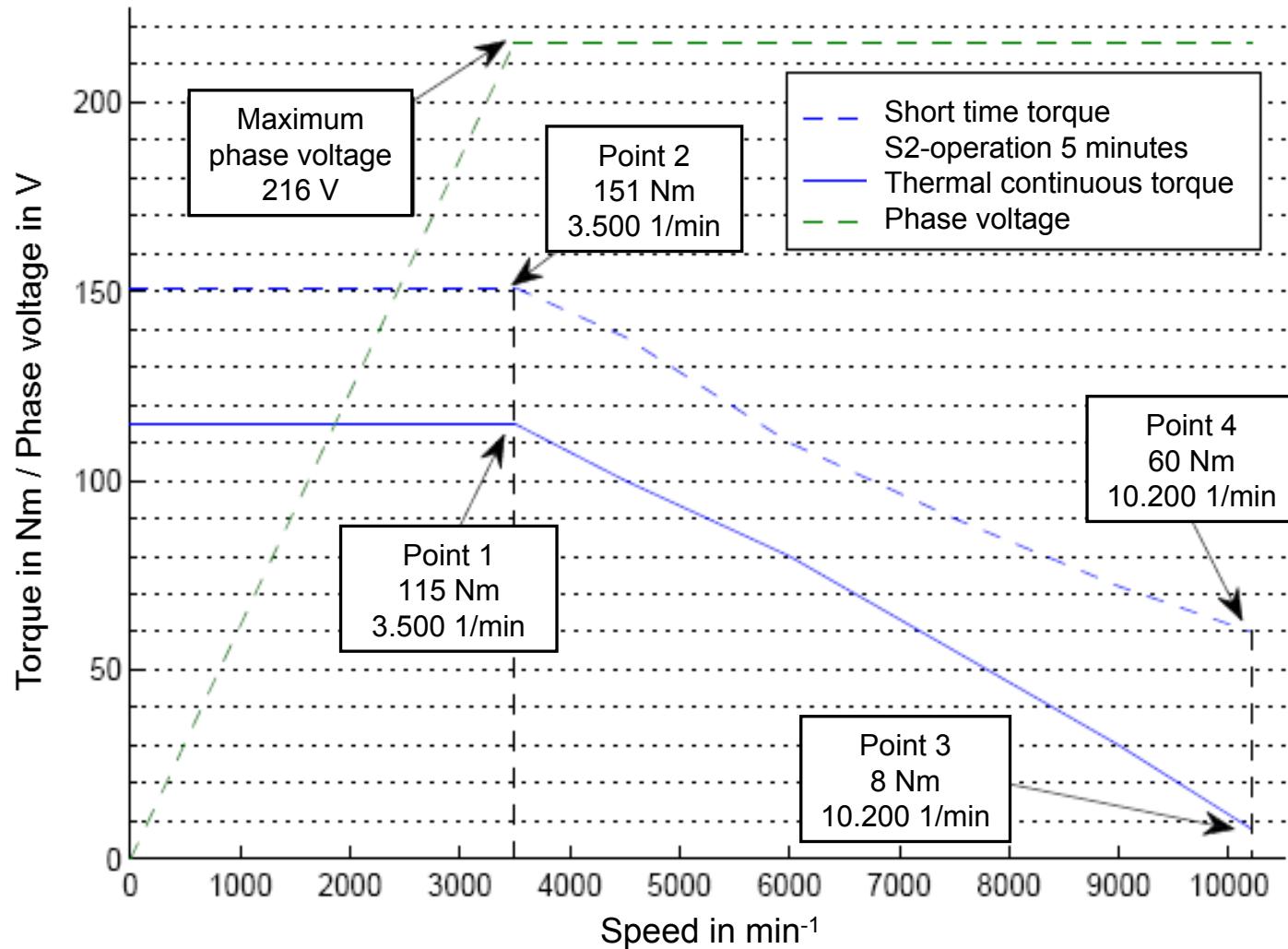
# Example: E-car solutions in motor characteristic field



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# Example: Border lines of a PM-synchronous-motor (*Brusa*)



# Example: E-car: PM-motor and vehicle-load data



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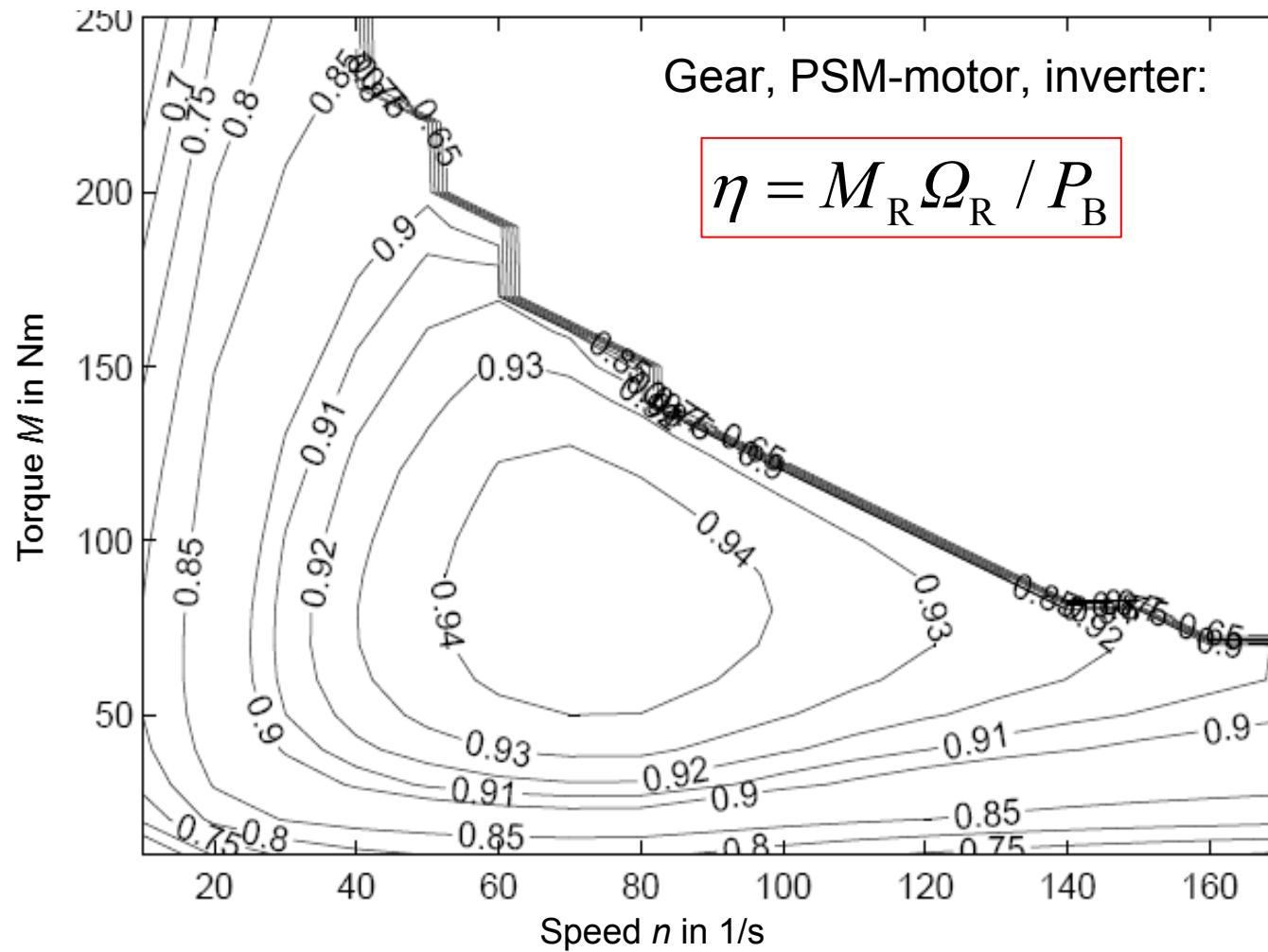
Point in characteristic	Speed in m/s resp. km/h	$I_d$ in A	$I_q$ in A
1 ( $n_N / M_d$ )	13.8 / 49.7	0	102
2 ( $n_N / M_{S2}$ )	13.62 / 49	0	139
3 ( $n_{\max} / M_d$ )	41.55 / 149.6	84	7
4 ( $n_{\max} / M_{S2}$ )	41.05 / 147.78	109.5	52.5

Speed	Thermal continuous torque in Nm	Maximum short time torque (S2-5 min operation)
$n_N = 58.1 \text{ /s}$ $n_{\max} = 170.1 \text{ /s}$	115 / point 1 8 / point 3	151 / point 2 60 / point 4

# Example: E-car (Brusa-drive) calculated efficiency field



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## **Example: Losses in four operation points**

**Due to high accelerating force slip losses also occur!**



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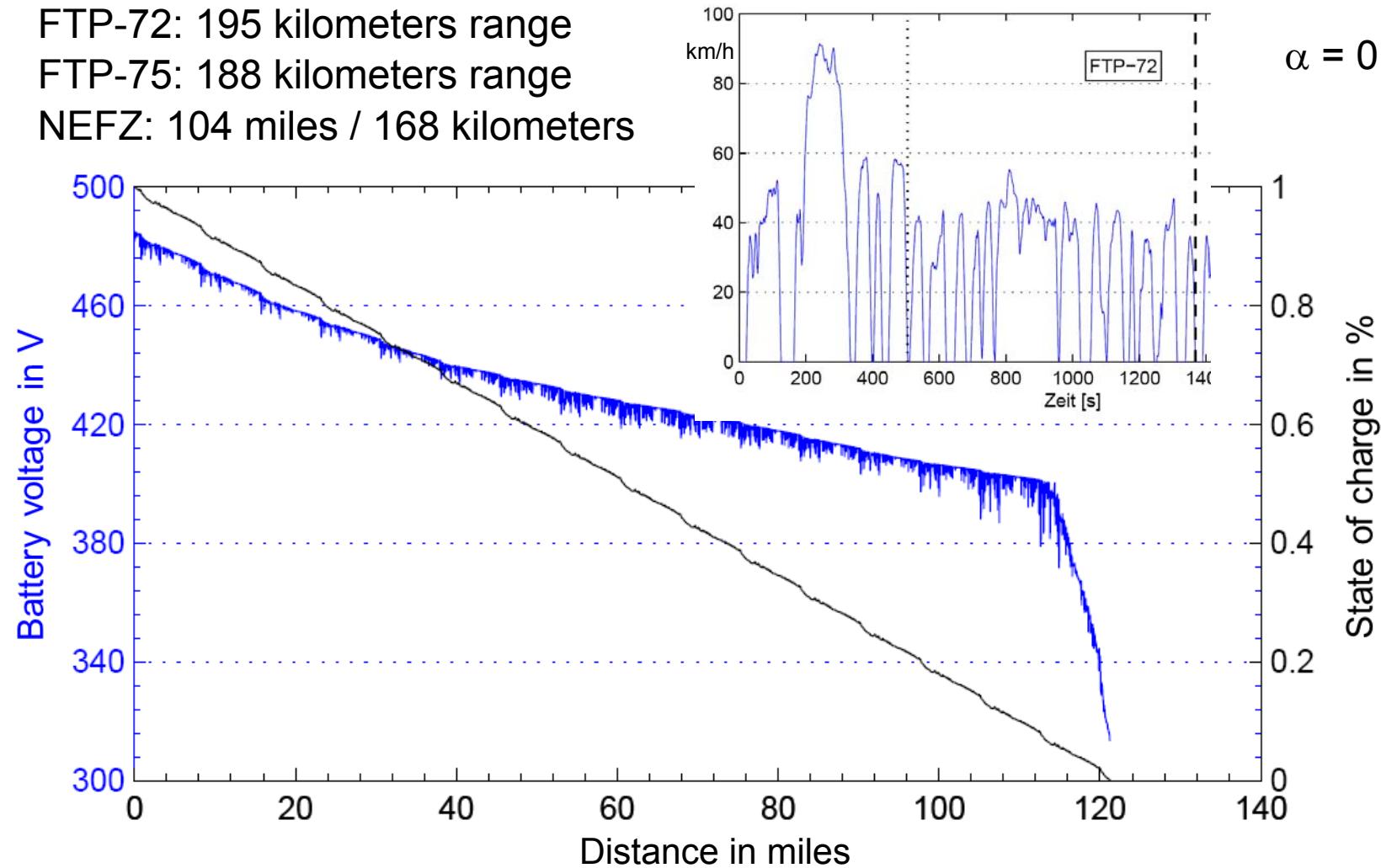
Losses in W	Point 1 ( $n_N / M_d$ )	Point 2 ( $n_N / M_{S2}$ )	Point 3 ( $n_{\max} / M_d$ )	Point 4 ( $n_{\max} / M_{S2}$ )
Wheel slip losses	1237	2280	16	936
Gear	190	247	127	365
Power electronics	794	916	736	985
Board grid	150	150	150	150
Motor	1944	3245	3700	5190
Battery	623	1135	51	1605
Sum of losses	4838	7973	4780	9231
Driving power in kW	40.5	52.5	8.4	62.8
Efficiency in %				
Total vehicle	89.3	86.8	63.7	87.2
Motor	95.6	94.4	70.0	92.5
Power electronics	98.4	98.4	94.3	98.5

$$\alpha = 0$$

## Example: Range E-car in FTP-72 cycle



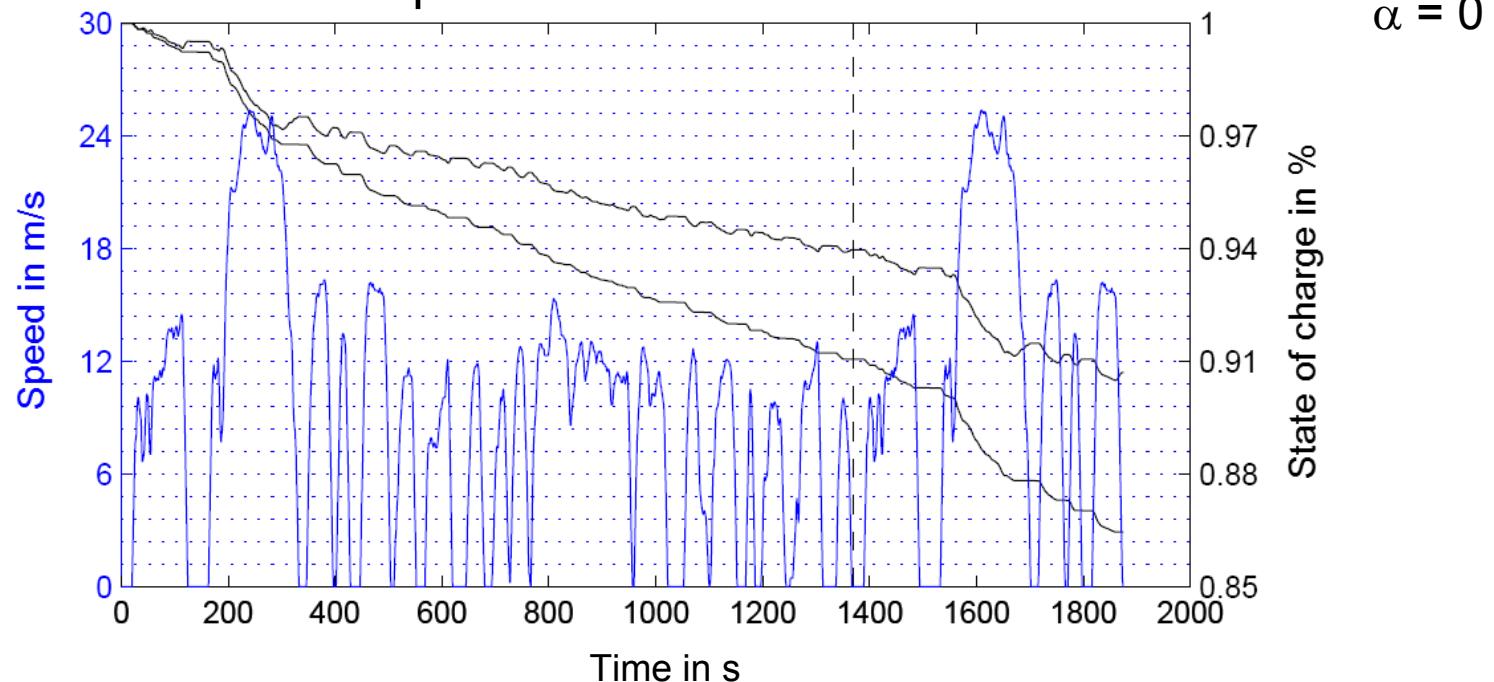
- FTP-72: 195 kilometers range
- FTP-75: 188 kilometers range
- NEFZ: 104 miles / 168 kilometers



# Example: E-car in FTP-72 cycle – Recuperation



- Difference due to recuperation in FTP-72 and FTP-75



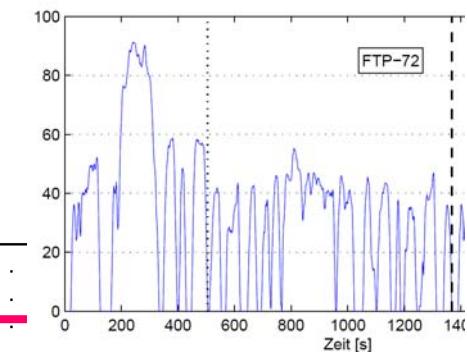
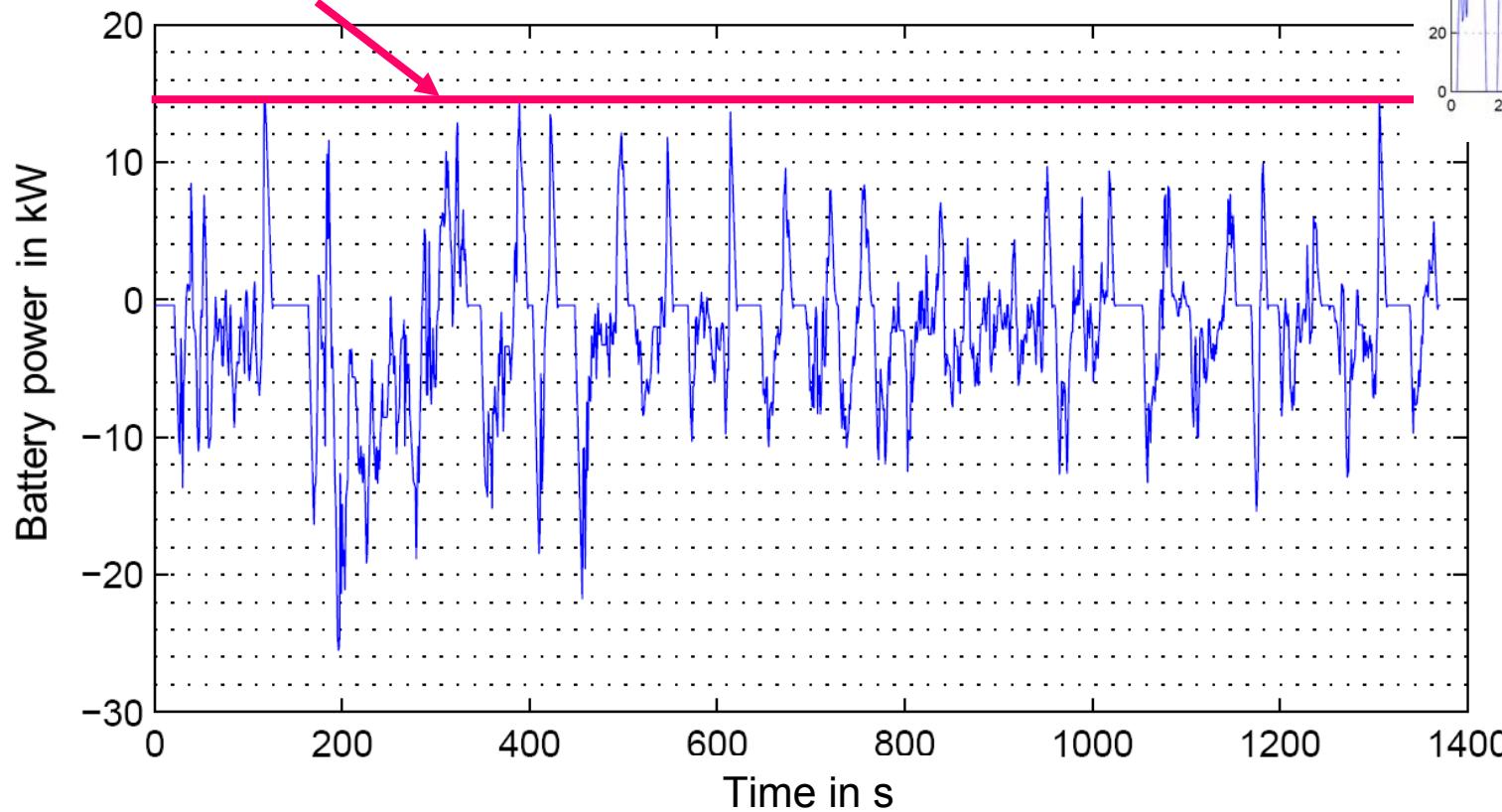
	FTP-72	FTP-75
State of charge with recuperation	94%	91%
State of charge <u>without</u> recuperation	90,9%	86,5%
Savings	34%	33,3%

# Example: E-car in FTP-72 cycle – Battery loading



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- Battery power during FTP-72 cycle
- Limit for feed-back at 14.6 kW



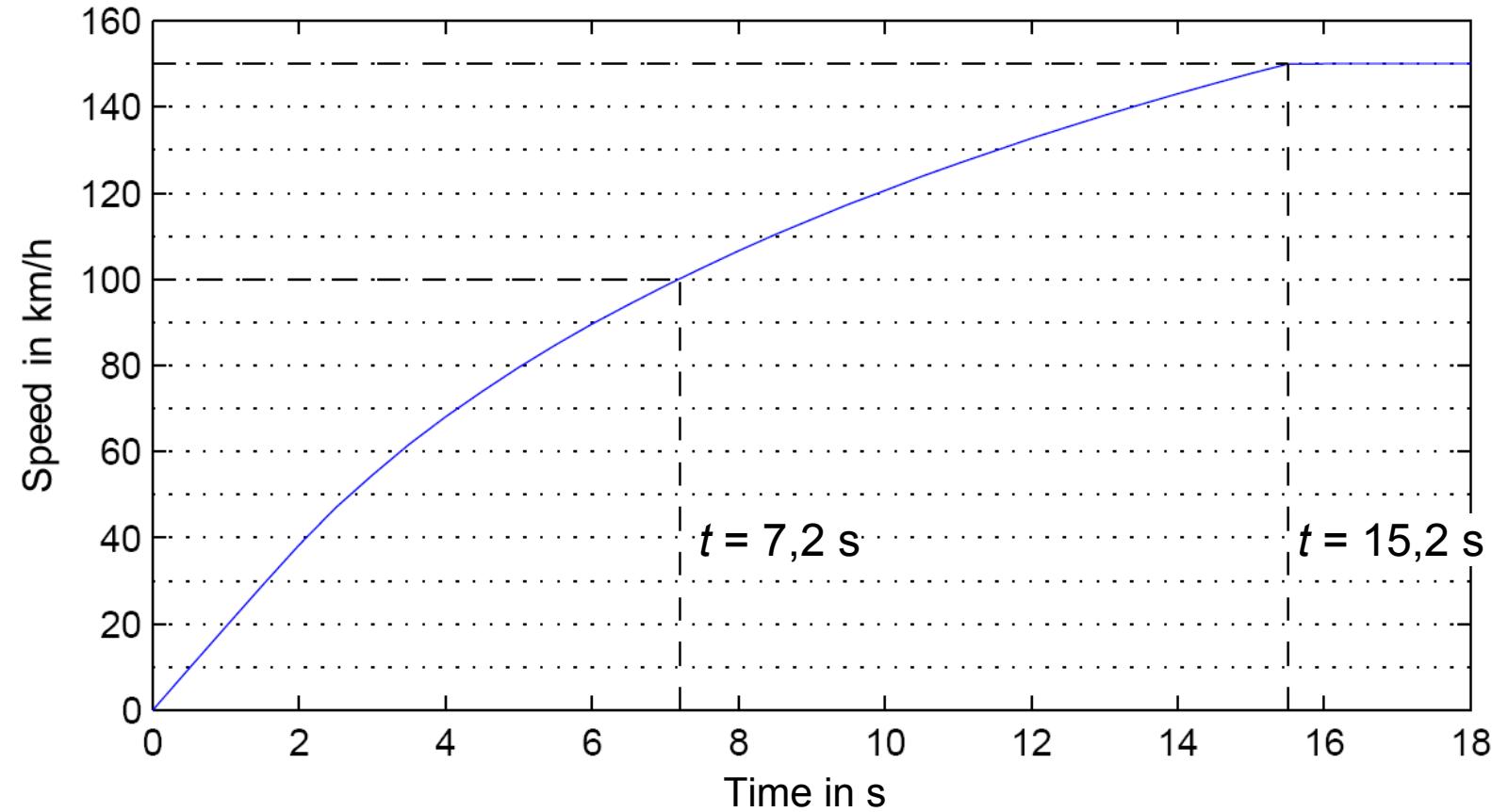
## Example: E-car results in sprint



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- 7,2 seconds from zero to 100 km/h
- 15,2 seconds from zero to 150 km/h

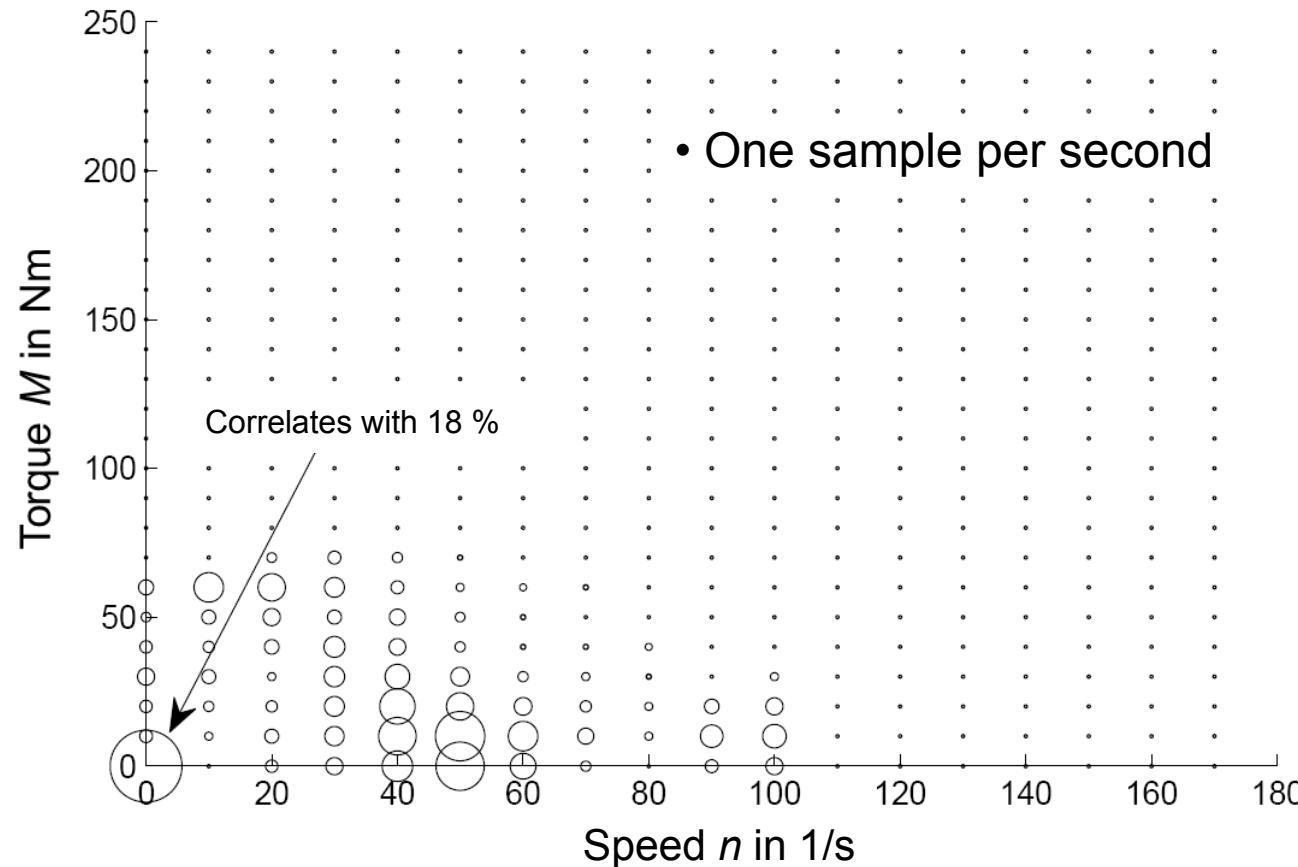
Empty car mass 900 kg,  $\alpha = 0$



# Sample: E-car operating time in % in the motor operation map



- Evenly screened occurrence of operation points during the FTP-72 cycle
- Torque-speed-combinations at gear input in steps of 10 Nm and 10 1/s

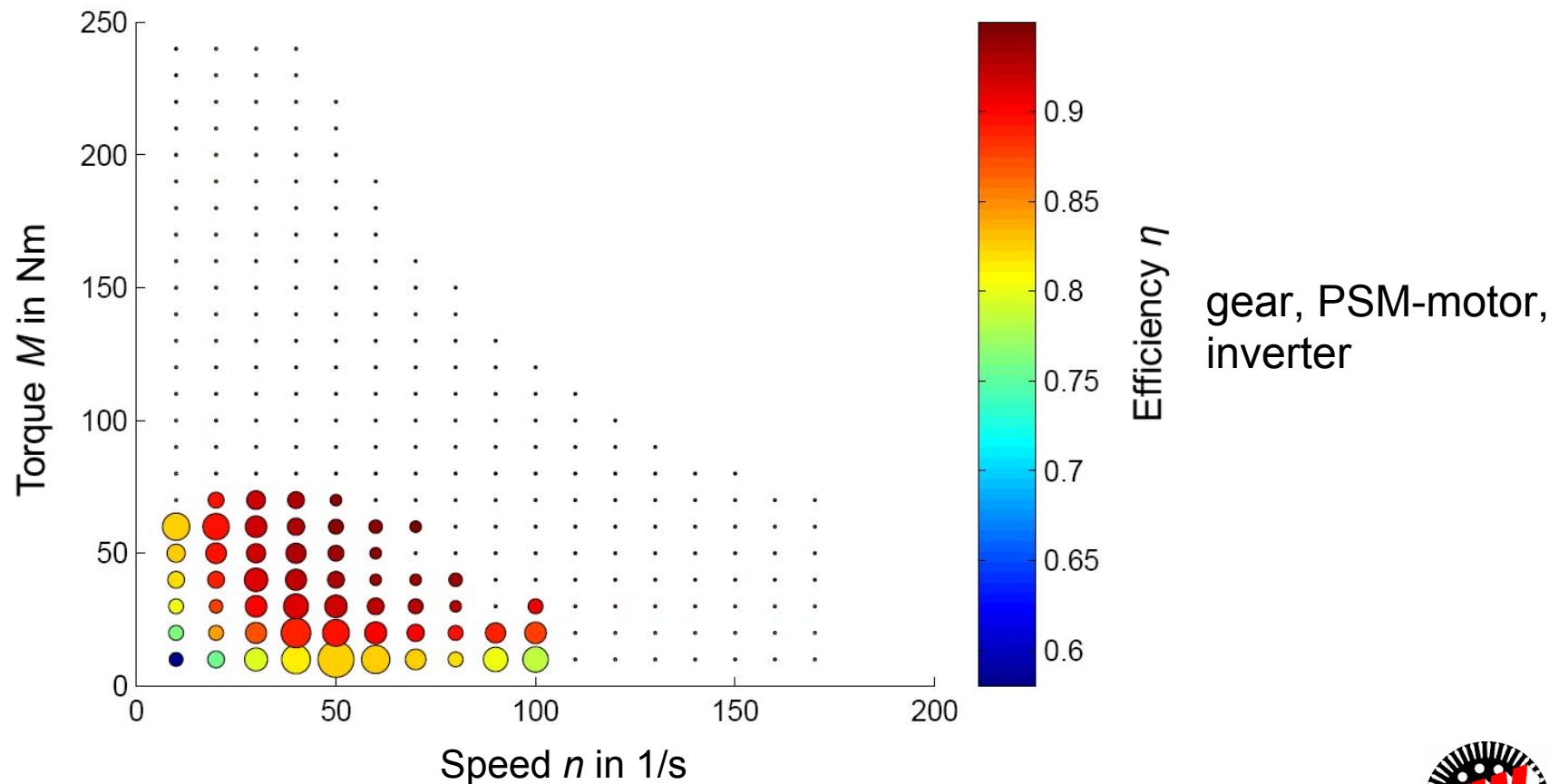


## Example: E-car: Occurrence of different operation points and correlating efficiency during FTP-72 cycle



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- Area size of points = duration of this operation point
- Color = efficiency



# Planning and application of electrical drives (PAED) – Drives for electric vehicles



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*Have fun while self-designing  
an E-car-drive !*



*Source: Tesla roadster*