

# Elektrische Hochdrehzahlantriebe- Auslegungsgrundlagen und Beispiele aus der Praxis



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**Rotor of PM synchronous machine with  
magnetic bearings, 40 kW, 40000/min**

*Source: TU Darmstadt, Germany*

# Elektrische Hochdrehzahlantriebe - Auslegungsgrundlagen & Beispiele aus der Praxis (Electric high-speed drives – design & examples)



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## Contents

- Basics on High-speed Drives
- Mechanical challenges of High-speed drives
- Which type of E-machine for high speed?
- Bearing concepts for high speed
- Electromagnetic design for High-Speed
- Examples for High-Speed drives
- Conclusions



# Basics on High Speed Drives

## Why High-Speed Drives ?

Advantages of high rotational speed  $n$ :

High power  $P$  = Low torque  $M$

$$P = 2\pi \cdot n \cdot M$$

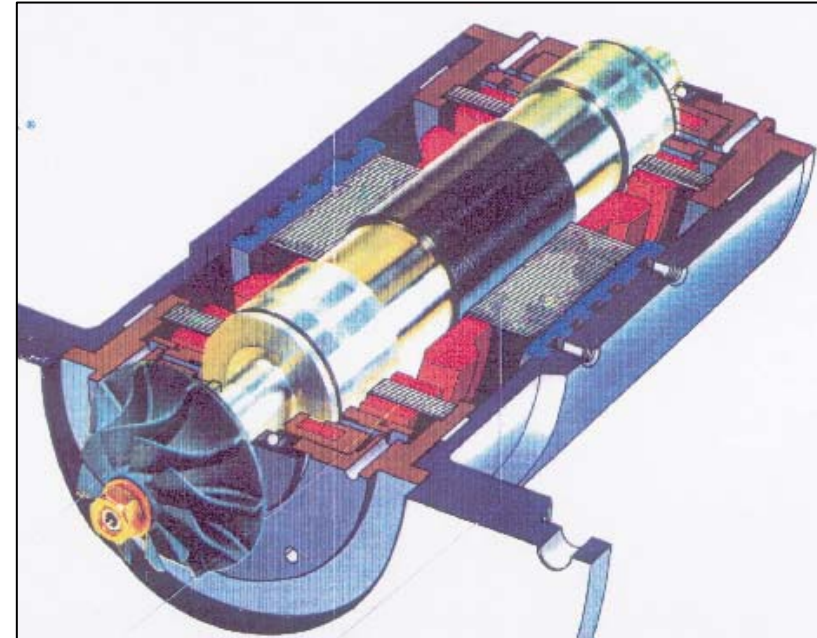
$$M = P / (2\pi \cdot n)$$

“Size” of a machine (volume  $V$ ):

Determined by „torque density”  $m = M/V$

$$V = M / m \sim P / (n \cdot m)$$

High power  $P \Rightarrow$  low torque  $M$  = low volume  $V$



Cut-view: Maglev turbo-compressor rotor

Source: Piller, Germany

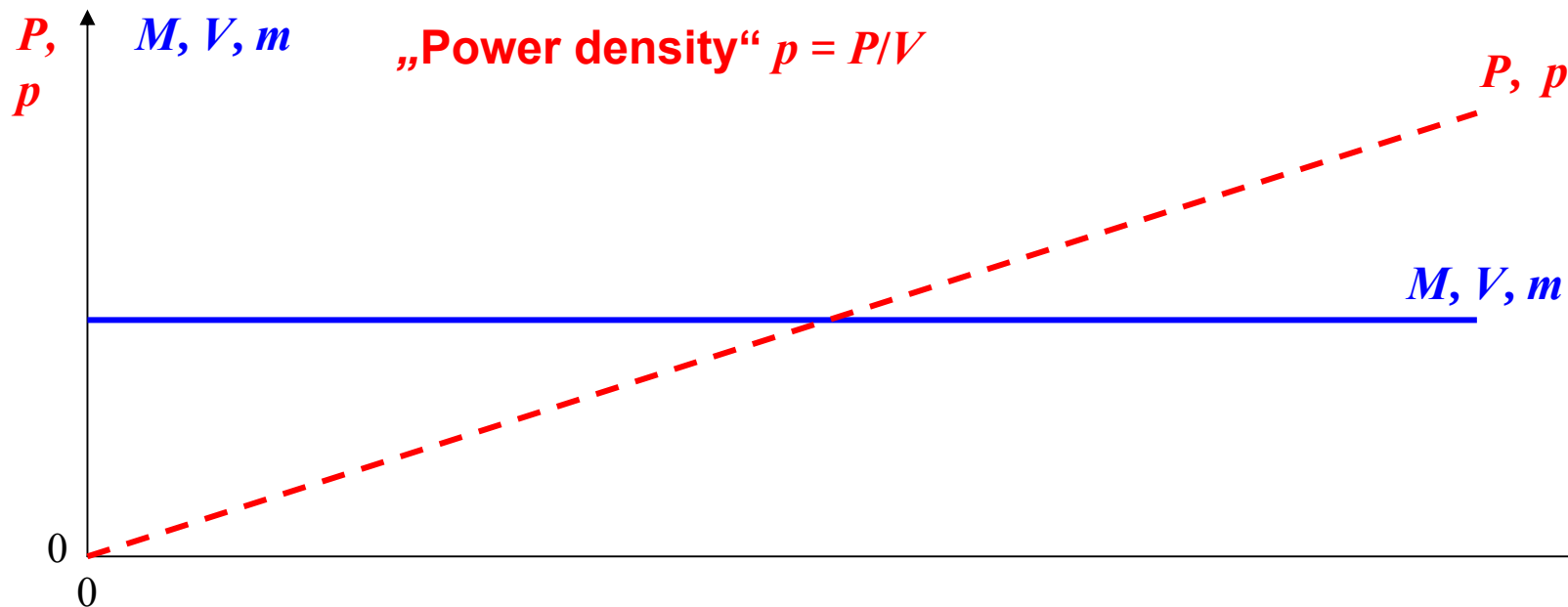
# Motor power determined by speed $P \sim n$

- **Mechanical system = „machine“:**

Torque  $M$  determines machine volume  $V$  via torque density  $m$

Small torque  $M$  = small machine size  $V$

“Power determined by speed”  $P \sim n$



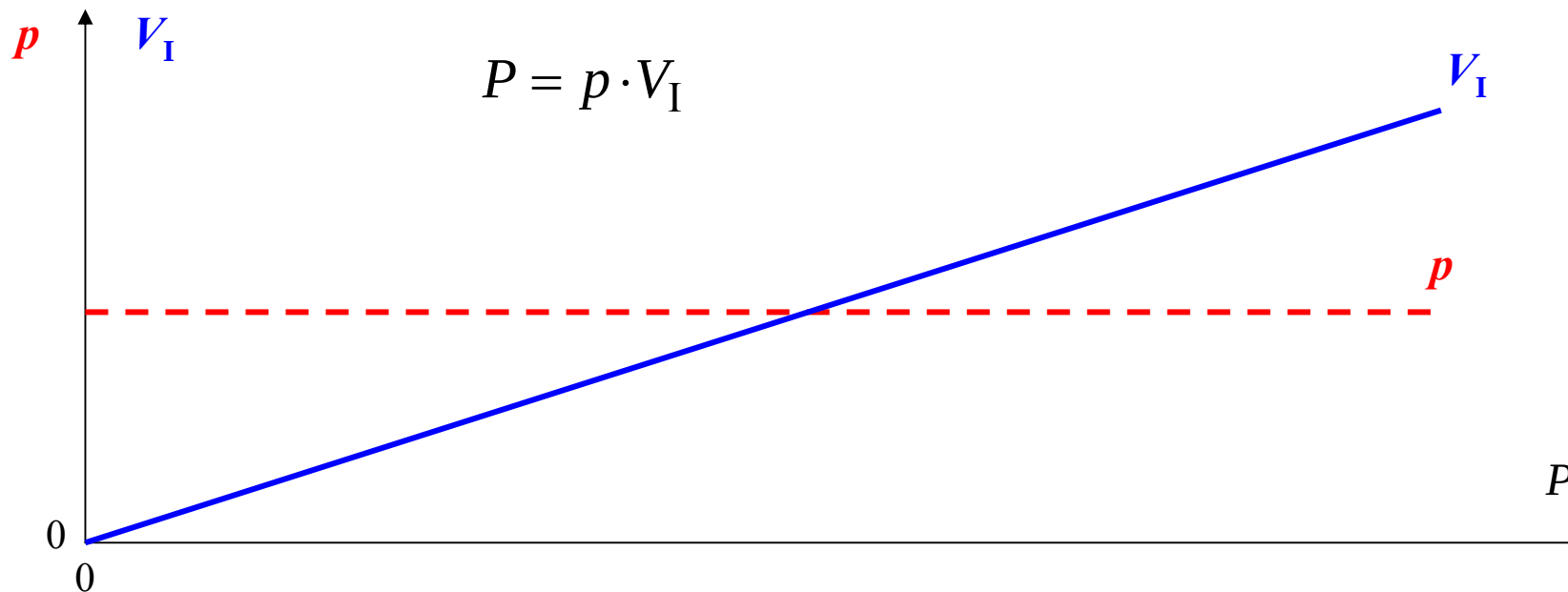
# Inverter size determined by power $V_I \sim P$

- **Electronic system = feeding inverter:**

“Power from voltage  $U$  & current  $I$ “:  $S \sim U \cdot I$

Apparent power  $S = P / \cos\varphi$  determines inverter size (volume  $V_I$ ) via  $p$

Small power  $S$  = small inverter size  $V_I$



# Why “High-Speed” E-Machines?

- Small volume/power  $V/P$  ratio advantageous = “high power density  $p = P/V$ ”
- Gearless drive system = reduced maintenance & vibrations
- Wide rated “power/speed”-range  $P_N/n_N$ :  
(1 000 000 ... 500 000 /min), 0.1 kW ... 3000 /min, 1000 MW
- Increasing field of applications as  
pumps,  
compressors,  
small gas turbines,  
direct coupled air-craft generators,  
high speed cutting drives, ...

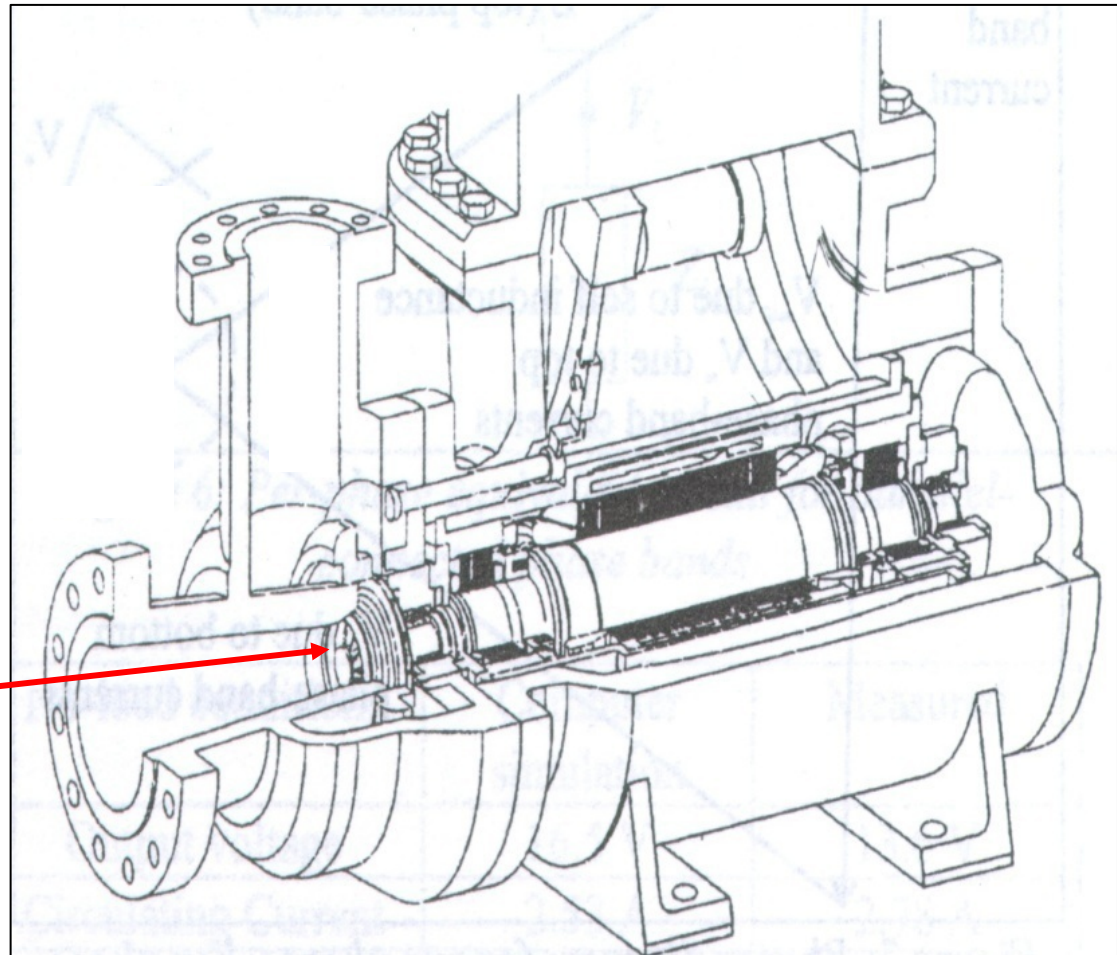
# Typical High-Speed Drive Application

## High-Speed PM generator with single stage turbine

Natural gas expansion turbine:

- *Small volume* at high power
- *Less mass*
- *Gearless direct drive*
- *Low maintenance*  
(magnetic bearings)

*Small single-stage turbine runner* for 500 kW at high speed 32 000 /min!



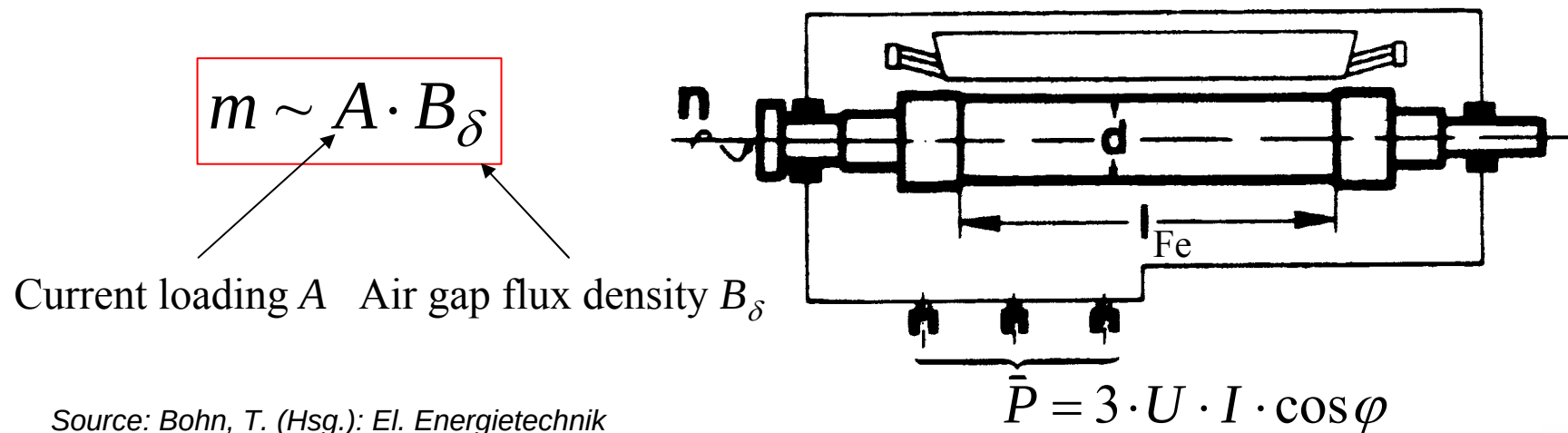
Source: Piller, Germany



# Torque density $m$

- Motor “active volume”  $V$  determined by rotor diameter  $d$  & active rotor length  $l_{Fe}$
- LORENTZ-force:  $F = I \cdot B_\delta \cdot l_{Fe}$  Torque:  $M = z \cdot F \cdot \frac{d}{2} = z \cdot I \cdot B_\delta \cdot l_{Fe} \cdot \frac{d}{2}$
- Three-phase winding,  $N_s$  turns per phase =  $z$  conductors:  $z = 3 \cdot 2N_s$

• **Torque density:**  $m = \frac{M}{V} = \frac{z \cdot I \cdot B_\delta \cdot l_{Fe} \cdot \frac{d}{2}}{d^2 \cdot l_{Fe} \cdot \pi / 4} \sim \frac{z \cdot I}{d \cdot \pi} \cdot B_\delta = A \cdot B_\delta$



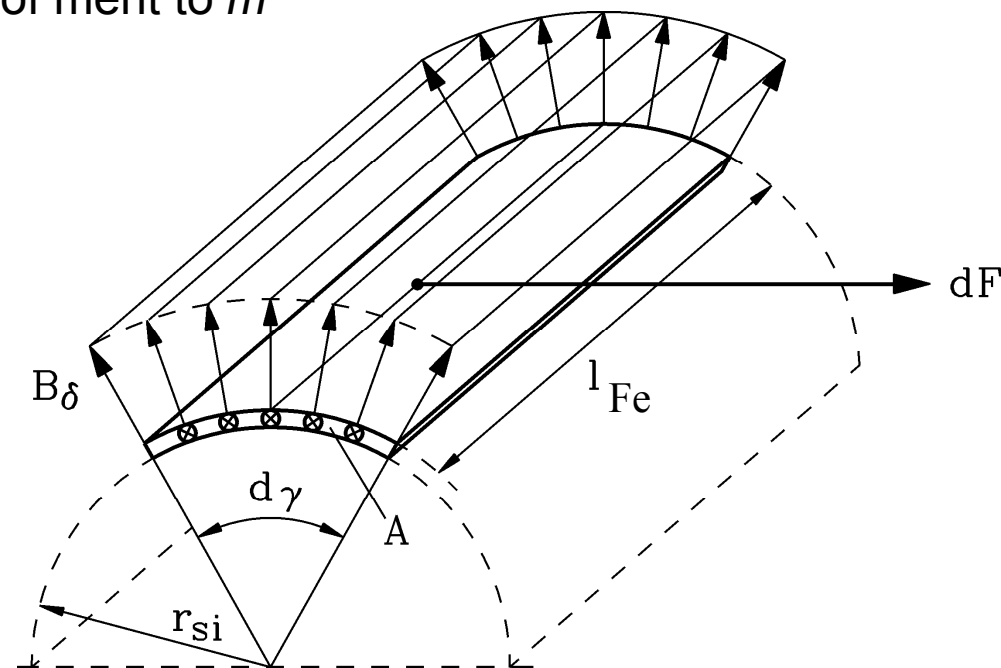
Source: Bohn, T. (Hsg.): El. Energietechnik



# Specific thrust $\tau$

„Specific thrust“: 
$$\tau = \frac{z \cdot F}{d \cdot \pi \cdot l_{Fe}} = \frac{2M}{d^2 \cdot \pi \cdot l_{Fe}} = \frac{m}{2}$$

$\tau$ : Alternative figure of merit to  $m$



# Elektrische Hochdrehzahlantriebe - Auslegungsgrundlagen & Beispiele aus der Praxis (Electric high-speed drives – design & examples)



## Contents

- Basics on High-speed Drives
- **Mechanical challenges of High-speed drives**
- Which type of E-machine for high speed?
- Bearing concepts for high speed
- Electromagnetic design for High-Speed
- Examples for High-Speed drives
- Conclusions



# Mechanical challenges of High-speed drives

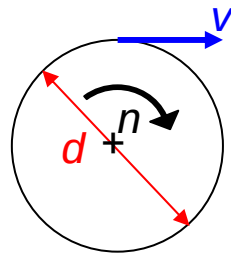
- **Challenge 1:** Rotor integrity at high speed due to high centrifugal forces
  - **Challenge 2:** Rotor vibrations, excited by rotating imbalance forces  
⇒ Elastic vibration behaviour of rotor  
= **rotor dynamics**
- ⇒ **Rotor strength** and **rotor dynamics**  
dominate the High-speed-machine design !

## Challenge 1: What means “High-Speed” ?

- NOT ONLY: High “revolutions per second”  $n$  !

BUT:

High rotor circumference speed  $v$



$$v = d \cdot \pi \cdot n \cong 100 \dots 250 \text{ m/s}$$

( $d$ : Rotor outer diameter)

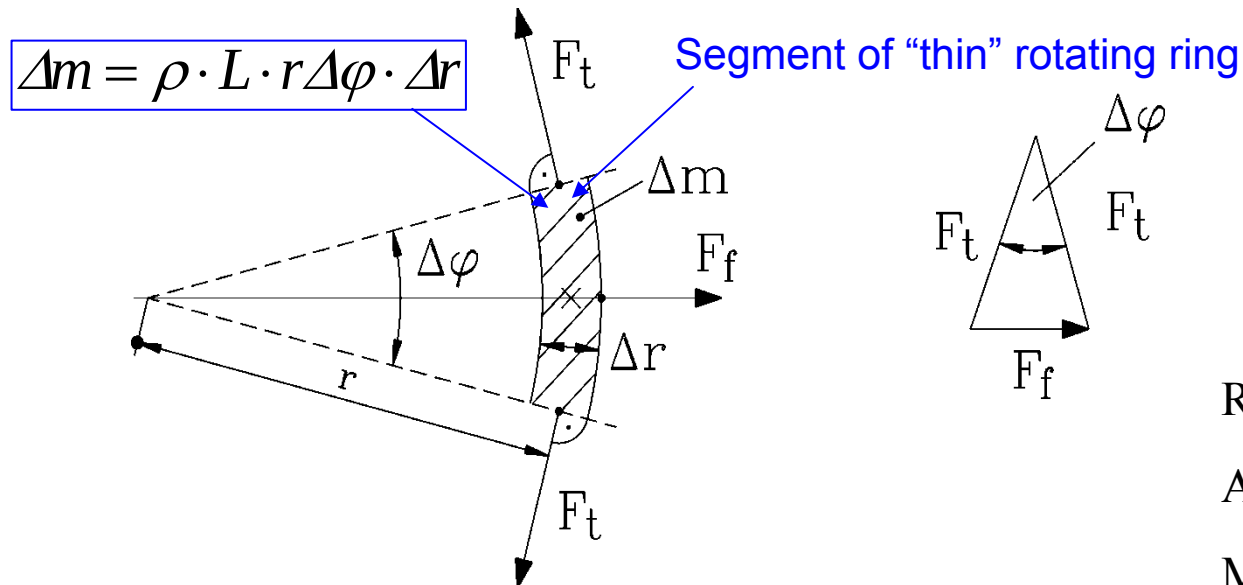
- High mechanical (tangential) stress  $\sigma_t$  due to high centrifugal forces !

⇒ Stress  $\sigma$  proportional to mass density  $\rho$  and to  $v$  !

$$\sigma_t \sim \rho \cdot v^2$$

## Example:

### Tangential stress $\sigma_t$ in a “thin” rotating ring



$$F_f = \Delta m \cdot r \cdot (2\pi n)^2$$

$$F_f \approx F_t \cdot \Delta \varphi$$

Ring diameter  $d = 2r$

Axial length  $L$

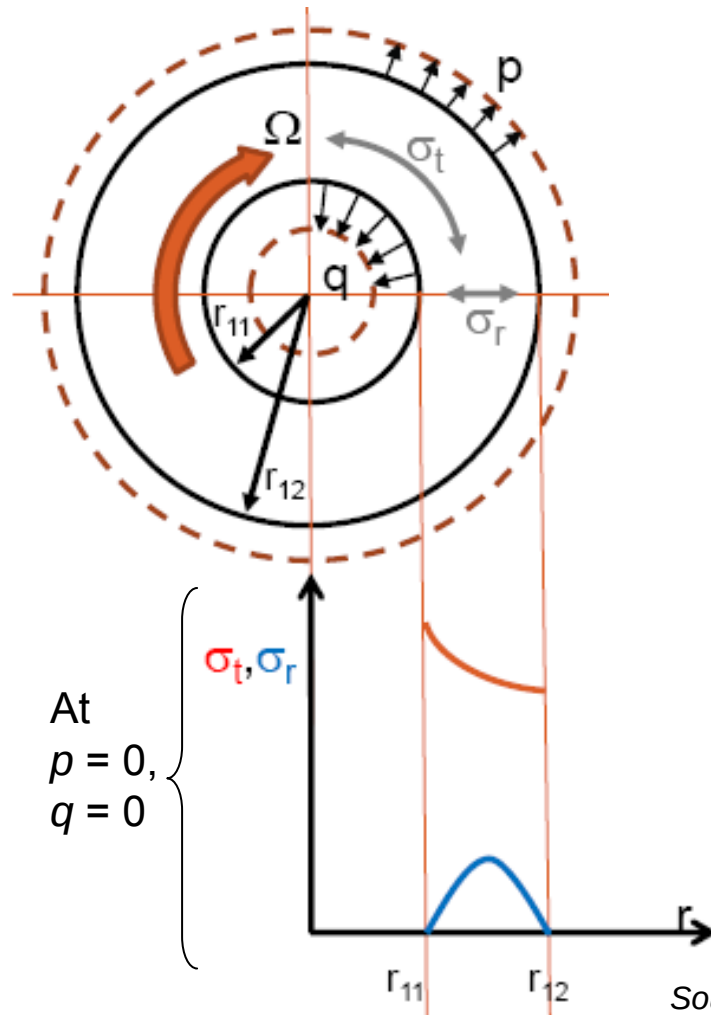
Mass density  $\rho$

Tangential stress  $\sigma_t$  :

$$\sigma_t = \frac{F_t}{L \cdot \Delta r} \approx \frac{F_f / \Delta \varphi}{L \cdot \Delta r} = \rho \cdot r^2 \cdot (2\pi n)^2 = \rho \cdot v^2$$

$$\sigma_t = \rho \cdot v^2$$

# Rotor stress distribution



$$\Omega = 2\pi \cdot n$$

## Rotor model as rotating „thick“ ring:

- **Tangential** and **radial** stress
- General loading:  
Centrifugal load ( $\Omega$ ), shrink fit load ( $p, q$ ),  
thermal expansion stress load ( $p, q$ )
- At pure centrifugal load:  $p = 0, q = 0$ :

$$\sigma_t \sim \rho \cdot v^2 \quad \sigma_r \sim \rho \cdot v^2 \quad \sigma_t \gg \sigma_r$$

⇒ Dominating **tangential** stress

Source: Canders, W.-R.: TU Braunschweig, 2014

## Example: “High-Speed” stress

$$\sigma_t \sim \rho \cdot v^2$$

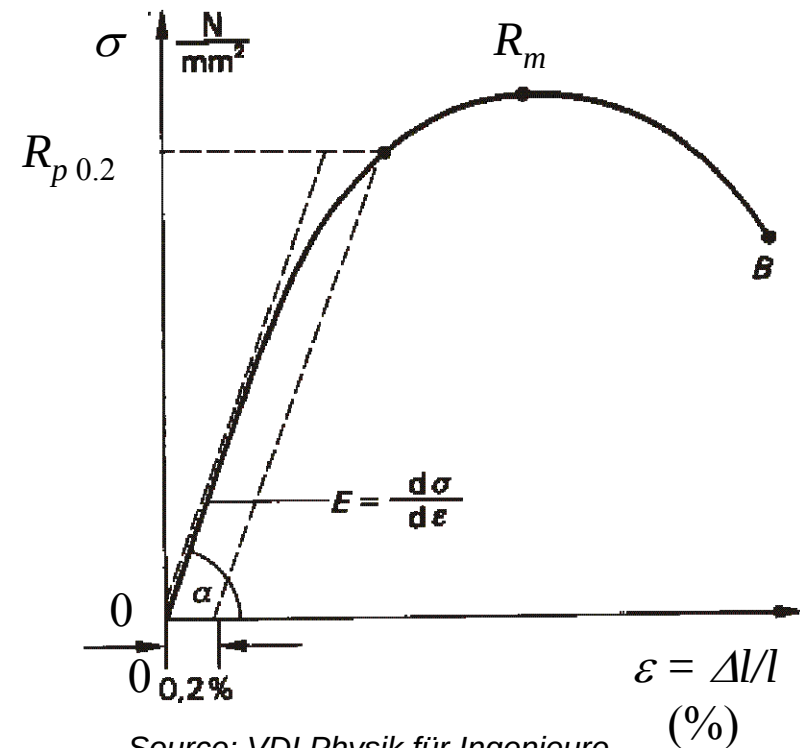
Yield strength of steel sheet:

$$R_{p,0.2} = 350 \text{ N/mm}^2$$

ROTATING “thin” steel ring ( $\rho = 7850 \text{ kg/m}^3$ )  
at  $v = 211 \text{ m/s}$

Tangential stress reaches yield strength  
at which ring diameter  $d$ ?

- a) At  $d = 1.3 \text{ m}$ :  $n = 3\,000 \text{ /min}$
- b) At  $d = 90 \text{ mm}$ :  $n = 45\,000 \text{ /min}$



⇒ BOTH speed levels 3000/min & 45 000/min are **“high-speed” cases!**



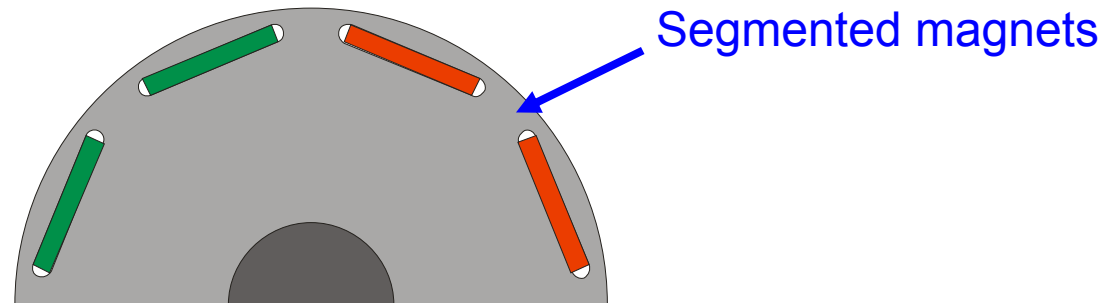
# Typical “High-Speed” limits

- Circumferential speed  $v$  is the „characteristic“ parameter for rotor strength
- „High speed“ means typically:  $v \geq 100 \text{ m/s}$

Typical **circumferential speed limits** for different E-machine designs:

| Permanent magnet synchronous machine | Permanent magnet synchronous machine  | Synchronous machine, el. excitation | Synchronous machine, el. excitation | Induction motor                  |
|--------------------------------------|---------------------------------------|-------------------------------------|-------------------------------------|----------------------------------|
| Buried magnets                       | Surface magnets, carbon fibre bandage | Salient pole                        | Cylindrical massive rotor           | Massive cage rotor with end caps |
| 80 m/s                               | 280 m/s                               | 90 m/s                              | 220 m/s                             | 200 m/s                          |

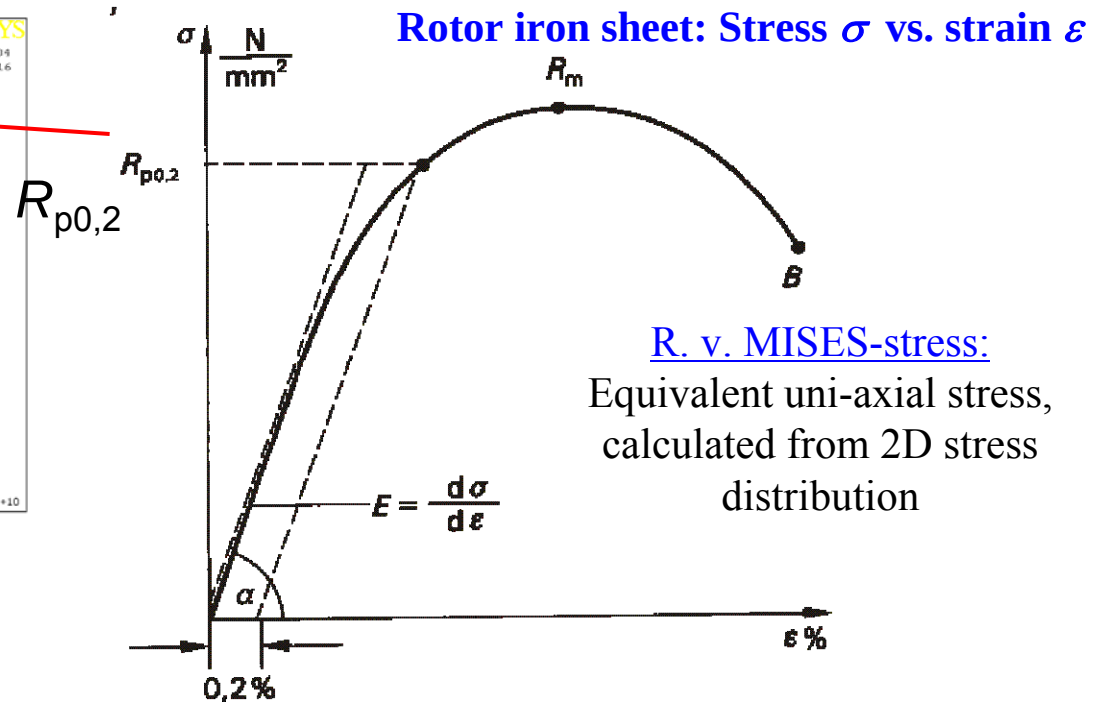
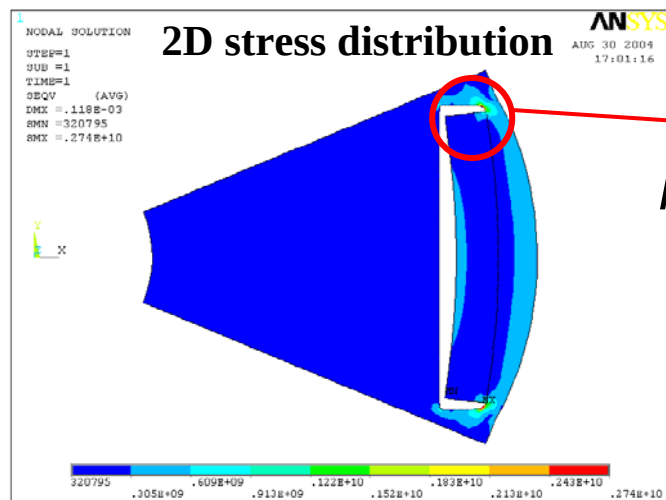
# Fixing buried magnets at high speed (1)



- No bandage  $\Leftrightarrow$  magnets are fixed by rotors sheets
- Small magnetic air gap
- Less magnet material in case of flux concentration
- **Segmented magnets** per pole with radial iron bridges for higher centrifugal force capability

## Fixing buried magnets at high speed (2)

- Detailed mechanical calculation necessary, requires **Finite Element Calculation**
- Max. tensile strength must stay below 0.2%-deformation limit of sheet  $R_{p0,2}$

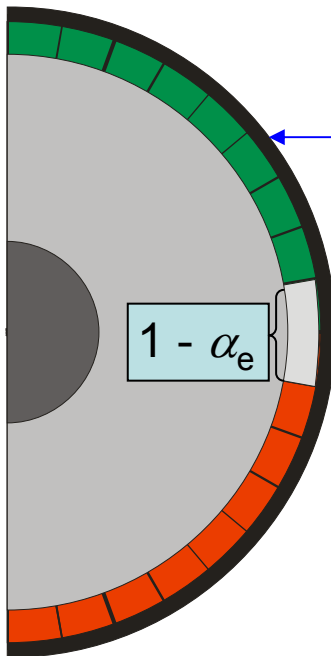


R. v. MISES-stress:  
Equivalent uni-axial stress,  
calculated from 2D stress  
distribution

Source: VDI Physik für Ingenieure

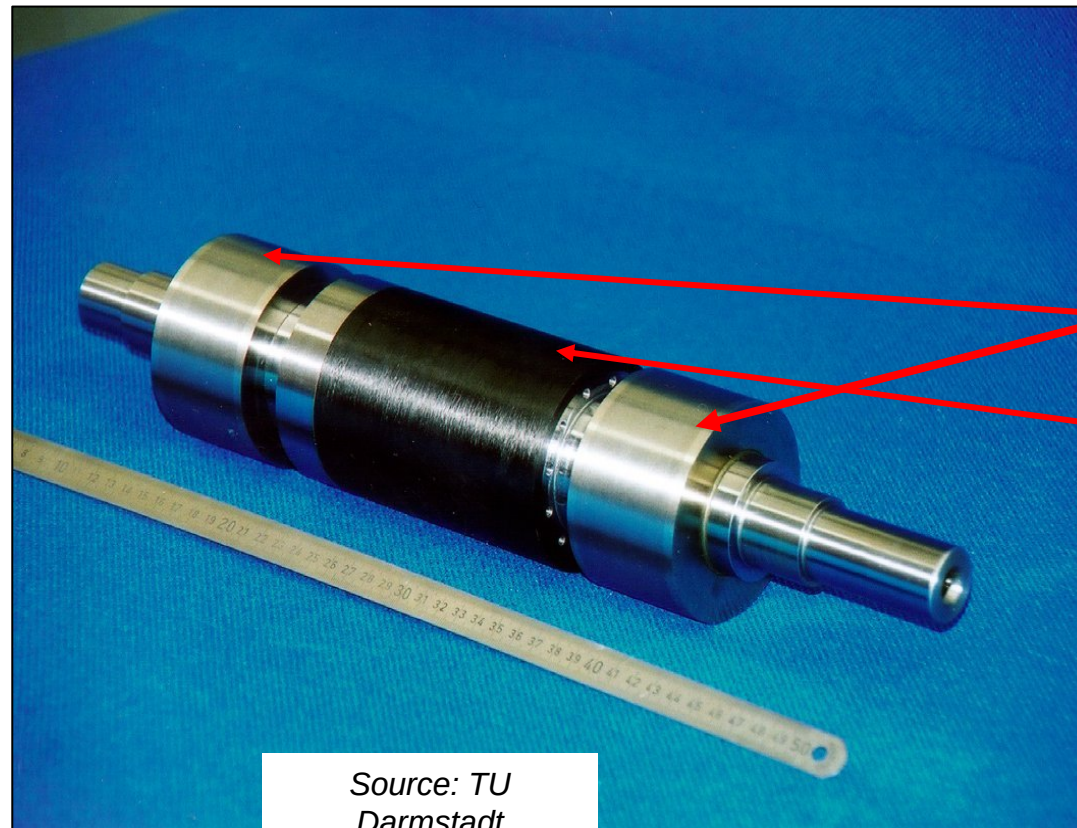
# Fixing of magnets by bandage

## Surface mounted magnets $\alpha_e < 1$ “dangerous”!



Pre-fabricated CFC bandage, pressed onto rotor

- 4-pole rotor
- Pole coverage ratio  $\alpha_e = 8/9 < 1$



PM-Rotor

40 kW,  
40000/min

Magnetic  
bearings

Carbon fiber  
bandage

Outer diameter:  
ca. 90 mm

Source: TU  
Darmstadt

## Example:

# Damaged Rotor due to Magnet Edge Pressure

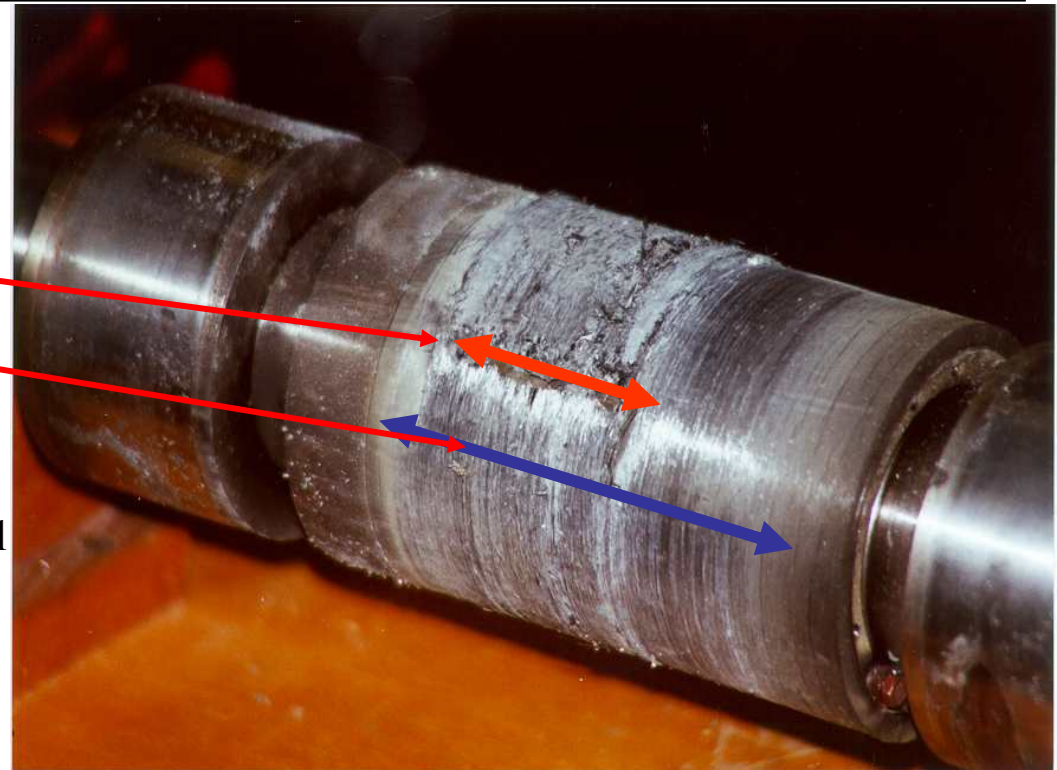
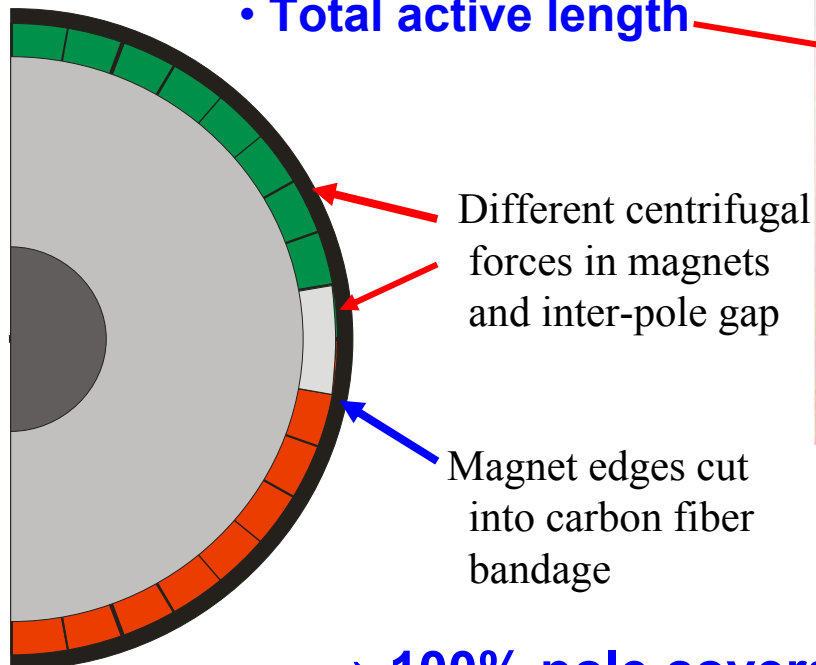


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Breaking of bandage at  
35 000/min

• Break length

• Total active length



4-pole rotor with PM,  
carbon fiber bandage and magnetic bearings

Source: TU Darmstadt

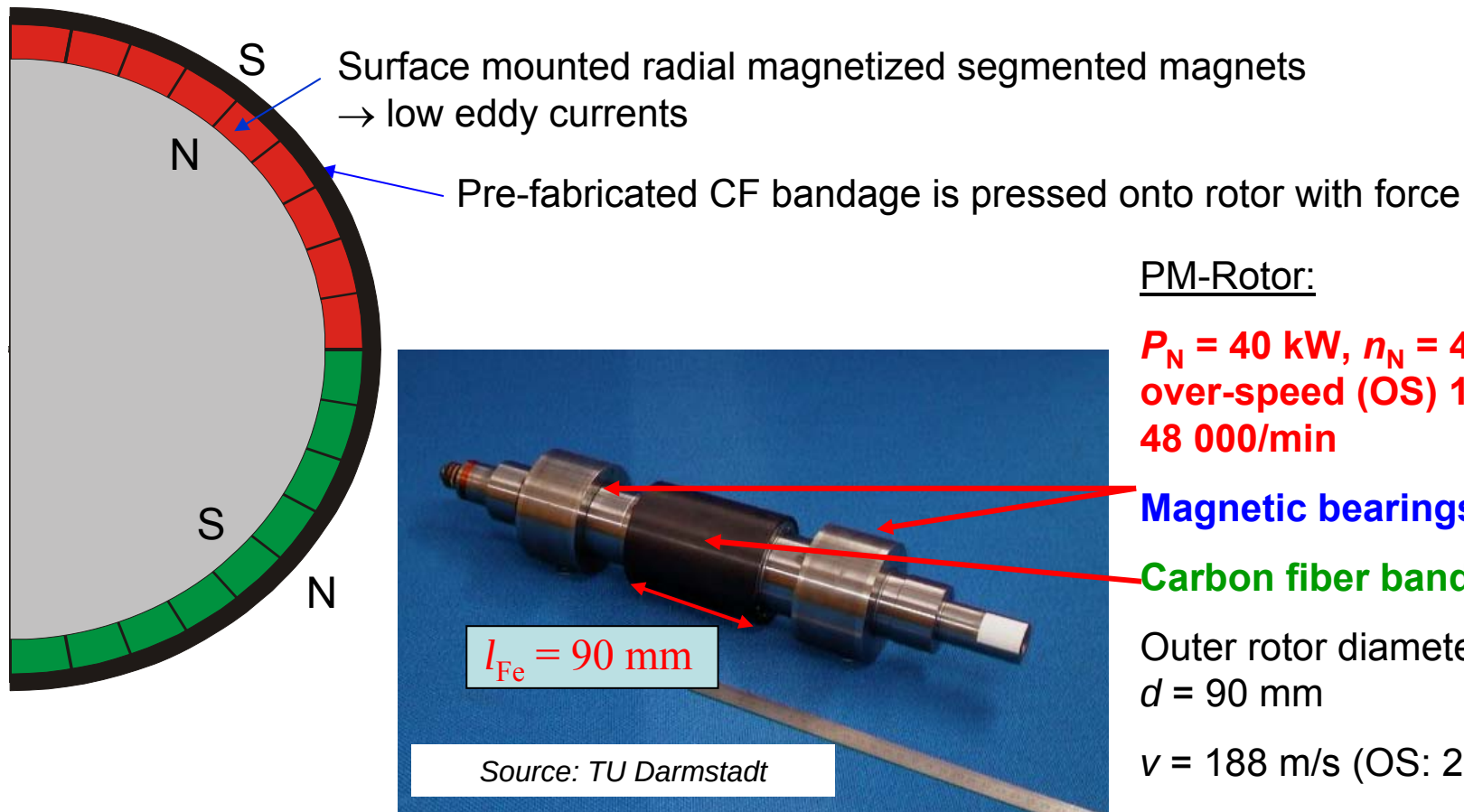
⇒ 100% pole coverage ratio recommended  $\alpha_p = 1$  !



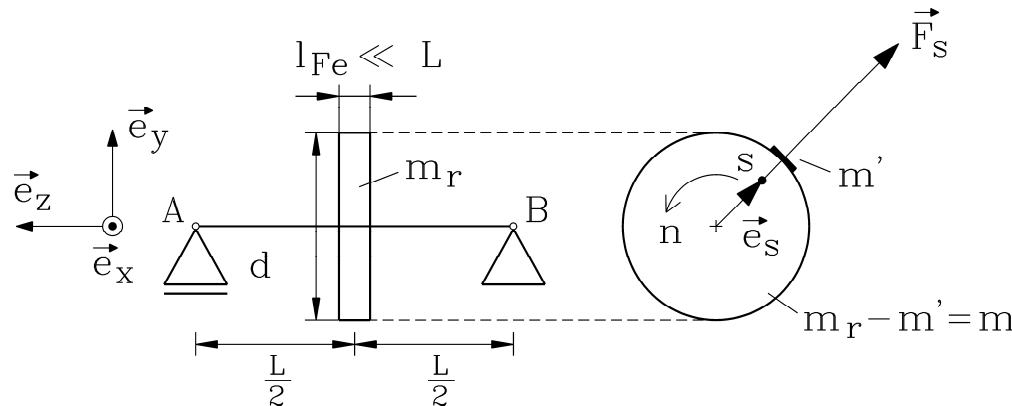


# PM synchronous rotor, 100% coverage

Example: Distributed double-layer integer-slot stator winding,  
semi-closed stator slots, 4-pole rotor, pole coverage ratio 100%



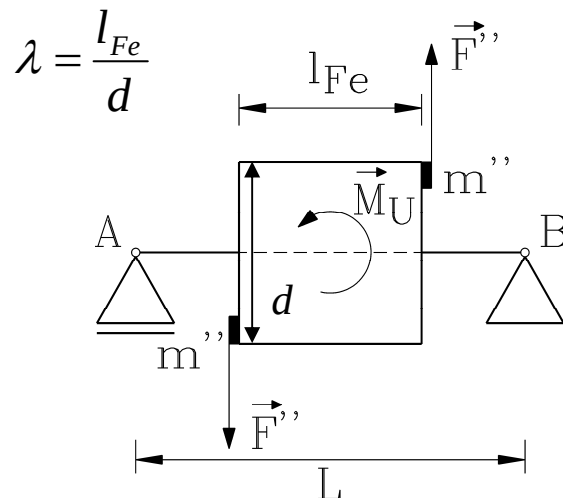
## Challenge 2: Rotor dynamics: Residual rigid rotor imbalance



1) „Static“ imbalance  $U_S$   
at disk-like rotor ( $l_{Fe} \ll L$ )  
leads to imbalance force  $F_S$

$$\vec{U}_S = m_r \cdot \vec{e}_S \Rightarrow \vec{F}_S = m_r \cdot \vec{e}_S \cdot \Omega^2$$

$$\Omega = 2\pi \cdot n$$



S: Center of gravity  
 $m', m''$ : Imbalance mass

$m_r$ : Rotor mass  
 $F_S$ : Centrifugal force

2) „Dynamic“ imbalance  $M_U$

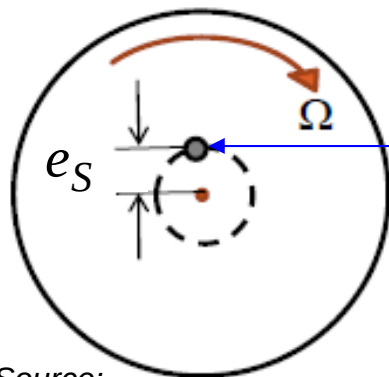
at „long“ rotor ( $l_{Fe} \sim L$ )

leads to imbalance torque  $M'' = F'' \cdot l_{Fe}$

$$M_U = m'' \cdot \frac{d}{2} \cdot l_{Fe} \rightarrow M'' = F'' \cdot l_{Fe} = m'' \cdot \frac{d}{2} \cdot l_{Fe} \cdot \Omega^2$$

# Quality class **G** of rotor imbalance

- Imbalance forces: **Counter-balanced** by balancing masses in two rotor planes for static and dynamic imbalance = “rotor balancing”
- **Residual imbalance** after “rotor balancing” NOT zero  $\Rightarrow$  “Imbalance class” **G**



Orbiting centre of gravity with  $\Omega$

$$v_s = G: \text{Orbiting circumference velocity} \quad v_s = \Omega \cdot e_s$$

$G$  = Quality class of imbalance (ISO 1940)

Typical for high speed machines:  $G = 1 \text{ mm/s}$  or  $0.4 \text{ mm/s}$

Source:  
Canders, W.-R.:  
TU Braunschweig, 2014

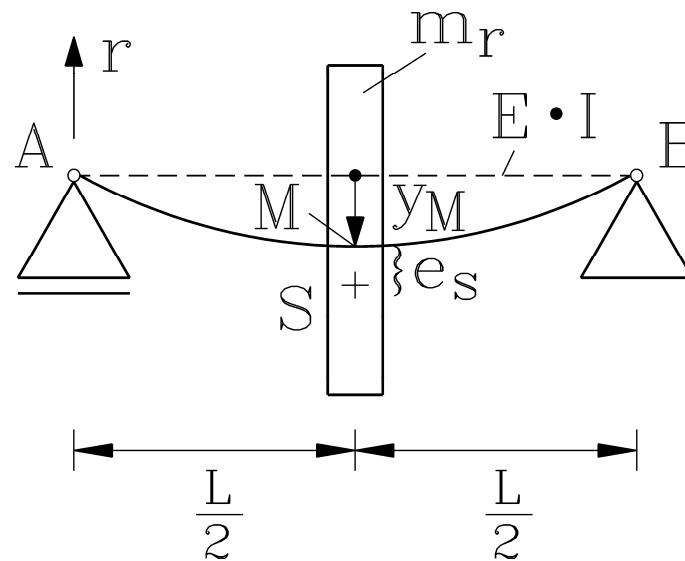
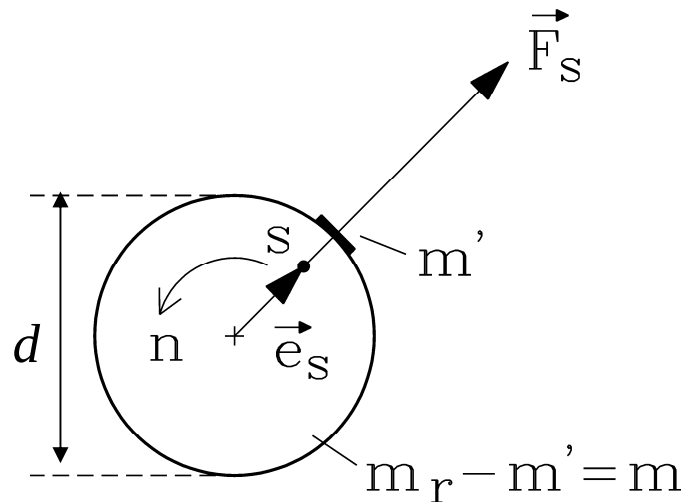
**Example:** „Static“ imbalance  $U_s$ :

$$e_s = 0.24 \mu\text{m}, n = 40\,000/\text{min} \Rightarrow G = 1 \text{ mm/s}$$



# Rotating imbalance forces excite rotor vibrations (1)

- The rotating residual imbalance forces **excite rotor vibrations** with rotational speed  $n$ , because a) the **bearings are not rigid**, but elastic, b) the **rotor is elastic** and allows bending deformation  $y_M$



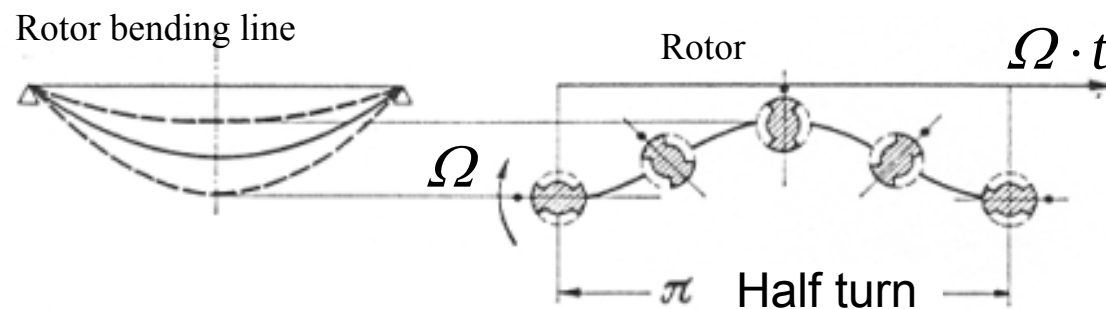
# Rotating imbalance forces excite rotor vibrations (2)

Different additional vibration excitations exist:

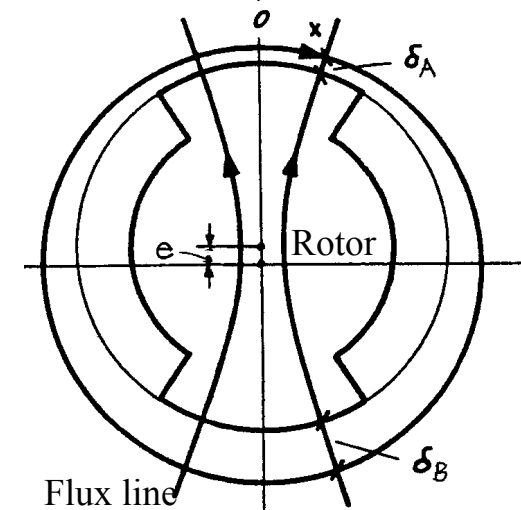
- Misaligned coupling,
- Anisotropic rotor stiffness,
- Rotor eccentricity  $e$ :

(i) Static and (ii) dynamic ( $\Omega$ -depending) rotor eccentricity value  $e$ ;  
In combination with single-sided unbalanced magnetic pull !

Source: Wiedemann, E.; Kellenberger, W.;  
Springer-Verlag, 1968



Anisotropic rotor stiffness

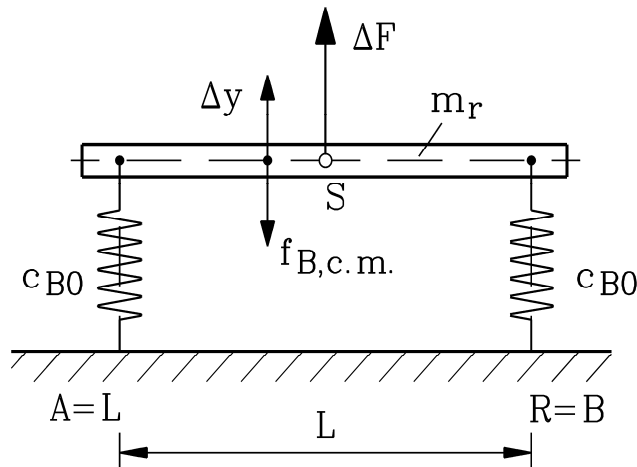


Rotor eccentricity  $e$

# Rigid rotor vibrates in elastic bearings: „Rigid body mode vibration“

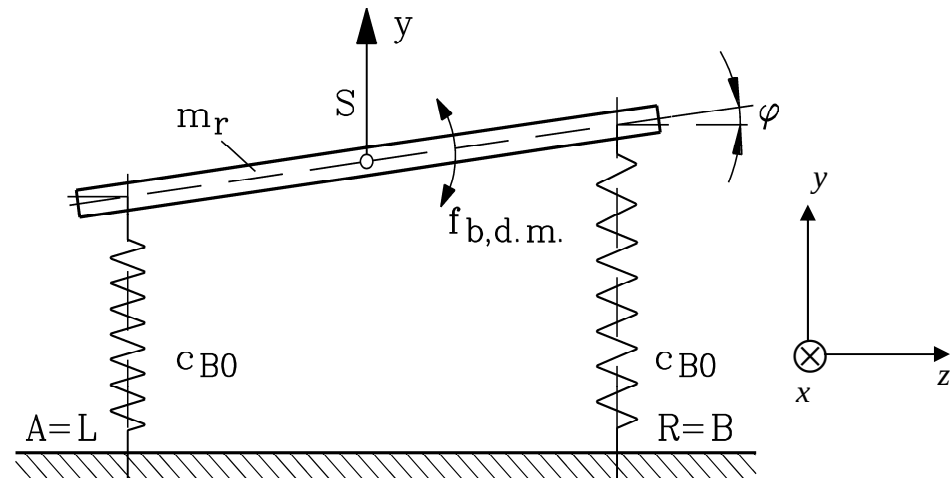
- Elastic bearings are represented by spring constant  $c_{B0} \Rightarrow$  Two vibration modes

## Common mode vibration



$$f_{B,c.m.} = \frac{1}{2\pi} \cdot \sqrt{\frac{c_{B0}}{m_r}}$$

## Differential mode vibration



$$f_{B,d.m.} = \frac{1}{2\pi} \cdot \frac{L}{2} \cdot \sqrt{\frac{c_{B0}}{J_x}} > f_{B,c.m.}$$

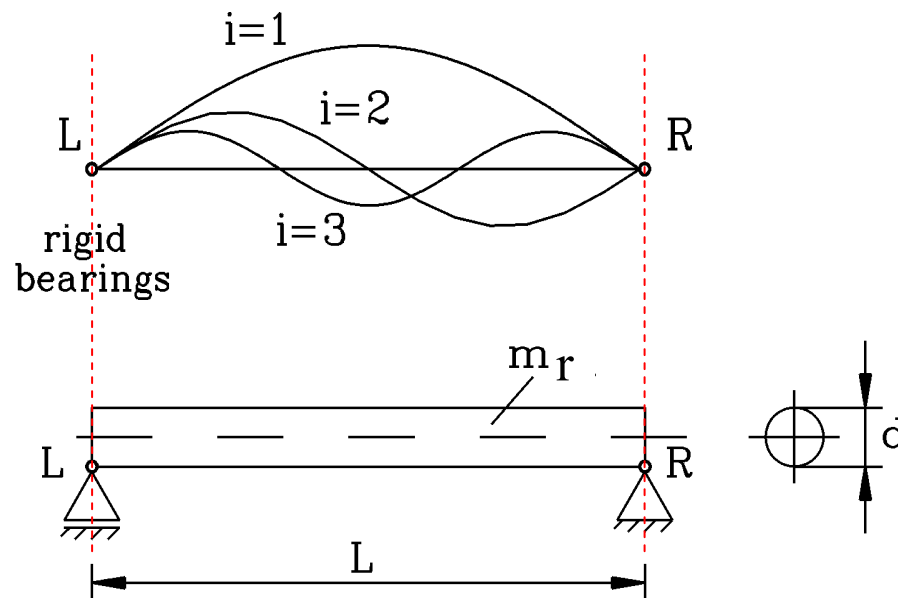
$J_x$ : Angular momentum around x-axis

Source: Parkus Mechanik fester Körper, Springer, Vienna

# Bending of elastic rotor in rigid bearings

- **Simplified approach: Rotor (shaft) considered as elastic cylindrical beam:**  
Diameter  $d$ , length  $L$  between bearings, mass density  $\rho$ , Young's modulus  $E$
- **Bending vibrations with “eigen”-frequencies  $f_b$**  (at rigid bearings):

$$f_{b,i} = \frac{1}{2\pi} \cdot \left( \frac{i \cdot \pi}{L} \right)^2 \cdot \sqrt{\frac{E}{\rho}} \cdot \frac{d}{4} \quad i = 1, 2, 3, \dots \quad \text{mode number } i \quad m_r = \rho \cdot L \cdot d^2 \cdot \pi / 4$$



## Example:

$$i = 1: \quad 703 \text{ Hz}$$

$$i = 2: \quad 2^2 \cdot 703 = 2812 \text{ Hz}$$

$$i = 3: \quad 3^2 \cdot 703 = 6327 \text{ Hz}$$

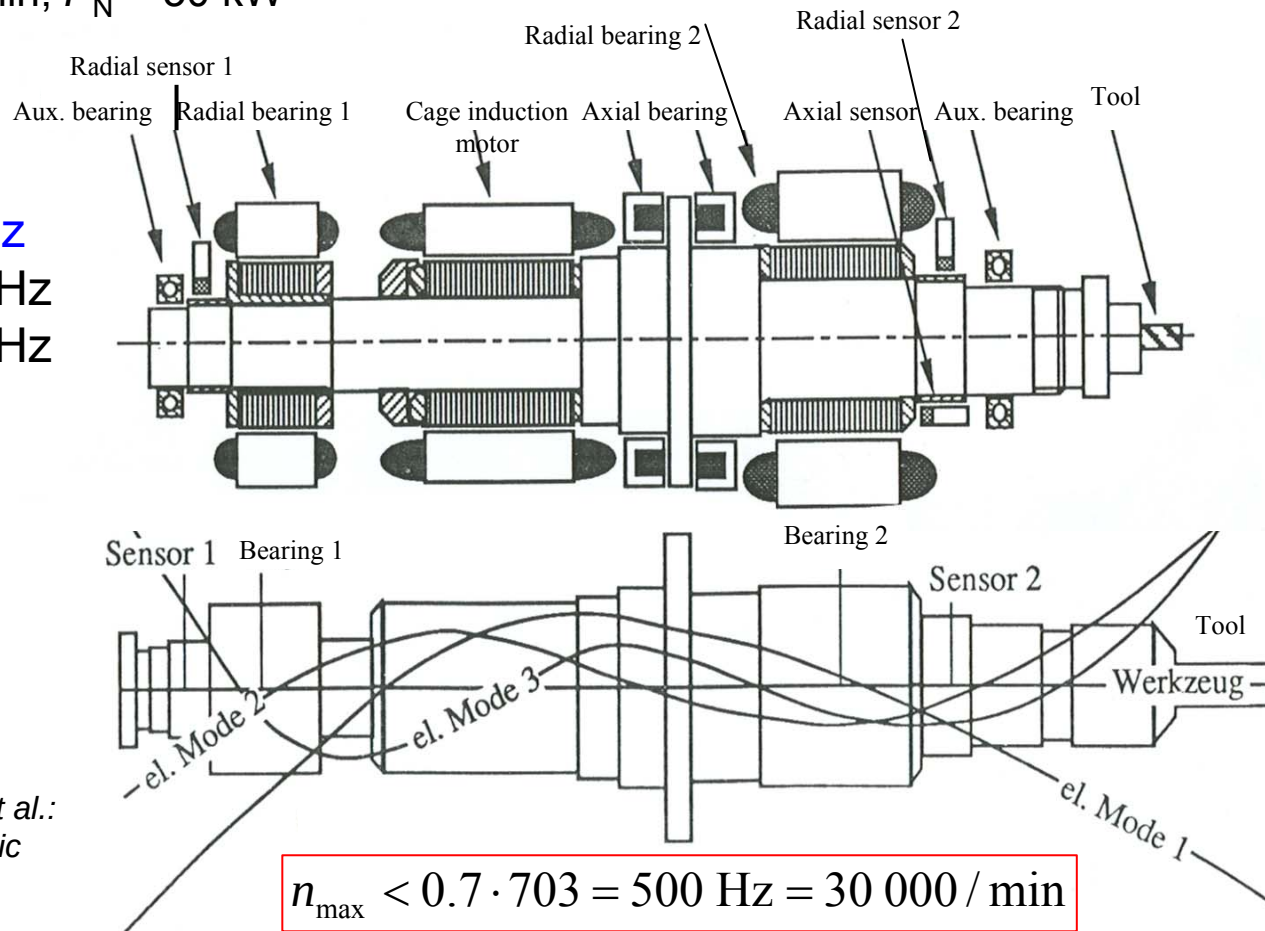
- a) Real frequencies are lower!
- b) Exciting  $n$  below  $0.7 \cdot f_{b,1}$ :  
Rotor “behaves” rigid!

## Example: Natural bending vibration modes of a milling spindle rotor

**2-pole “High-Speed” Aluminum-squirrel cage rotor:** 2 radial & 1 axial magnetic bearing

$n_N = 35\,000 \text{ /min}$ ,  $P_N = 30 \text{ kW}$

$k = 1: 703 \text{ Hz}$   
 $k = 2: 1758 \text{ Hz}$   
 $k = 3: 2990 \text{ Hz}$



Source:

Schweitzer, G. et al.:  
Active magnetic  
bearings

# Influence on rotor bending frequencies

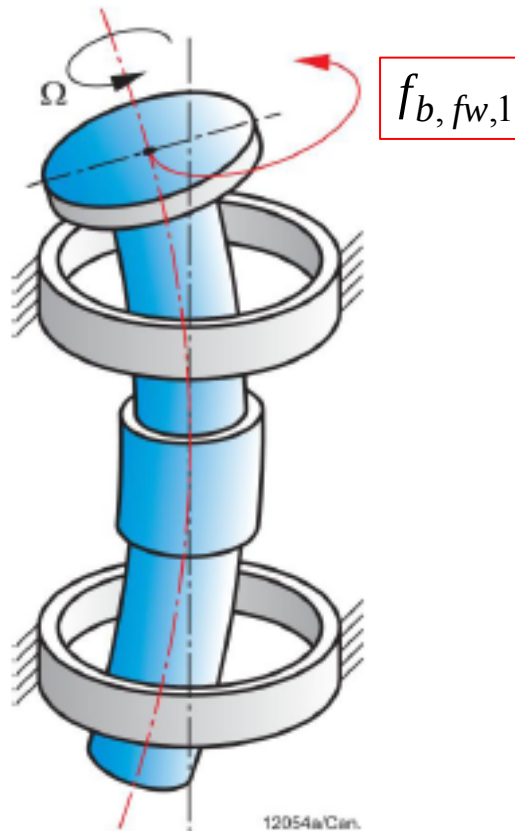
- Bigger (longer) rotors have lower bending frequencies  $f_b \sim d / L^2$
- Real rotor geometry  $\Rightarrow$  more complicated  $f_b$ -calculation
- Equivalent Young's modulus of stacked rotor iron:  
How to determine?  $\Rightarrow$  Mainly be experiment!
- Finite stiffness of rotor bearings  $c_{B0}$ 
  - a) reduces bending frequencies and
  - b) shifts nodes of bending modes
- Unbalanced magnetic pull reduces  $c_B < c_{B0} \Rightarrow$  Reduction of bending frequency
- Rotor gyroscopic effect  $\Rightarrow$  Rotor "swirls" in
  - a) forward swirling mode (fw)
  - b) backward swirling mode (bw)

$\Rightarrow$  Bending frequency splits up into two "eigen-frequencies" per bending mode  $i$

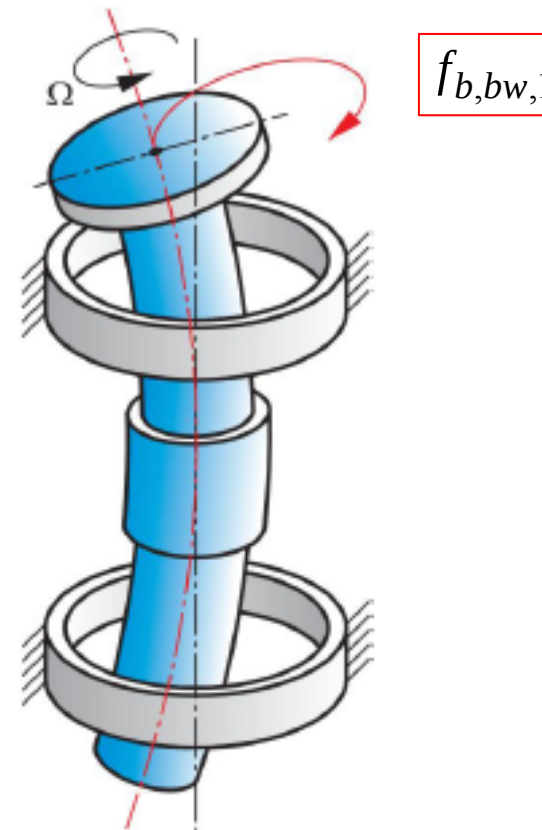
$$f_{b,i} \Rightarrow f_{b, fw,i} \quad \text{and} \quad f_{b, bw,i}$$

# Forward and backward swirling

Forward



Backward



Source: Canders, W.-R.: TU Braunschweig, 2014

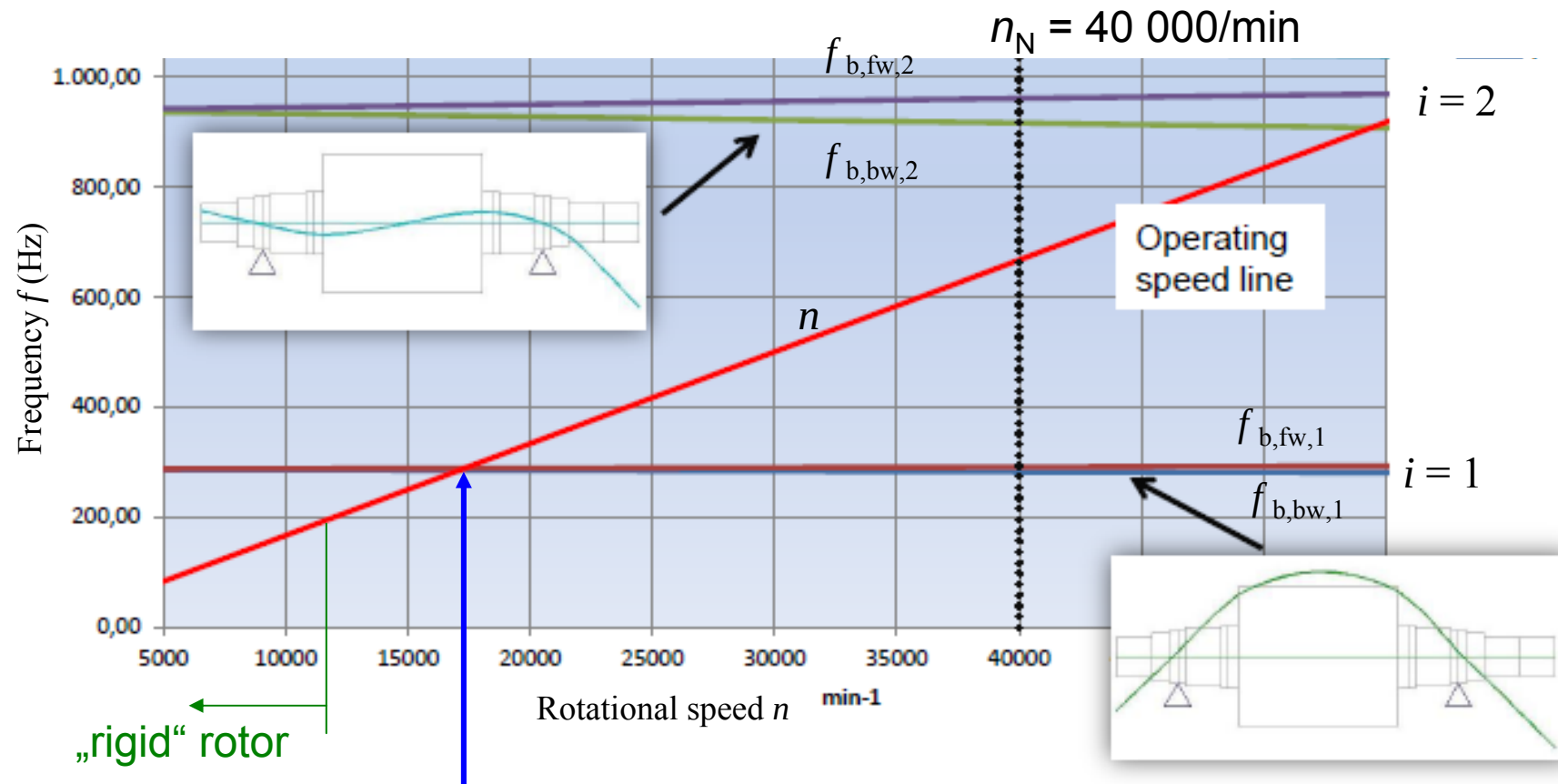
## Example: Campbell diagram

PMSM, laminated rotor yoke, surface magnets, carbon fibre bandage:

$P_N = 60 \text{ kW}$ ,  $d = 86 \text{ mm}$ ,  $v = 180 \text{ m/s}$ ,  $l_{Fe} = 90 \text{ mm}$



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Bending resonance at 17000/min = 1<sup>st</sup> critical speed

Source: Canders, W.-R.: TU Braunschweig, 2014





# Elastic rotor balancing

- If rotational speed  $n$  above e.g. second bending frequency  $f_{b,2}$ , an **elastic rotor balancing** in two additional rotor planes is necessary
- Elastic balancing needed to **minimize rotor bending amplitude**  $y_M$  at the resonance points

$$n = f_{b,1} \text{ and } n = f_{b,2}$$

- **At smaller rated power** the rotor length  $L$  is small enough, so that the bending natural frequencies are higher than the maximum operation speed  $n_{\max}$

$$n_{\max} < f_{b,1}$$

- If possible, keep  $n_{\max}$  below  $0.7 \cdot f_{b,1} \Rightarrow$  Rotor “behaves” as rigid body !

## Mechanical limits for rotor volume $V \sim l_{Fe} \cdot d^2$ at “high-speed” and rigid rotor

- Max. surface velocity  $v_{\max}$  at rated speed  $n_N$  determines max. rotor diameter  $d_{\max}$ :

$$d_{\max} = v_{\max} / (n_N \cdot \pi) \sim (\sqrt{\sigma_{\max} / \rho}) / n_N \quad \sigma_{\max} \sim \rho \cdot v_{\max}^2$$

- Rotor diameter-length ratio  $\lambda$  (“slimness”):  $\lambda = l_{Fe} / d$

- 1<sup>st</sup> Rotor bending frequency limits the length:

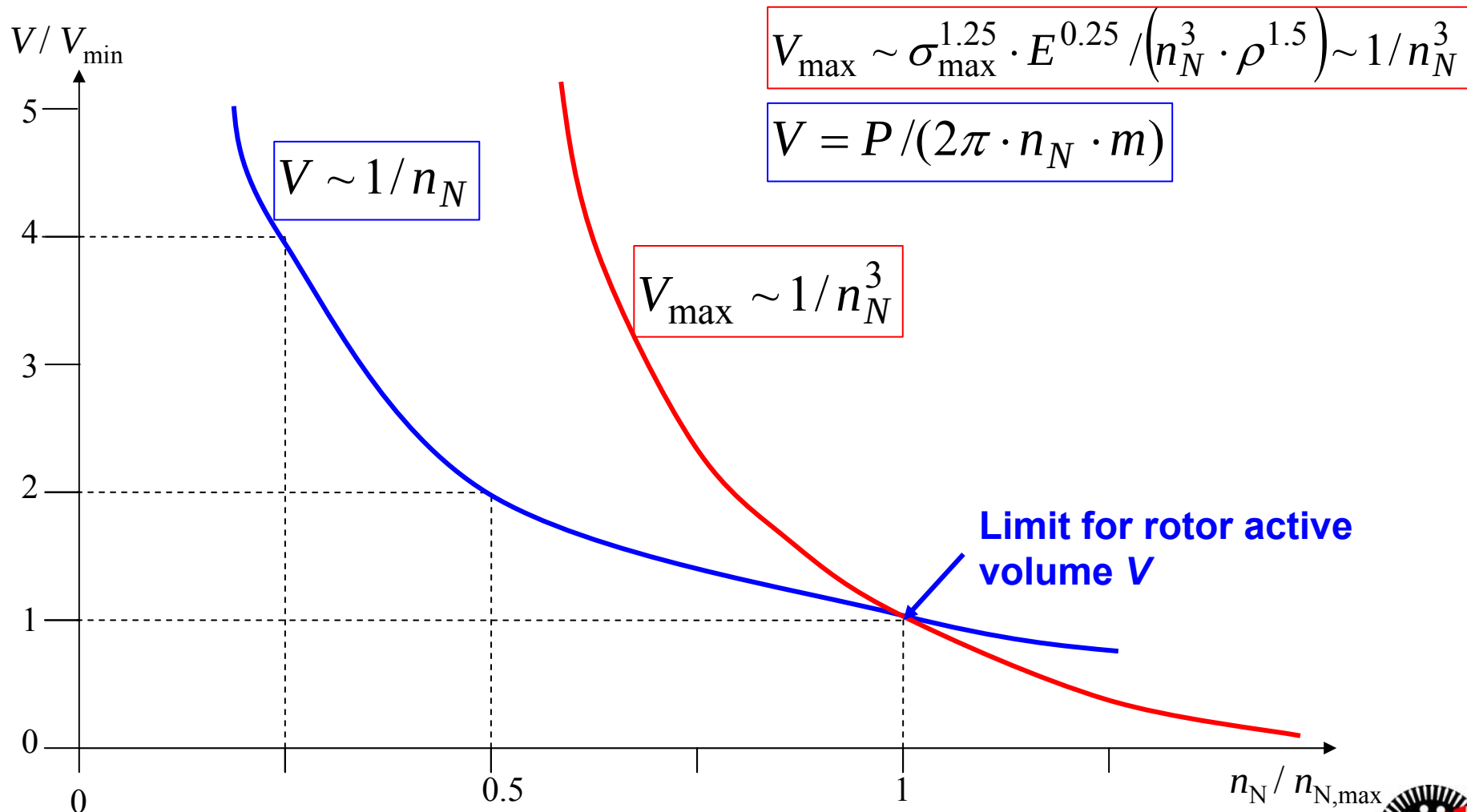
$$f_{b,1} = \frac{n_N}{0.7} \Rightarrow L_{\max} \sim \sqrt{\frac{d_{\max}}{n_N}} \cdot \sqrt[4]{\frac{E}{\rho}} \sim l_{Fe,\max} \Rightarrow \lambda_{\max} = l_{Fe,\max} / d_{\max}$$

- Limit for rotor active volume  $V$ :

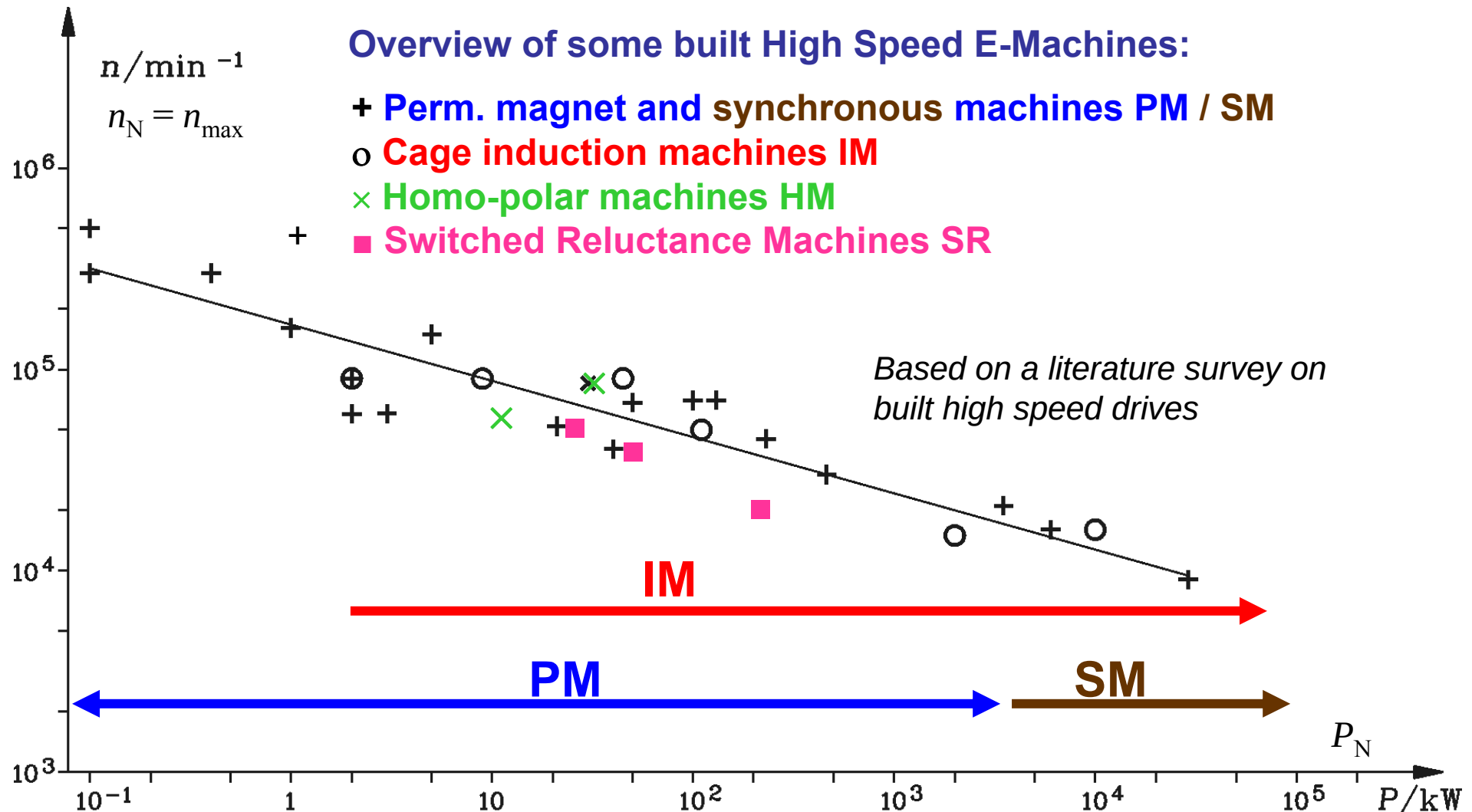
$$V_{\max} \sim d_{\max}^2 \cdot l_{Fe} \sim \sigma_{\max}^{1.25} \cdot E^{0.25} / (n_N^3 \cdot \rho^{1.5})$$

The higher the speed  $n_N$  and mass density  $\rho$ ,  
the lower the maximum admissible rotor volume  $V_{\max}$   
at given maximum stress  $\sigma_{\max}$

# Limits for rotor volume $V \sim l_{\text{Fe}} \cdot d^2$ at “high-speed” and rigid rotor



# Reduced maximum speed $n$ with increased rated power $P_N$



# Elektrische Hochdrehzahlantriebe - Auslegungsgrundlagen & Beispiele aus der Praxis (Electric high-speed drives – design & examples)

## Contents

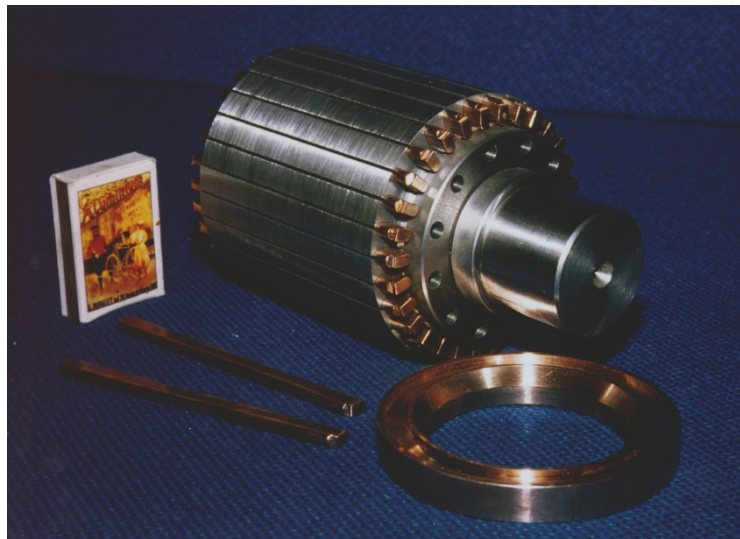
- Basics on High-speed Drives
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# Types of High Speed Motors

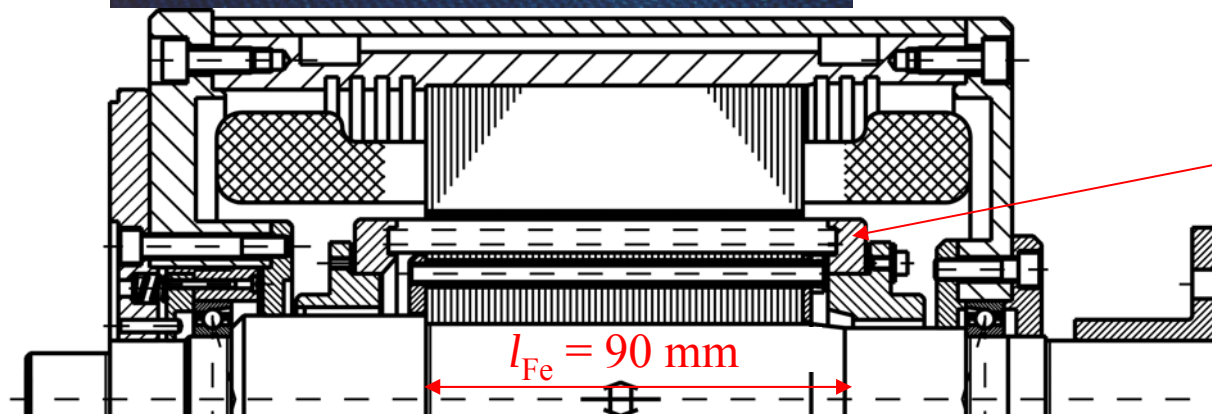
- **PM synchronous machines**  
Rotor magnet fixation essential
- **Electrically excited synchronous machines**  
At higher rated power of interest (MW-range)
- **Cage induction machines (e.g. with massive iron rotor)**  
Cage centrifugal forces needs end caps
- **Cage-less massive rotor induction machines**  
Robust rotor, but slip-dependent losses big in massive iron
- **Homo-polar machines**  
Special machine design, additional losses in massive rotor iron
- **Switched Reluctance Machines**  
Rotor cog-wheel losses, additional iron losses in rotor

# Cage induction machine with laminated rotor

## Example: 4-pole rotor



- Squirrel cage rotor winding
- Retaining caps for end rings
- **Laminated** rotor for low additional losses
- $P_N = 30 \text{ kW}$ ,  $n_N = 24\,000/\text{min}$  (OS: 120%)
- Spindle ball bearings
- Outer rotor diameter  $d = 90 \text{ mm}$ ,  $v = 113 \text{ m/s}$   
OS: 136 m/s

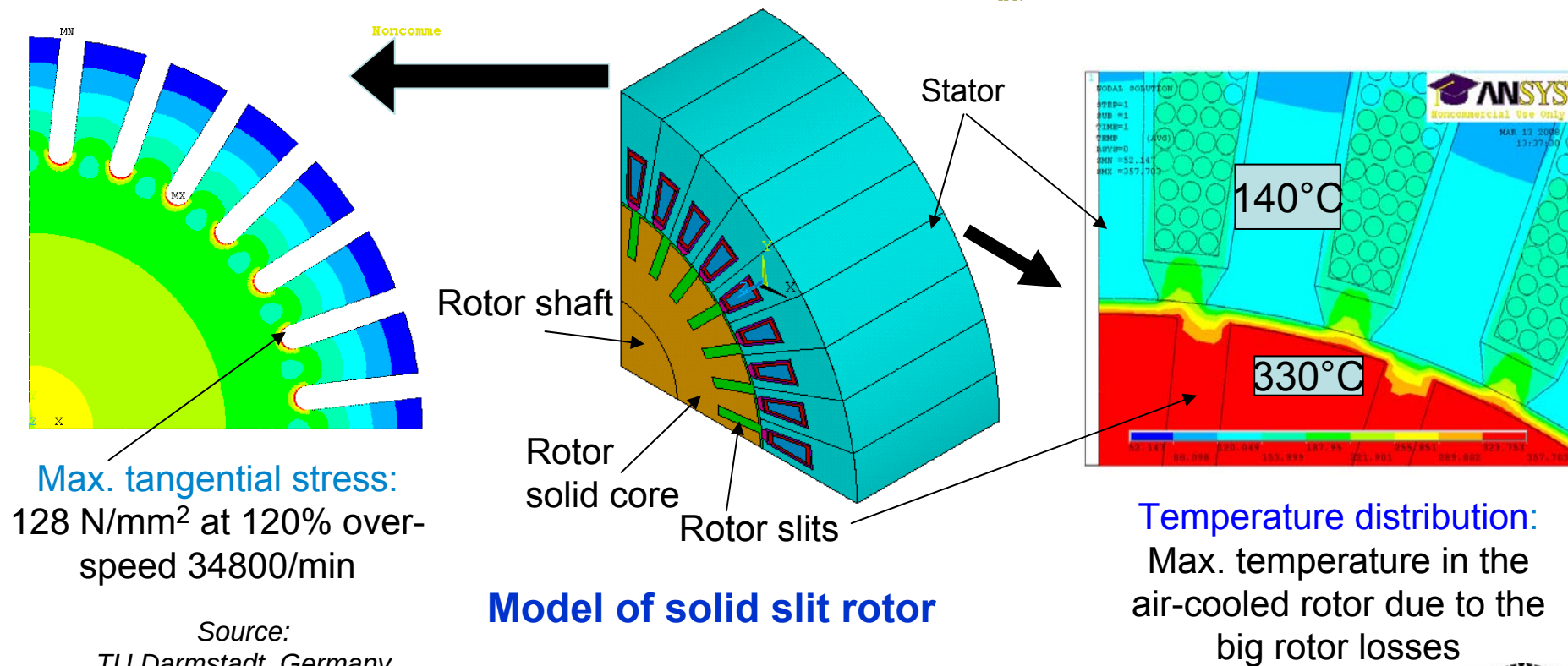


Caps for cage end rings

Source:  
TU Darmstadt, Germany

# Cage-less massive rotor induction machine

**Example:** 2-pole massive slit rotor with copper end rings,  $n_{\max} = 29000/\text{min}$ ,  $d = l_{\text{Fe}} = 90 \text{ mm}$ , low power factor, high rotor slip-dependent losses  $\Rightarrow$  special rotor cooling needed for  $P_N = 24 \text{ kW}$ , spindle bearings

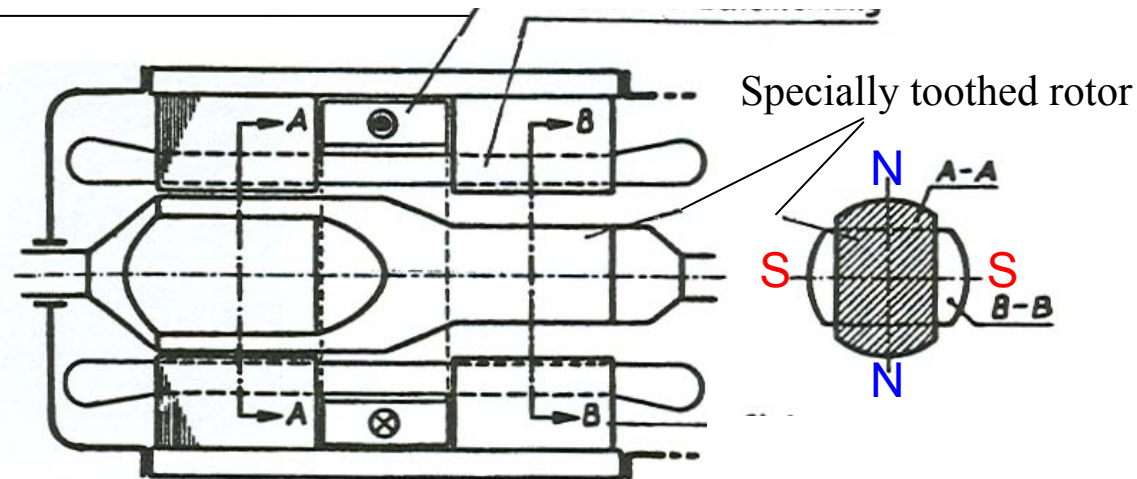




# Homo-polar synchronous machine (ARCO)

**Example:** Three-phase electrically excited synchronous machine:  
4-pole massive rotor with stator-side DC excitation

Central ring coil DC excitation 3-phase AC winding

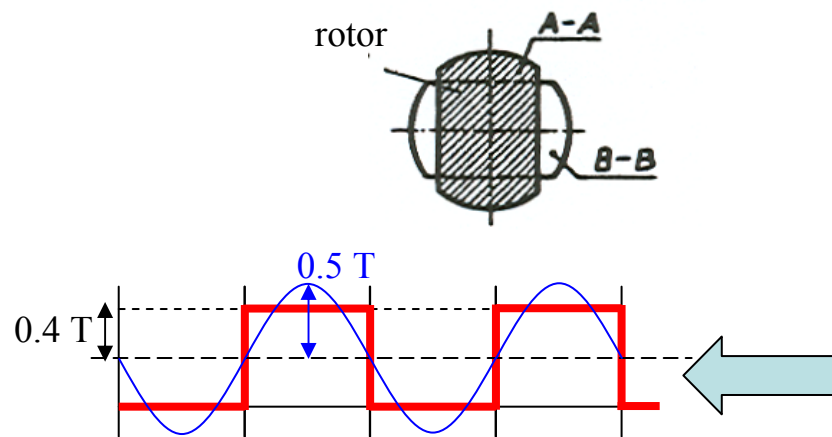


Two-halves stator

- No winding or magnet in the rotor
- Variable DC excitation or PM axial excitation
- No slip rings
- Massive rotor: additional surface eddy current losses due to stator slotting
- Low iron saturation needed!

Source: H. Kleinrath, *Stromrichtergespeiste Drehfeldmaschinen*, Springer, Wien, 1980

# Homo-polar synchronous machine (ARCO)

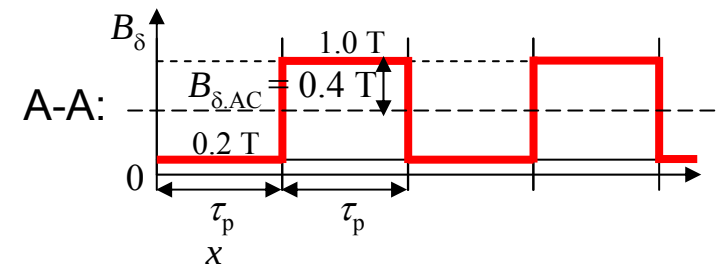


The **fundamental wave** of the AC air gap field component  $B_{\delta,AC}$  induces the stator 3-phase winding with the back EMF  $U_p(I_f)$  like in conventional synchronous machines

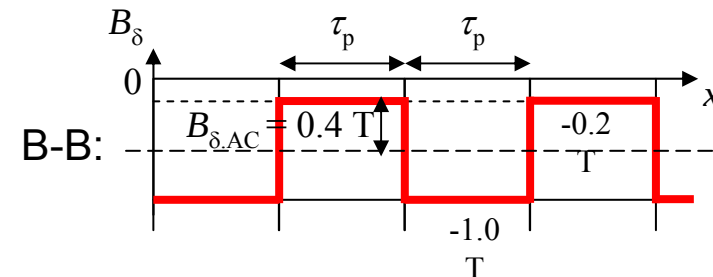
Source: H. Kleinrath,  
Stromrichtergespeiste  
Drehfeldmaschinen, Springer, Wien,  
1980

Radial air gap flux density  $B_\delta(I_f)$  at no-load ( $I_s = 0$ ):

a) Rotor half A-A: Homo-polar positive field



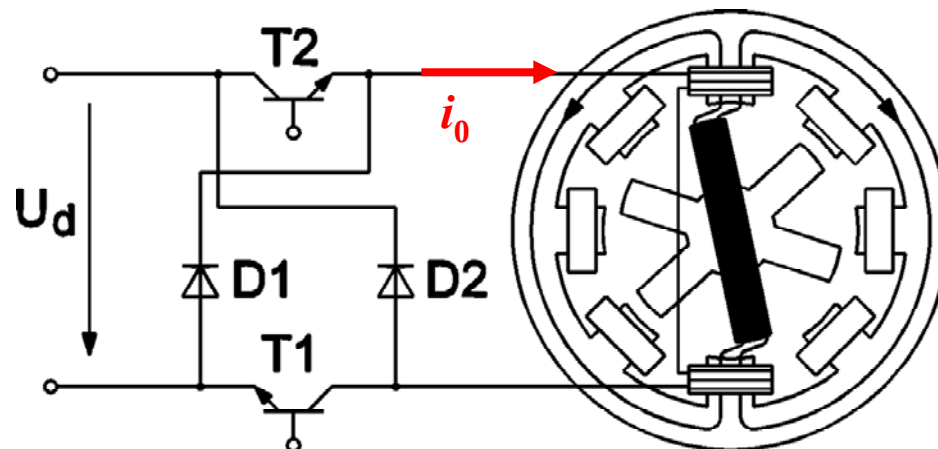
b) Rotor half B-B: Homo-polar negative field



The modulation of the air-gap field  $B_\delta$  by the rotor reluctance yields an AC air gap field component  $B_{\delta,AC}$ , which for both motor halves A-A, B-B is **IN PHASE**

# Switched Reluctance Machines

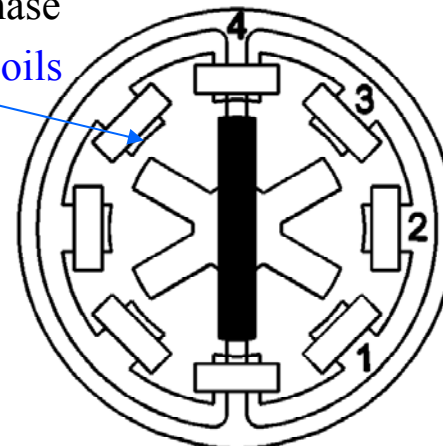
**Example:** 2-pole laminated rotor with 4-phase stator AC excitation,  $Q_r = 6$  rotor teeth



Half-H-Bridge inverter per phase

Stator tooth coils

- Inter-tooth rotor gaps should be filled to reduce windage losses
- Rather high stator frequency  $f_s = n \cdot Q_r$  needed
- Rotor iron losses



Stepwise uni-polar current feeding:

Phase 4



Phase 1



Phase 2



Phase 3



Source: E. Hopper, MACCON, Germany



# Stator frequency and pole count

## El. excited synchronous & induction machines:

Low pole count  $2p \Rightarrow$  low electrical frequency  $f_s \Rightarrow$   
 $\Rightarrow$  low iron losses & low inverter frequency:  $2p = 2$  poles

e.g.  $n_{\max} = 40\,000$  /min,  $2p = 2$  poles,  $f_s = 667$  Hz

## PM synchronous machines:

Pole count 2 or better 4 poles  $\Leftrightarrow$

Limit by rotor PM demagnetization due to stator field

e.g.  $n_{\max} = 40\,000$  /min,  $2p = 4$  poles,  $f_s = 1.33$  kHz

## Switched reluctance machines:

Rotor tooth count  $Q_r$ :

SRM behaves like a synchronous machine with  $2Q_r$  poles

e.g.  $n_{\max} = 40\,000$  /min,  $Q_r = 4$ ,  $f_s = 2.66$  kHz

$$f_s = n \cdot p$$

$$f_s = n \cdot Q_r$$

# Elektrische Hochdrehzahlantriebe - Auslegungsgrundlagen & Beispiele aus der Praxis (Electric high-speed drives – design & examples)



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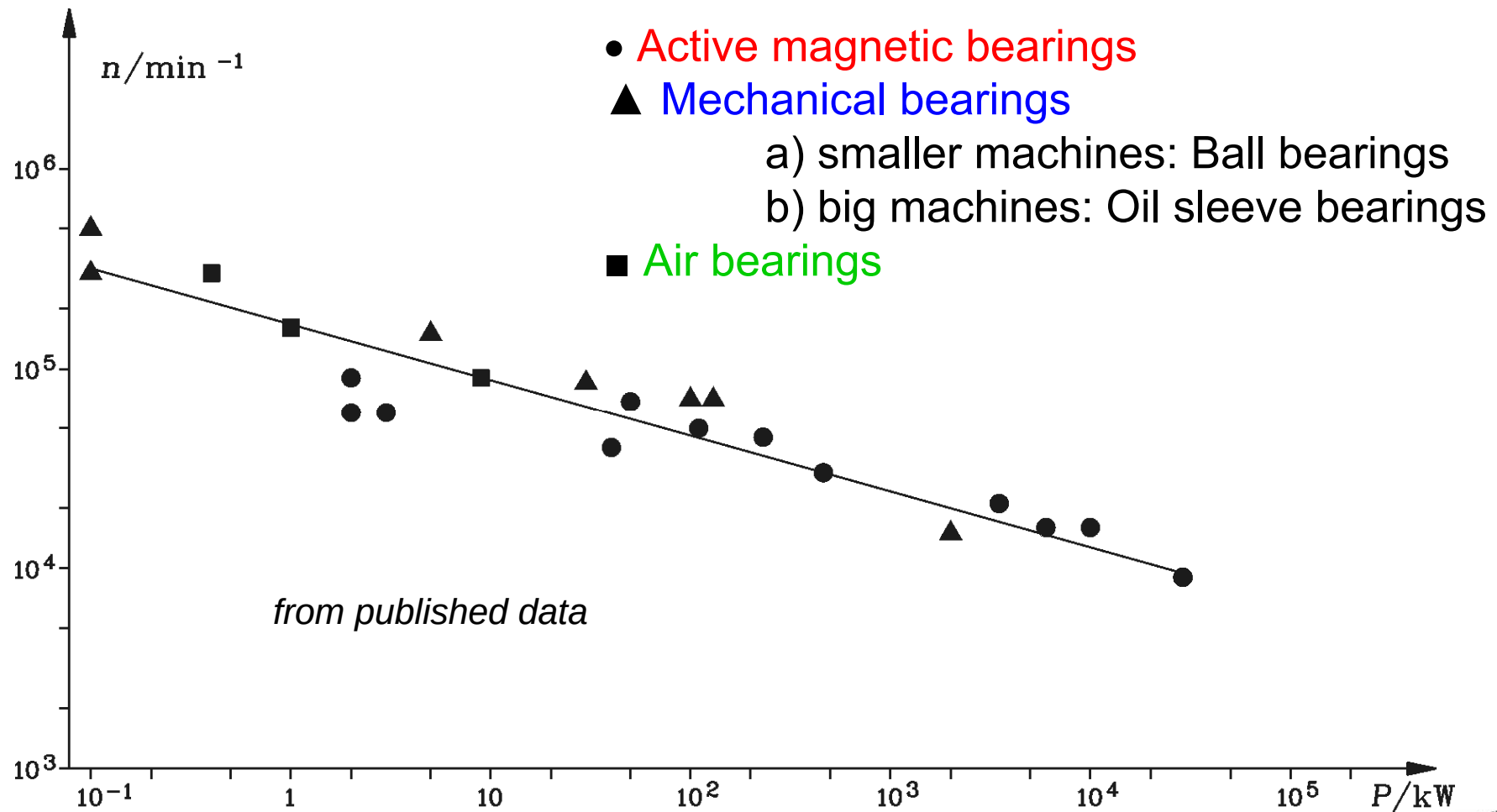
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- Electromagnetic design for High-Speed
- Examples for High-Speed drives
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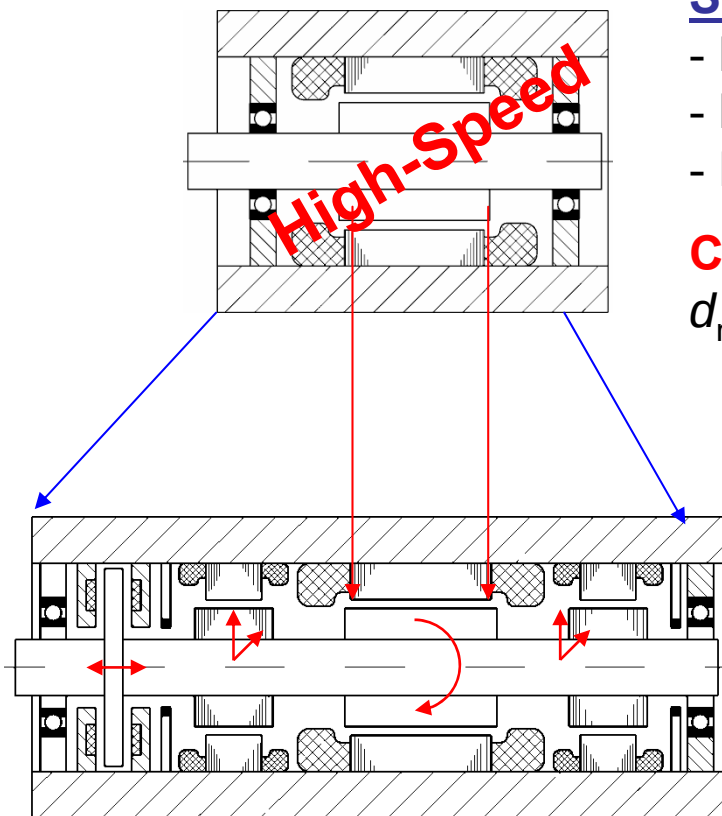
# Different bearing types (Selection)

- Oil-lubricated high-speed **ball bearings** (spindle bearings):  
Highest stiffness, but mechanical speed limit
- Oil-lubricated **sleeve bearings**, at high rotor mass:  
Coupling of vertical and horizontal vibration movement  $\Rightarrow$   
 $\Rightarrow$  Upper speed limit due to bearing instability
- **Air cushion** sleeve bearings, at low rotor mass:  
Reduced stiffness, bearing instabilities
- **Magnetic bearings (MB)**: No mechanical friction and wear  
Controlled MB: Lower dynamic stiffness due to controller delay  
Self-stable MB: Limited magnetic forces  $\Rightarrow$  Low static stiffness

# Bearings for high speed operation



# Ball bearings vs. active magnetic bearings



Usually **longer machine** with AMB

## Spindle ball bearings:

- More, but small balls = low centrifugal force per ball
- Minimum oil lubrication = minimum friction
- Hybrid bearings = Ceramic balls = higher stiffness

**Circumference velocity**  $v_B \sim d_m \cdot n : (1 \dots 2) \cdot 10^6 \text{ mm/min}$   
 $d_m$ : Average bearing diameter       $n$ : Rot. speed

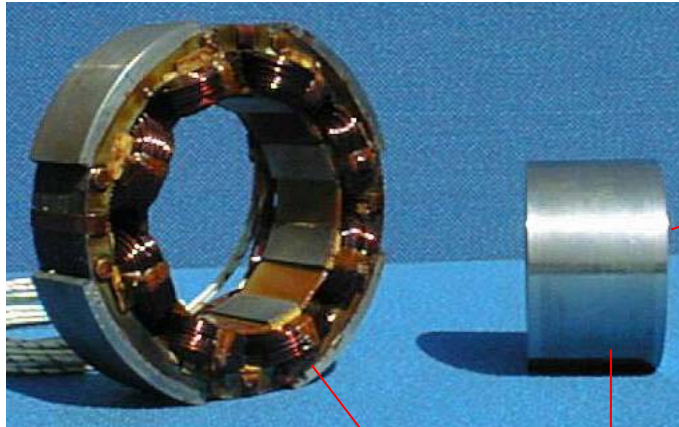
## Active magnetic bearings (AMB):

**Plus:** + No contact  
+ No lubricant  
+ No maintenance  
+ Same high speed  $v$  as motor

**Need:** - DC-Chopper & DC-Control,  
- Position sensors & auxiliary bearings  
- Bearing actuators



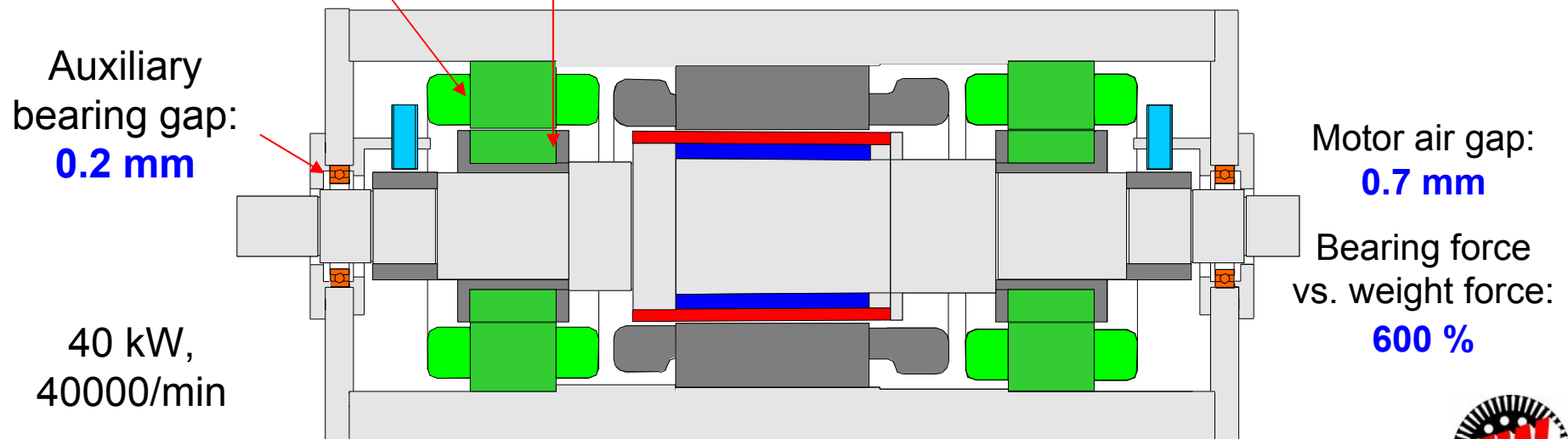
# Active radial magnetic bearings for High-Speed



Radial magnetic bearing: gap **0.4 mm**



Two radial magnetic bearings, PM rotor



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# Loss components in High Speed E-Machines

## Dominating loss components in “high-speed” motors:

- Iron losses  $P_{Fe}$  = Eddy current & hysteresis losses in iron sheets
- Air friction losses  $P_{fr}$
- Additional losses (= eddy current losses)  $P_{ad}$  in massive, conductive parts

$I^2R$ -losses  $P_{Cu,s}$  are usually less decisive!

- ⇒ **Low loss iron sheets** may reduce iron losses  
e.g.: 2 W/kg losses at 1.5 T, 50 Hz such as HF-sheets (0.1 mm thickness)
- ⇒ **Twisted litz wires** may reduce eddy current losses in slot conductors
- ⇒ **Segmented, insulated rotor magnets** reduce there eddy currents
- ⇒ Slot-less stator windings (= “**air-gap winding**”) approximates sine-wave air-gap field distribution ⇒ reduces rotor eddy current losses
- ⇒ Stator AC currents should have **minimum ripple** due to inverter switching

# Loss components in PM Synchronous High Speed E-Machines

## No-load losses:

a) **Stator iron losses:**  $P_{Fe,s} \sim B_{\delta}^2 \cdot f_s^x \sim B_{\delta}^2 \cdot n^x$

$x = \text{ca. } 1.8$ , considering eddy-current and hysteresis losses

b) **Friction losses** at the rotor surface:  $P_{fr,w} \sim \rho_{air} \cdot d^4 \cdot l_{Fe} \cdot n^3$

Depending on rotor and stator surface condition & bearings:  $y = 2 \dots 3$

$$P_{fr,b} \sim d_m \cdot n^y$$

## Load losses:

c) **Armature winding losses** ( $I^2R$ - losses):  $P_{Cu,s} = 3 \cdot R_s \cdot I_s^2$

d) **Additional losses**  $P_{M+Fe,r} = f(n, \text{ current shape}) \sim I_s^2 \cdot n^z$

- In stator winding:  $P_{ad,s}$  due to eddy currents of high frequency current

- In rotor magnets and rotor iron  $P_{M+Fe,r}$ ,  $z = \text{ca. } 1.5 \dots 2$ ,  
depending on rotor geometry and stator current wave shape

$B_{\delta}$ : Air-gap flux density amplitude,  $I_s$ : Stator phase current rms,

$f_s$ : Stator frequency,  $R_s$ : Stator ohmic winding resistance per phase

# Inverter Operation for High Speed

- Voltage:  $U_i \sim n \cdot N_s \cdot k_w \cdot d \cdot l_{Fe} \cdot B_\delta$   **high  $n \Rightarrow$  low  $N_s \sim 1/n$**

$N_s$ : Number of turns per phase,  $k_w$  ( $\approx 0.9$ ) fundamental winding factor

- High fundamental frequency:  
e. g.  $n = 200\,000$  /min, two-pole motor:  $f_s = 3.3$  kHz =  $n$   
high switching frequency  $f_T \approx 5f_s$  (e.g. 16.5 kHz)
- Motor stator inductance  $L_d$  per phase rather small:  $L_d \sim \mu_0 \cdot N_s^2 \cdot l_{Fe}$
- Current ripple amplitude  $I_T$  **rather big**:  $I_T \sim U_T / (f_T \cdot L_d) \sim f_s$   
( $U_T$ : Switching voltage harmonic amplitude)

**Need:** Low current harmonics  $I_T$  to reduce additional losses

**Solutions:**

- a) Very high switching frequency  $f_T$
- b) 3-level-inverter
- c) (Active) output sine wave filter

# Torque density $m$ at “High-Speed”

- Increased iron, friction and additional losses at high speed  $P_{\text{Fe+fr+ad}}$  !
- $P_{\text{Fe+fr+ad}}$  must be limited  $\Rightarrow$  Reduction of  $A$  and  $B$  necessary
- Reduction of  $A$  and  $B$  leads to certain reduction of  $m$ :  $m \downarrow \Leftrightarrow n_N \uparrow$

$$P/V = 2\pi \cdot n_N \cdot M_N / V = 2\pi \cdot n_N \cdot m$$

## Note:

If torque density  $m$  decreases inverse with raising rated speed  $n_N$ :  $m \sim 1/n_N$   
then high speed drives would have **no benefit**  
from increased power per volume  $P/V$  at elevated speed!

## BUT:

With special “high speed technology”  $B_\delta$  and  $A$  may be kept  
at reasonable high values!

# Design features of High Speed E-Machines

- Necessary at high speed:

⇒ **Low loss iron sheets**: (e.g. 0.1 mm HF sheets):

Reduction of  $B_{\delta}^2$  less than  $1/n$  !

$$B_{\delta}(n) > 1/\sqrt{n}$$

⇒ **Special stator windings** for low additional losses (e.g. twisted litz wire):

Reduction of  $A^2 \sim I_s^2$  less than  $1/n$  !

$$A(n) > 1/\sqrt{n}$$

- Increased power density  $P/V \Rightarrow$  Less volume  $V \Rightarrow$   
Increased loss density  $P_d/V \Rightarrow$  **Improved cooling system** necessary !

e.g. **Stator water jacket cooling**:

Increased heat transfer coefficient  $\alpha \Rightarrow$  temperature rise  $\Delta\vartheta$  kept within limits!

$$\Delta\vartheta_{\text{Cu,s}} \sim P_d / \alpha \Rightarrow \Delta\vartheta_{\text{Cu,s}} \leq \Delta\vartheta_{\text{lim}}$$

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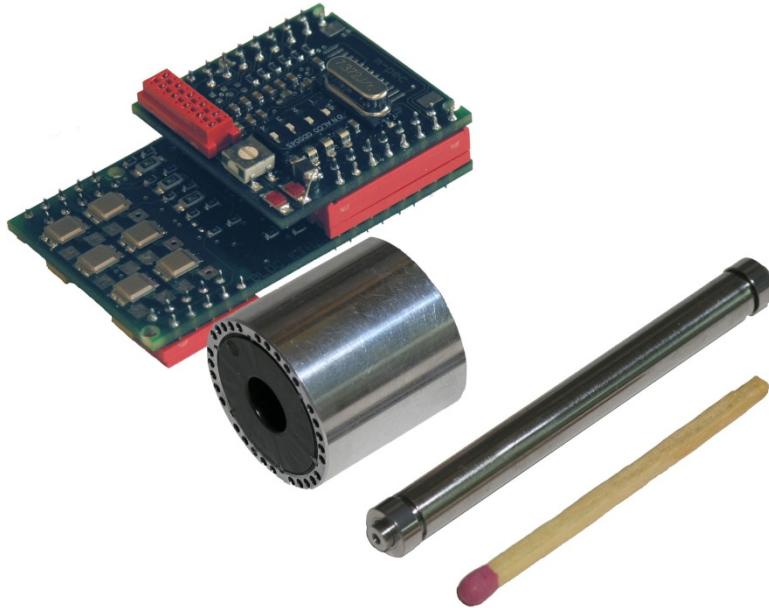
# Examples for High-Speed drives

## Permanent-magnet synchronous machines

- a) with different rotor magnet fixation,
- b) different power & speed rating,
- c) different cooling system and motor utilization,
- d) different bearing systems,
- e) different stator winding technology

# High-Speed PM Synchronous Machine

“Ultra high-speed” motor for a meso-scale gas turbine



100 W, 500 000/min

|                |          |         |
|----------------|----------|---------|
| Torque         | $M_N$    | 2 mNm   |
| Phase voltage  | $U_N$    | 11 V    |
| Current        | $I_N$    | 3 A     |
| Frequency      | $f_N$    | 8.3 kHz |
| Rotor diameter | $d$      | 6 mm    |
| Stack length   | $l_{Fe}$ | 15 mm   |

$$P = 2\pi \cdot n \cdot M_N =$$

$$= 2\pi \cdot \frac{5 \cdot 10^5}{60} \cdot 2 \cdot 10^{-3} = 100 \text{ W}$$

$$m = \frac{M_N}{d^2 \cdot l_{Fe} \cdot \pi / 4} = 0.5 \text{ N/cm}^2$$

Source: ETH Zurich, Switzerland

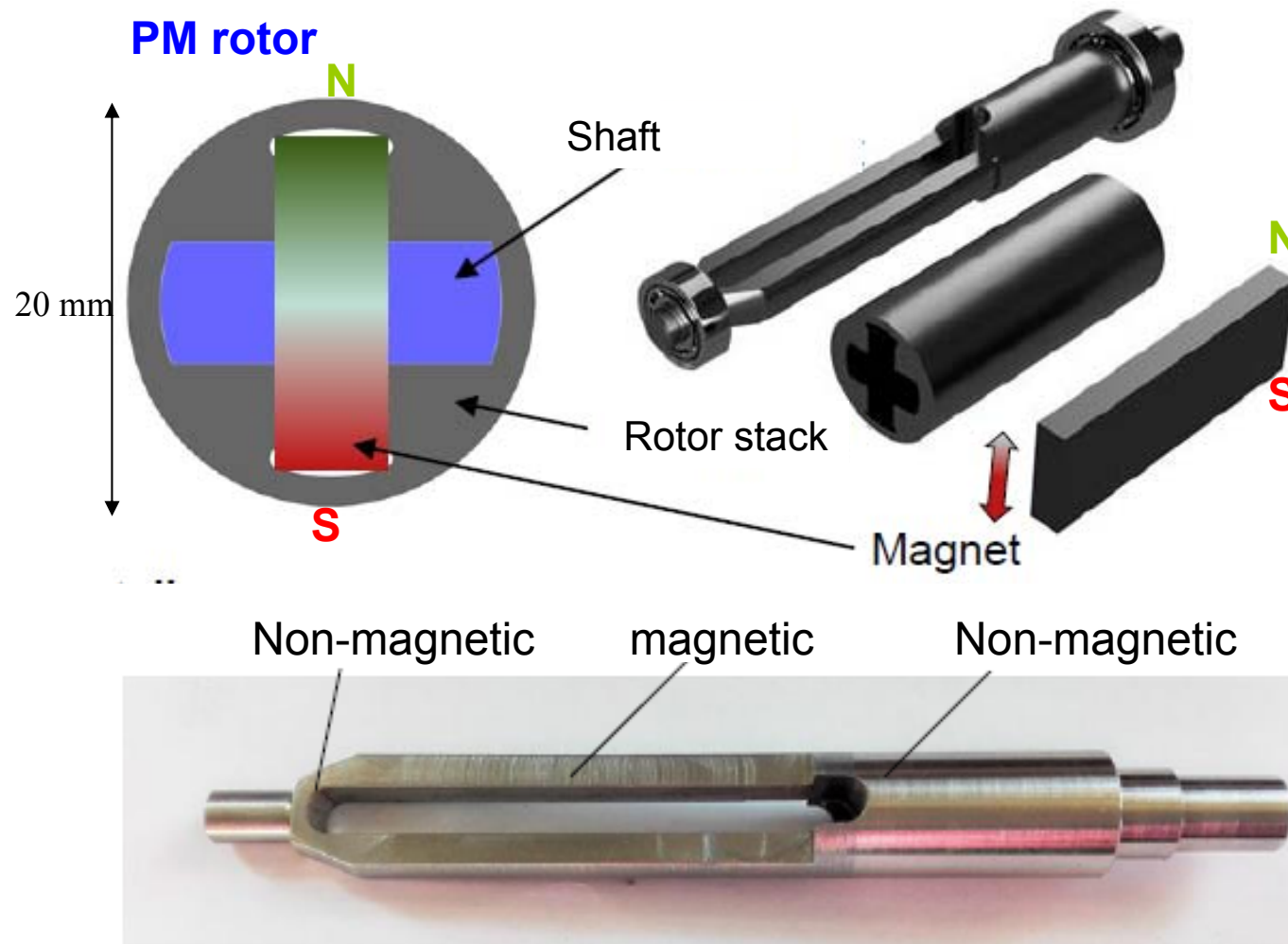
- Two-pole PM motor, six-step voltage feeding
- Titanium rotor sleeve
- Circumference speed: 157 m/s
- Mechanical bearings  $n \cdot d_m \cong 2 \cdot 10^6 \text{ mm/min}$

# High-Speed PM Synchronous Machine

## Two-pole PM synchronous motor with buried magnets (1)



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



$$f_s = 2083 \text{ Hz}$$

$$n = 125\,000/\text{min}$$

Source: Schiefer, M.:  
Antriebssysteme 2017,  
VDE/Karlsruhe, Germany



# High-Speed PM Synchronous Machine

## Two-pole PM synchronous motor with buried magnets (2)



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

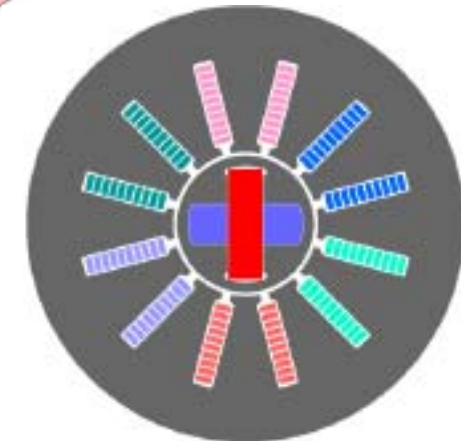
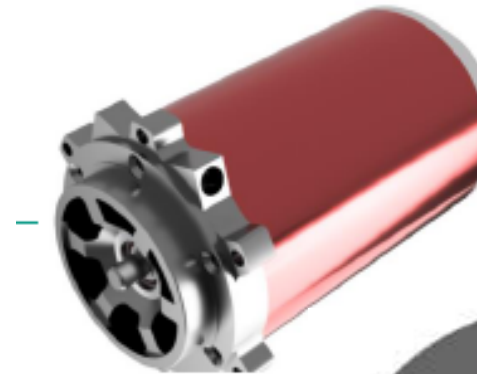
High slot fill factor 65%

Water jacket cooling 50°C

High current loading → high  $m$ -value

$A = 688 \text{ A/cm}$

|                                 |                          |
|---------------------------------|--------------------------|
| Rated power $P_N$ (Th. Cl. F)   | 15.7 kW                  |
| Rated phase current $I_{s,N}$   | 45 A                     |
| Rated DC link voltage $U_{d,N}$ | 600 V                    |
| Speed                           | 125 000/min              |
| Rotor diameter                  | $d = 20 \text{ mm}$      |
| Active iron length              | $l_{Fe} = 50 \text{ mm}$ |
| Rotor mass                      | Ca. 2 kg                 |
| Max. efficiency                 | 95%                      |



$$v = d \cdot \pi \cdot n = 130 \text{ m/s}$$

$$A = \frac{2 \cdot 3 \cdot N_s \cdot I_s}{d \cdot \pi} = \frac{6 \cdot 16 \cdot 45}{2 \cdot \pi} = 688 \frac{\text{A}}{\text{cm}}$$

$$m = \frac{M_N}{d^2 \cdot l_{Fe} \cdot \pi / 4} = 7.6 \text{ N/cm}^2$$

Source: Schiefer, M.: Antriebssysteme 2017,  
VDE/Karlsruhe, Germany



# High-Speed PM Synchronous Machine

## 4-pole PM synchronous machine with carbon fibre bandage

Surface magnets ( $\text{Sm}_2\text{Co}_{17}$ ), 16 magnet segments / pole,  
carbon fiber bandage, radial magnetic bearings

$$P_N = 40 \text{ kW}$$

$$n_N = 40\,000 \text{ min}^{-1}$$

$$d = 88.6 \text{ mm rotor diameter, } l_{\text{Fe}} = 90 \text{ mm}$$

$$v_{\text{max}} = 222 \text{ m/s rotor surface velocity at 120\% over-speed}$$

$$m = \frac{M_N}{d^2 \cdot l_{\text{Fe}} \cdot \pi / 4} = 1.8 \text{ N/cm}^2$$

stator with water  
jacket cooling



Source: TU Darmstadt

Magnetic bearing  
stator

Magnetic bearing  
Rotor " $d_m$ "

$$"d_m" \approx 60 \text{ mm} :$$

$$n \cdot d_m = 2.4 \cdot 10^6 \text{ mm/min}$$

Radial distance sensors (eddy current principle)

Rotor with  
CFC-bandage



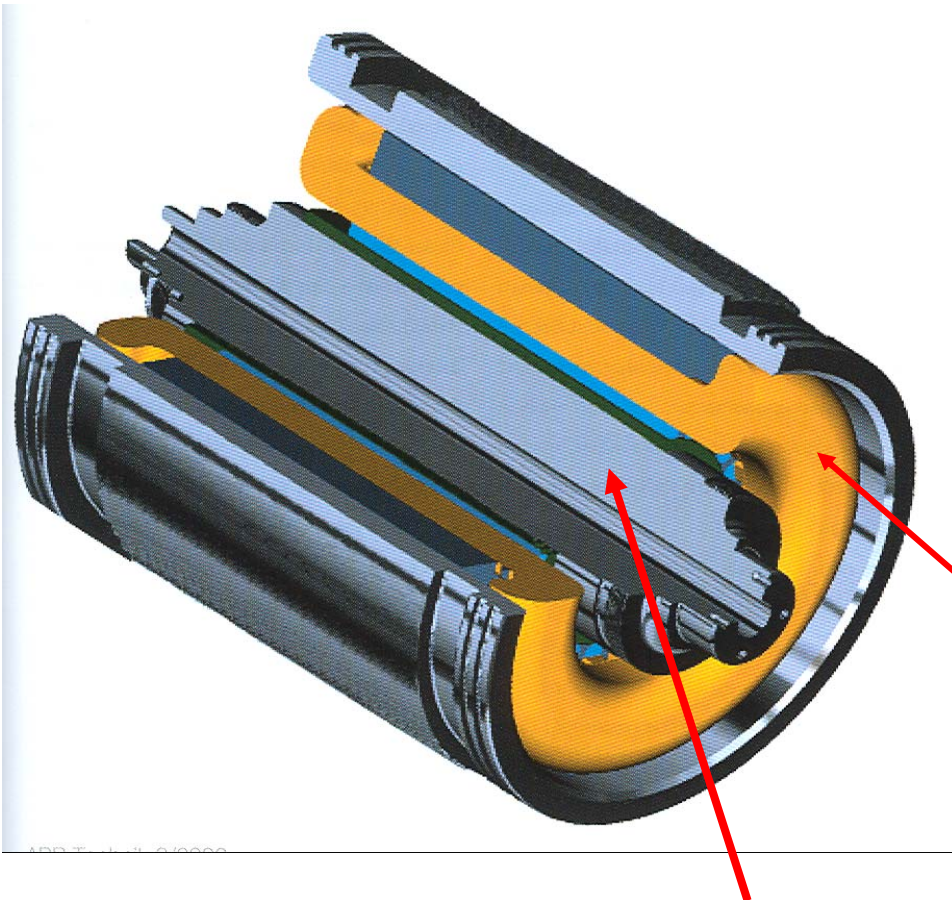
# High-Speed PM Synchronous Machine

## PM 4-pole synchronous generator for micro gas turbine



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

70 000/min, 2300 Hz, four pole PM-machine



Massive rotor iron, special air bearings

Four pole PM-rotor, Carbon fiber bandage



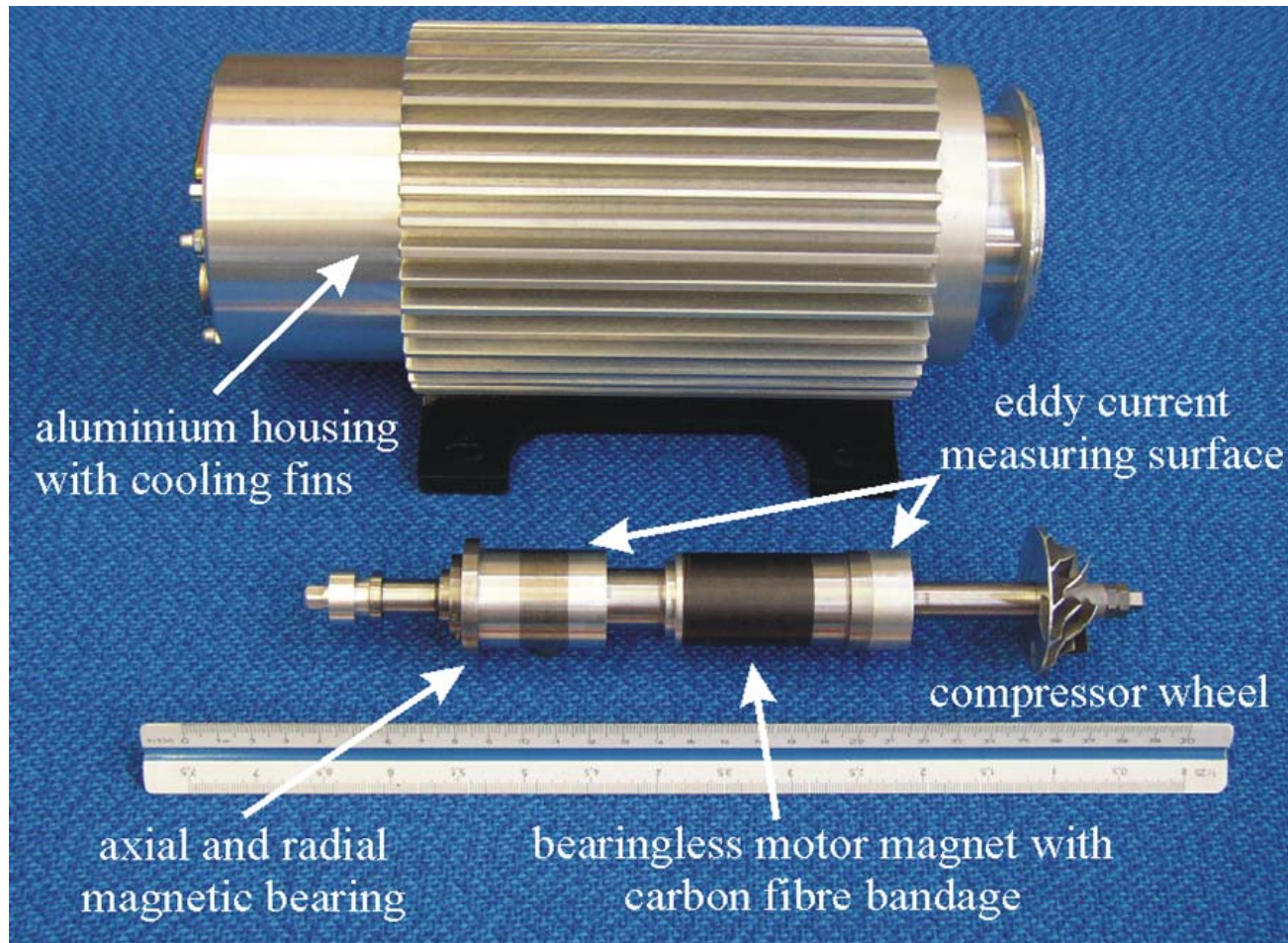
Stator with four pole three phase winding, fully encapsulated in resin for good heat transfer to iron

Source: ABB, Sweden



# High-Speed PM Synchronous Machine

Bearing-less high-speed PM motor 500 W, 60 000/min



$$n_N = 60\,000/\text{min}$$

$$P_N = 500\text{ W}$$

Two-pole motor:  
 $2p = 2$

$$f_s = 1000\text{ Hz}$$

$$v = 100\text{ m/s}$$

4-pole levitation  
winding

Air self-cooling

$$m = \frac{M_N}{d^2 \cdot l_{Fe} \cdot \pi / 4} = 0.33\text{ N/cm}^2$$

Source: TU Darmstadt,

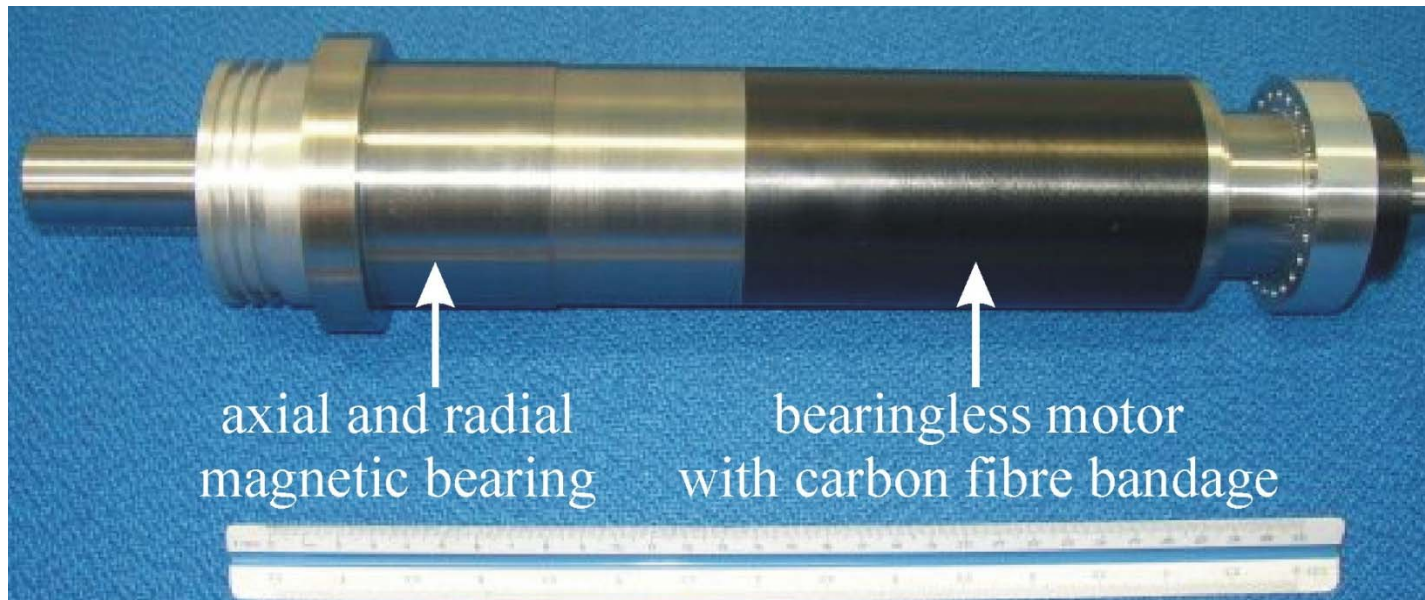
In co-operation with  
LTI, Lahnau, Germany





# High-Speed PM Synchronous Machine

Bearing-less high-speed PM motor 40 kW, 40000/min



$$n_N = 40000/\text{min}$$

$$P_N = 40 \text{ kW}$$

Four-pole:  
 $2p = 4$

$$f_s = 1333 \text{ Hz}$$

$$v = 167 \text{ m/s}$$

$$d = 80 \text{ mm}$$

$$l_{Fe} = 90 \text{ mm}$$

## BEARINGLESS concept:

### Two 3- phase stator windings:

- Four-pole drive winding  $2p_1 = 4$
- Six-pole levitation winding  $2p_2 = 6$

Source: TU Darmstadt,

In co-operation with LTI, Lahnu, Germany

$$m = \frac{M_N}{d^2 \cdot l_{Fe} \cdot \pi / 4} = 2.2 \text{ N/cm}^2$$

- Rotor successfully tested  
at 44000/min (185 m/s)

- Water-jacket cooling





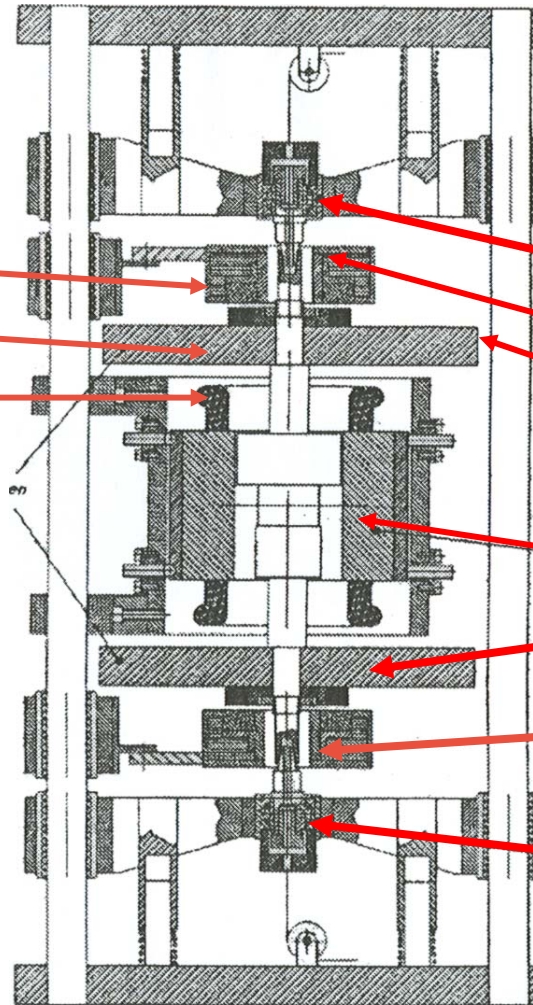
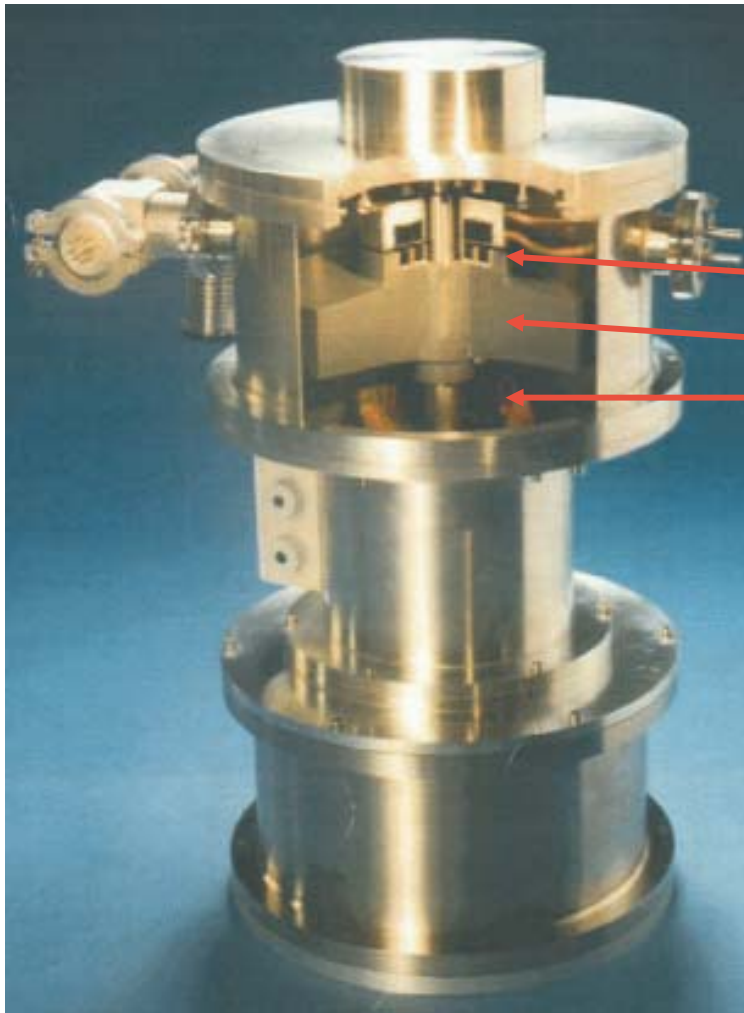
# Examples for High-Speed drives

**Homo-polar synchronous machine**

**Massive rotor cage induction machine**

**Cylindrical rotor synchronous machine**

# Homo-polar generator for flywheel



10 kW, 50 000/min  
Vacuum operation  
0.21 Pa !

Auxiliary bearing

HTSC magnetic bearing

Carbon fibre  
fly-wheel disc

**4-pole homo-polar  
synchronous generator**

Carbon-fibre fly-wheel disc

HTSC magnetic bearing

Auxiliary bearing

Source: FSZ Karlsruhe,  
Germany



# Cage induction machines with massive rotor

## Operation above 2<sup>nd</sup> bending eigen-frequency

Air-water  
cooler



**Example:** 2-pole rotor, 15000/min, 4 MW



- Gas pipe line compressor motor series
- Motor series 4 MW / 15000/min / 2.5 kNm ... 16 MW / 6000 /min / 25.5 kNm
- Copper cage, 2-pole motors, solid iron rotor, **ca. 240 m/s circumferential speed**
- 2 radial Active Magnetic Bearings; axial magnetic bearing at compressor wheel
- Medium voltage IGBT-PWM-voltage source converter

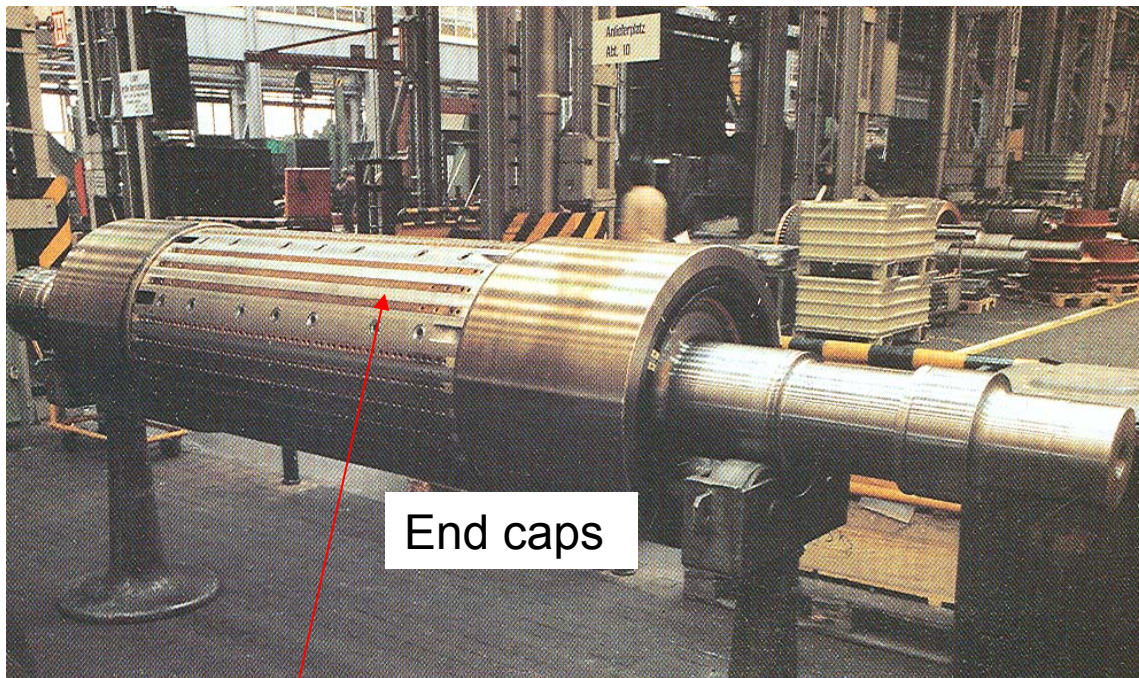
*Source: Siemens AG, Dynamowerk, Berlin, Germany*



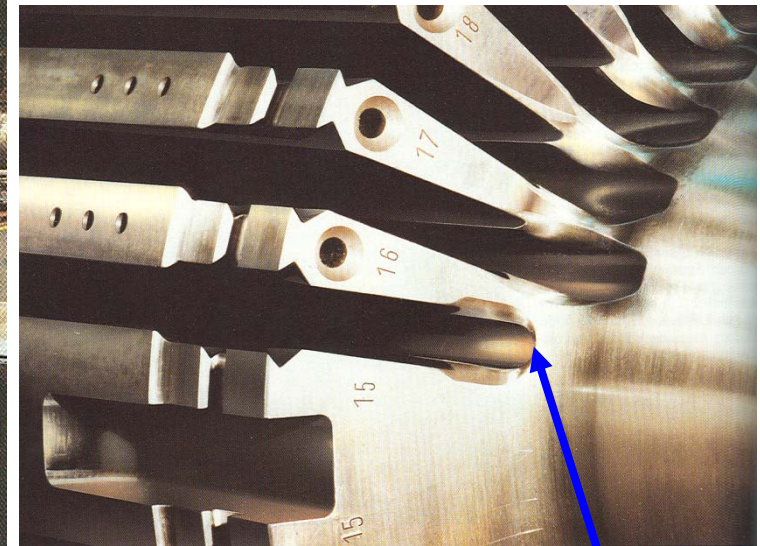
# Two-pole electrically excited high-speed solid steel rotor

## Motor operation at thyristor synchronous converter with block current wave form

17 MW, 6100/min, high speed converter-fed synchronous motor as compressor drive, oil sleeve bearings: Operation between 1<sup>st</sup> and 2<sup>nd</sup> bending frequency



Conducting rotor slot wedges as **damper bars**



Milled rotor slots prior to mounting of rotor DC excitation winding

Source: Siemens AG, Dynamowerk, Berlin, Germany



# Selected Examples of High-Speed Machines

## Largest High-Speed Machines are Two-Pole Turbine Generators

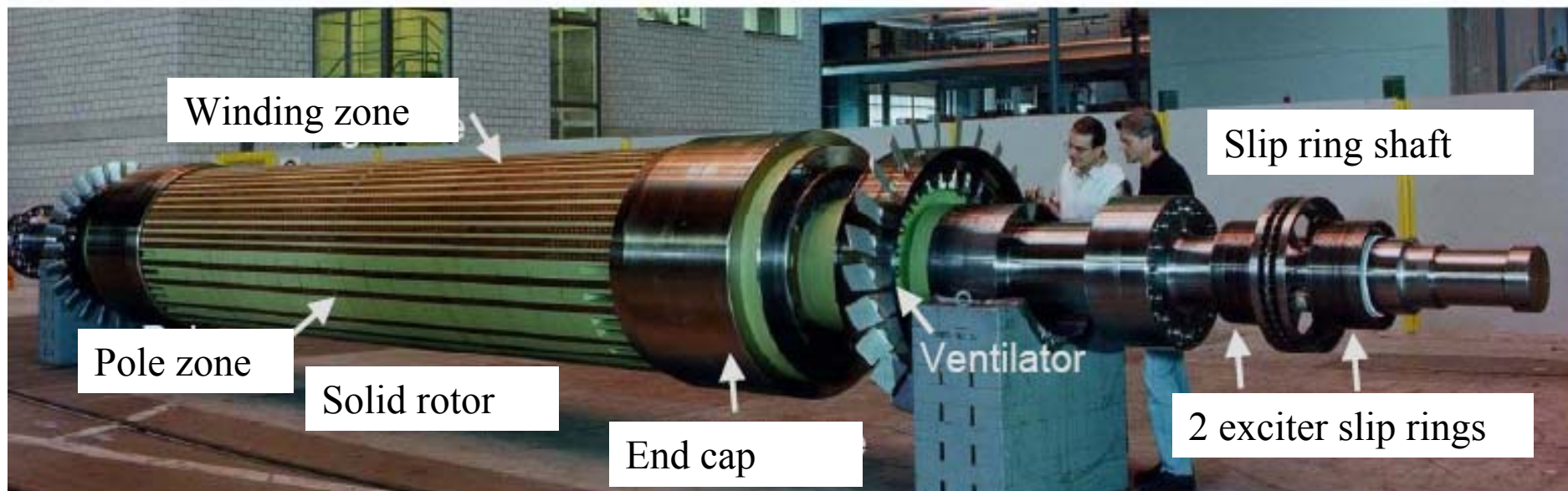


Example:  $f_s = 50$  Hz: Largest possible power: 1 GW at 50 Hz,  $n = 3000/\text{min}$

Rotor diameter:  $d = 1.25$  m:  $v = 188$  m/s = 676 km/h at  $2p = 2$ ,  $l_{Fe} = 8$  m  $m = 32.4$  N/cm<sup>2</sup>

⇒ Bigger rotor diameters **not possible** due to limited strength of steel

⇒ Longer rotors **not possible** due to strong rotor bending: 5 balancing planes



Manufacturing of Hydrogen gas-cooled two-pole Rotor, 1 GW, Lippendorf/Germany

Source: Alstom Power Generation, Mannheim

# PM synchronous High-speed machines

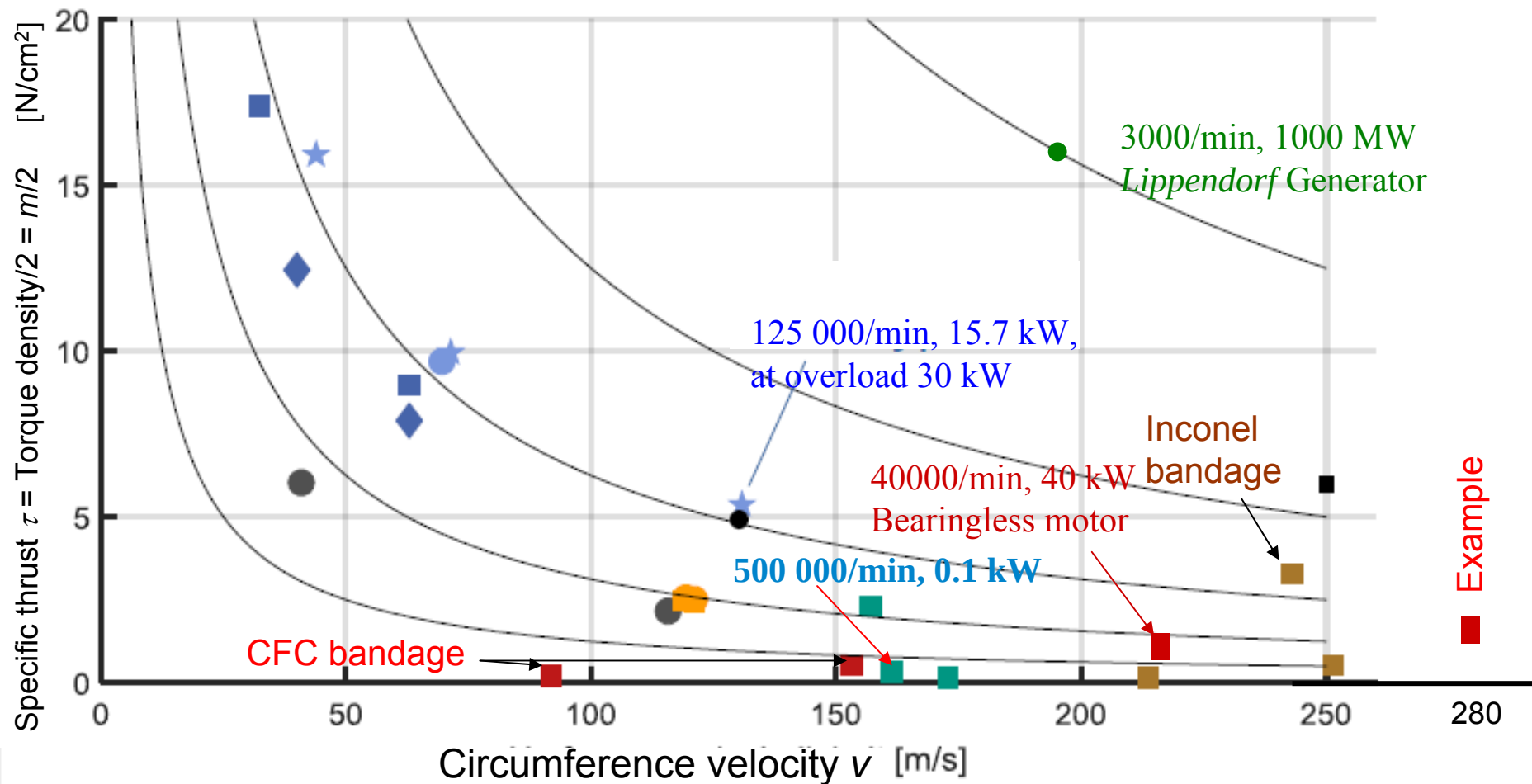
| Literature           | Sleeve type     | Maximum speed (rpm) | Power (kW) | Rotor diameter (mm) | Sleeve thickness (mm)   | Air-gap length (mm) | Stator diameter (mm) | Stack length (mm) |
|----------------------|-----------------|---------------------|------------|---------------------|-------------------------|---------------------|----------------------|-------------------|
| L. Zhao et al.       | Hollow shaft    | 200,000             | 2          | 22                  | -                       | 0.8                 | 35                   | 21                |
| C. Zwyssig et al.    | Titanium        | 500,000             | 1          | 10                  | 0.5                     | -                   | 25                   | 30                |
| P. D. Pfister et al. | Titanium        | 200,000             | 2.19       | 16.48               | 2                       | 1.36                | -                    | 30                |
| A. Tüysüz et al.     | Titanium        | 280,000             | 1          | 11                  | -                       | 0.75                | 27.5                 | 33                |
| C. Zwyssig et al.    | Titanium        | 500,000             | 0.1        | 6                   | -                       | -                   | 16                   | 15                |
| D. K. Hong et al.    | Inconel 718     | 120,000             | 15         | 34                  | 4.5                     | 1                   | 120                  | 50                |
| J. H. Ahn et al.     | Inconel 718     | 400,000             | 0.5        | 11.6                | -                       | 0.35                | 30                   | 19                |
| T. Abe et al.        | Inconel         | 240,000             | 5          | 20                  | 2                       | 0.5                 | 74                   | 40                |
| S. Jumayev et al.    | Stainless steel | 80,000              | 0.05       | 5.5                 | 0.25                    | 0.7                 | 22                   | 16                |
| T. Noguchi et al.    | Carbon fiber    | 220,000             | 2          | 25                  | 5 (sleeve + air-gap)    |                     | 110                  | 29                |
| T. Schneider et al.  | Carbon fiber    | 60,000              | 0.5        | 29.2                | 1                       | 1.4                 | 60                   | 36                |
| T. Noguchi et al.    | Glass fiber     | 150,000             | 1.5        | 19.5                | 4.25 (sleeve + air-gap) |                     | 70                   | 30                |

Source: Schiefer, M.: Antriebssysteme 2017,  
VDE/Karlsruhe, Germany

**“Specific thrust”  $\tau = m/2$  (  $\sim$  torque density  $m$ )  
vs. circumference velocity  $v \sim \sqrt{\sigma}$  of high-speed machines**



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Source: Schiefer, M.: Antriebssysteme 2017, VDE/Karlsruhe, Germany





## Example:

Experts only

### High-Speed PM generator with single stage turbine



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$$500 \text{ kW}, \quad 32000 / \text{min}, \quad d = 167 \text{ mm}: \quad v = d \cdot \pi \cdot n = 280 \text{ m/s}$$

Outer motor diameter (with water – jacket):  $d_{so} = 320 \text{ mm}$ ,  $l_{Fe} \approx 200 \text{ mm}$

Total rotor length (overall):  $L = 520 \text{ mm}$

$$M = 149 \text{ Nm}, \quad m = \frac{M}{d^2 l_{Fe} \pi / 4} = 3.4 \text{ N/cm}^2$$

$$B_\delta \approx 0.7 \text{ T}, \quad m \sim A \cdot B_\delta \Rightarrow A = 377 \frac{\text{A}}{\text{cm}} = \frac{6 \cdot N_s \cdot I_s}{d \cdot \pi} \Rightarrow N_s \cdot I_s = 3300 \text{ A}$$

$$U_i = \sqrt{2} \cdot \pi \cdot n \cdot N_s \cdot k_w \cdot d \cdot l_{Fe} \cdot B_\delta \Rightarrow \frac{U_i}{N_s} = 50.4 \text{ V}$$

Fundamental winding factor  $k_w \cong 0.9$

$$\text{Check : Power (at } \cos \varphi = 1 \text{): } 3 \cdot U_s \cdot I_s \approx 3 \cdot U_i \cdot I_s = 3 \cdot \frac{U_i}{N_s} \cdot N_s I_s = 500 \text{ kW}$$

$$\text{e.g.: } N_s = 6, U_i \cdot \sqrt{3} = 533 \text{ V}, I_s = 550 \text{ A}$$

Based on: Source: Piller, Germany



# Elektrische Hochdrehzahlantriebe - Auslegungsgrundlagen & Beispiele aus der Praxis (Electric high-speed drives – design & examples)

## Contents

- Basics on High-speed Drives
- Mechanical challenges of High-speed drives
- Which type of E-machine for high speed?
- Mechanical integrity at high speed
- Bearing concepts for high speed
- Electromagnetic design for High-Speed
- Examples for High-Speed drives
- Conclusions

# Conclusions

- High speed = **high circumference speed** 100 ... 250 m/s
- **Small** volume/power ratio & **gearless** drive system
- Wide rated “power/speed”-range:  
(500 000 ... 1 000 000)/min, 0.1 kW ... 3000 /min, 1 000 MW
- Different **bearing systems**
- PM & electrically excited synchronous machines,  
induction, homo-polar synchronous & switched reluctance machines
- Inverter fundamental frequency several kHz;  
**output filters** / three-level voltage source / elevated switching frequency
- Wide field of applications:  
**Increasing numbers of high-speed drives expected in the future**

# Elektrische Hochdrehzahlantriebe - Auslegungsgrundlagen & Beispiele aus der Praxis (Electric high-speed drives – design & examples)



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***Thank you for your attention !***

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