

4. Electrically excited synchronous machines



Source:
Siemens AG, Germany



DARMSTADT
UNIVERSITY OF
TECHNOLOGY



Dept. of Electrical Energy Conversion
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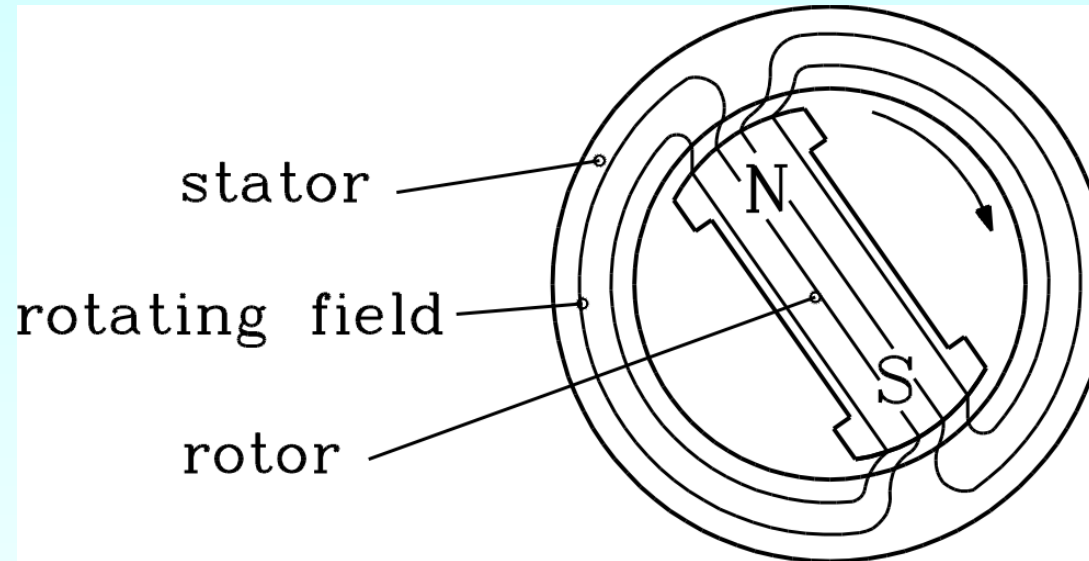


European
Chinese
Link in
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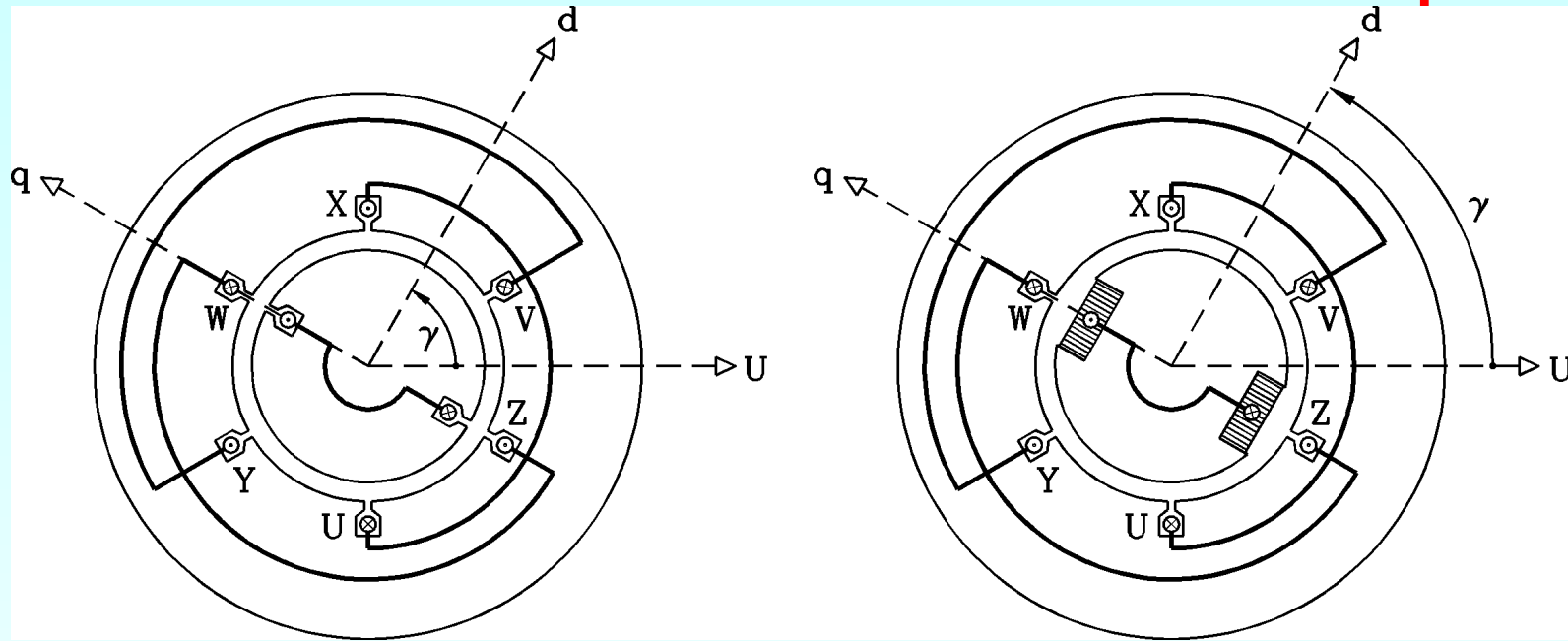
AC Rotating field machines: Basic principle

- AC rotating field machines: Induction machines, synchronous machines
- **Example:** Salient pole rotor synchronous machine: Working principle: 2-pole rotating field



- 3-phase sinus current system (rms I_s) in stator 3-phase winding excites rotating stator field.
- Exciting rotor winding (“**salient poles**”) fed via 2 slip rings with DC current: “**field current** / I_f ”. A 2-pole rotor magnetic DC field is excited.
- The 2-pole stator rotating field pulls via magnetic force the rotor **SYNCHRONOUSLY**.
- For calculating the operational performance of **AC rotating field machines** the calculation of the rotating field and its effects (voltage induction, torque generation) is needed. We use *AMPERE*’ s law, *FARADAY*’ s induction law, winding schemes and *FOURIER*-analysis.

Synchronous machine with round rotor and salient pole rotor

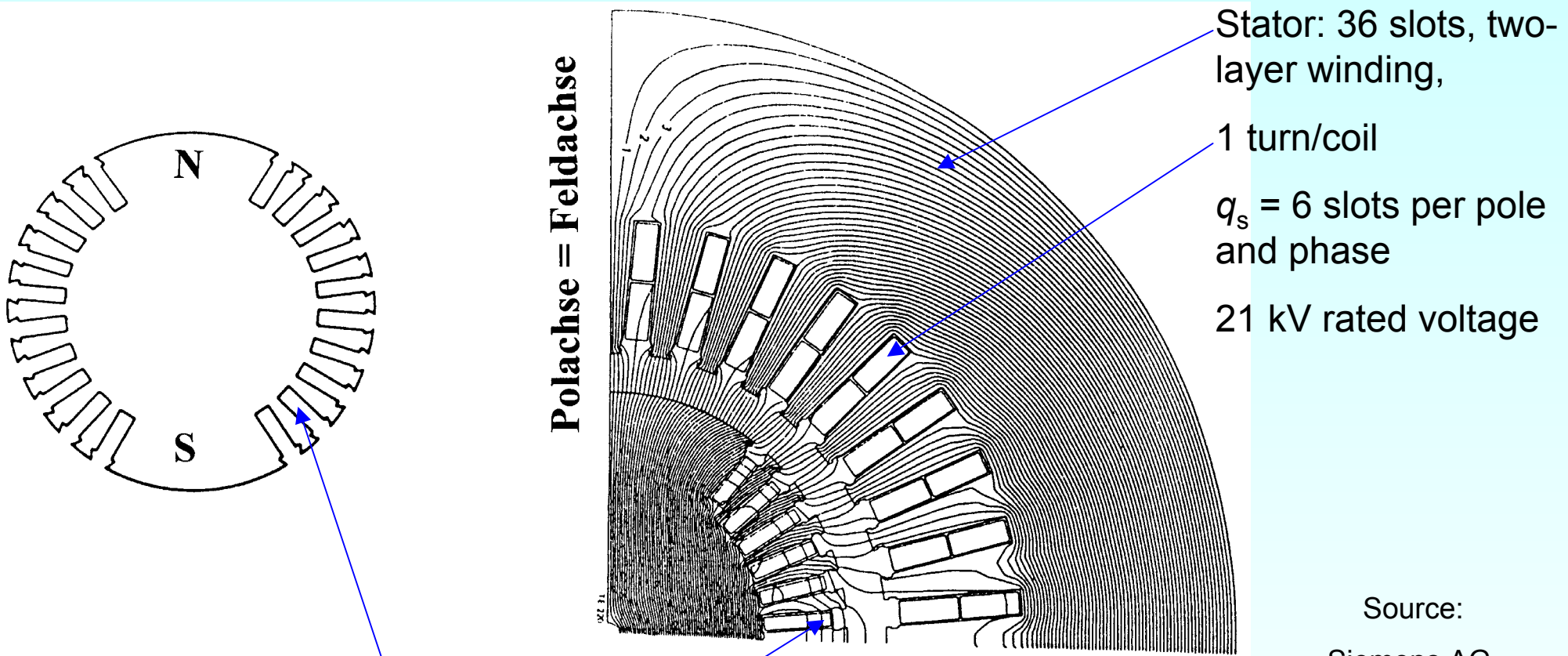


ROUND ROTOR: Field winding distributed in rotor slots; constant air gap

SALIENT POLE ROTOR: concentrated field winding on rotor poles; air gap is minimum at pole centre

- **Synchronous machine:** Rotor field winding excites static magnetic rotor field with DC field current I_f .
- **MOTOR**-operation: Stator 3-phase ac current system I_s excites **stator rotating air gap field**. This field rotates with $n = f_s/p$ and attracts rotor magnetic field, which has same number of poles. So rotor will rotate **synchronously** with stator field.
- **GENERATOR**-mode: Rotor is driven mechanically, and induces with rotor field in the stator winding a 3-phase voltage system with frequency $f_s = n \cdot p$. Stator current due to this voltage excites stator field, which rotates **synchronously with rotor**.

Synchronous machine with round rotor: Turbine generator for thermal power plant



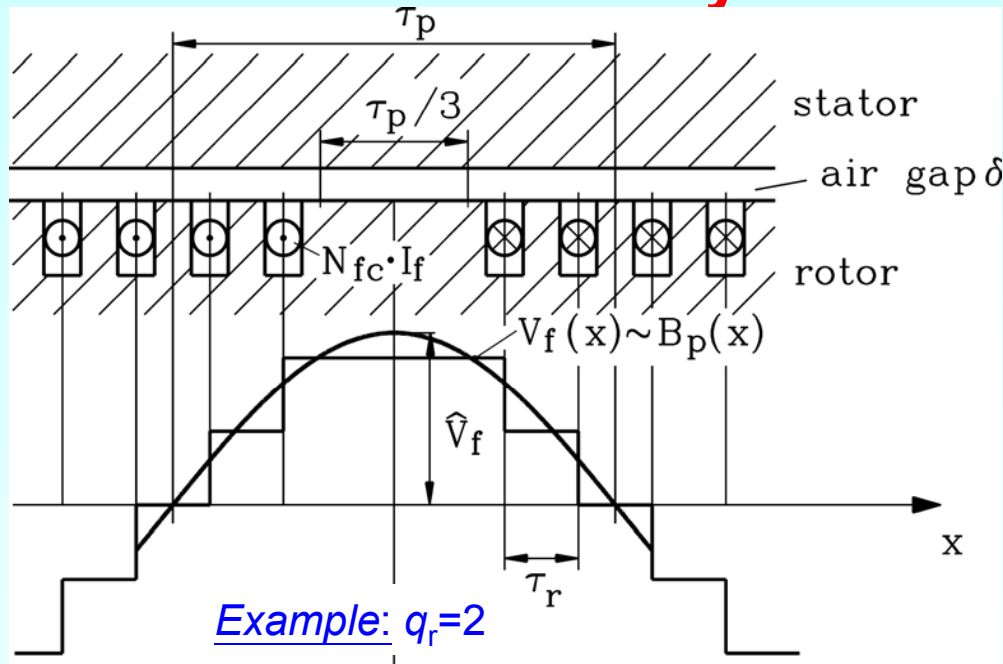
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Two-pole configuration: Rotor winding in rotor slots;

left: cross section with $q_r = 5$ rotor coils per pole

right: no-load field plot with $q_r = 6$ rotor coils per pole, stator current is zero

Rotor air gap field and stator back EMF of round rotor synchronous machine



- Rotor m.m.f. and air gap field distribution have steps due to slots and contain fundamental ($\mu = 1$):

$$\hat{V}_f = \frac{2}{\pi} \cdot \frac{N_f}{p} \cdot (k_{p,f} k_{d,f}) \cdot I_f$$

$$\hat{B}_p = \mu_0 \frac{\hat{V}_f}{\delta}, \quad N_f = 2p \cdot q_r \cdot N_{fc}$$

$$k_{p,f} = \sin\left(\frac{W}{\tau_p} \cdot \frac{\pi}{2}\right) = \sin(\pi/3) = \frac{\sqrt{3}}{2}$$

$$k_{d,f} = \frac{\sin(\pi/6)}{q_r \sin(\pi/(6q_r))}, \quad k_{wf} = k_{pf} k_{df}$$

- Back EMF U_p (synchronously induced stator voltage): Rotor field fundamental B_p induces in 3-phase stator winding at speed n a 3-phase voltage system U_p :

$$U_p = \omega \cdot \Psi_p / \sqrt{2} = \omega \cdot N_s k_{w,s} \cdot \Phi_p / \sqrt{2} = \sqrt{2} \pi f \cdot N_s k_{w,s} \cdot \frac{2}{\pi} l \tau_p \hat{B}_p$$

with frequency $f_s = n \cdot p \Rightarrow$ Current I_s will flow in stator winding.

Round rotor synchronous machine: Equivalent circuit

- Stator winding:** Three phase AC winding like in induction machines with self-induced voltage due to stator rotating magnetic field, described by stator air gap field **main reactance** X_h and **stator leakage flux reactance** $X_{s\sigma}$. With **stator phase resistance** R_s we get stator voltage equation per phase:

$$\underline{U}_s = \underline{U}_p + jX_h \underline{I}_s + jX_{s\sigma} \underline{I}_s + R_s \underline{I}_s$$

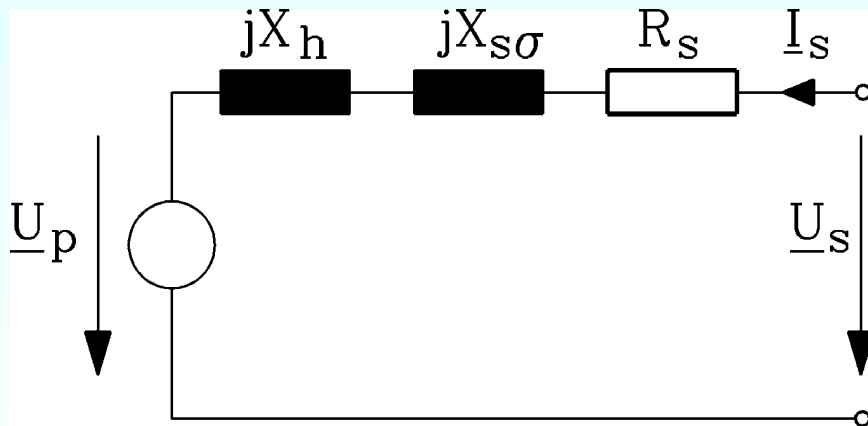
$$\underline{U}_s = \underline{U}_p + jX_d \underline{I}_s + R_s \underline{I}_s$$

"synchronous reactance":

$$X_d = X_{s\sigma} + X_h$$

contains effect of total stator magnetic field !

- Equivalent circuit per stator phase:** for stator voltage equation (ac voltage and current). In rotor winding only DC voltage and current: $U_f = R_f \cdot I_f$

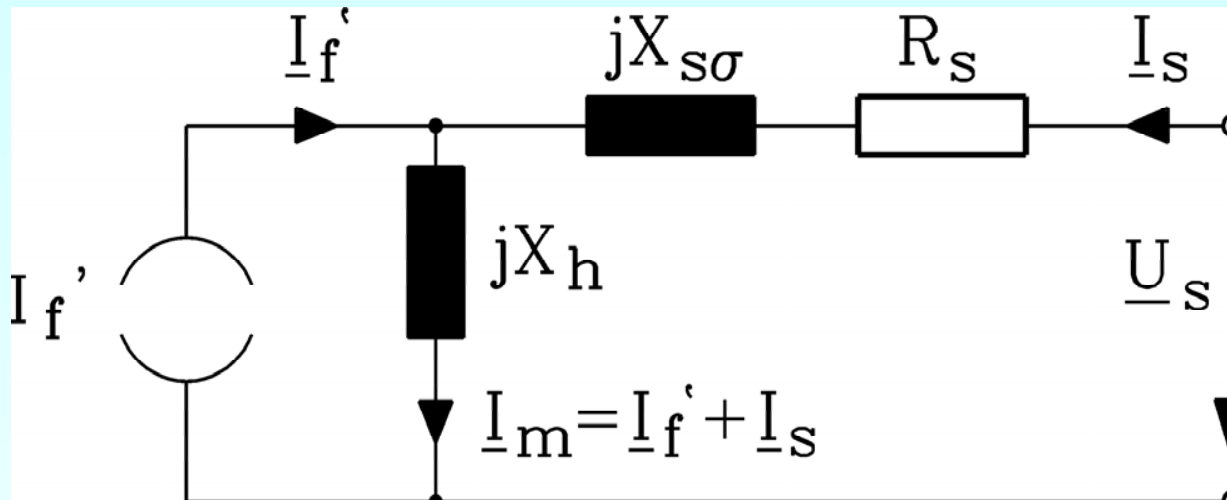


• Rotor electric circuit:

U_f : Rotor dc field voltage: (exciter voltage): U_f impresses via 2 slip rings and carbon brushes a rotor DC current (**field current I_f**) into rotor field winding. Field winding resistance is R_f .

Alternative “current-source” equivalent circuit

$$\underline{U}_s = \underline{U}_p + jX_d \underline{I}_s + R_s \underline{I}_s$$



Current source equivalent circuit, where voltage drop of $\underline{I}_f'$ at jX_h gives $\underline{U}_p$!

$$\underline{U}_p = jX_h \underline{I}_f'$$

Amplitude and phase shift of $\underline{U}_p$ may be described in equivalent circuit by **fictive AC stator current $\underline{I}_f'$!**

Transfer ratio for rotor field current

- **Stator self-induced voltage:** $\underline{U}_{s,s} = jX_h \underline{I}_s$ by stator air-gap field
- **Back EMF $\underline{U}_p$:** Induced by rotor air gap field. It may be changed by field current I_f arbitrarily DURING OPERATION = " **synchronous machine is controlled voltage source**".

a) **Amplitude of $\underline{U}_p$** is determined via I_f .

b) **Phase shift** of $\underline{U}_p$ with respect to stator voltage $\underline{U}_s$ is determined by relative position of rotor north pole axis with respect to stator north pole axis. Rotor pole position is described by **load angle ϑ** .

- **Amplitude and phase shift of $\underline{U}_p$:** may be described in equivalent circuit by **fictive AC stator current $\underline{I}'_f$** : $\underline{U}_p = jX_h \underline{I}'_f$

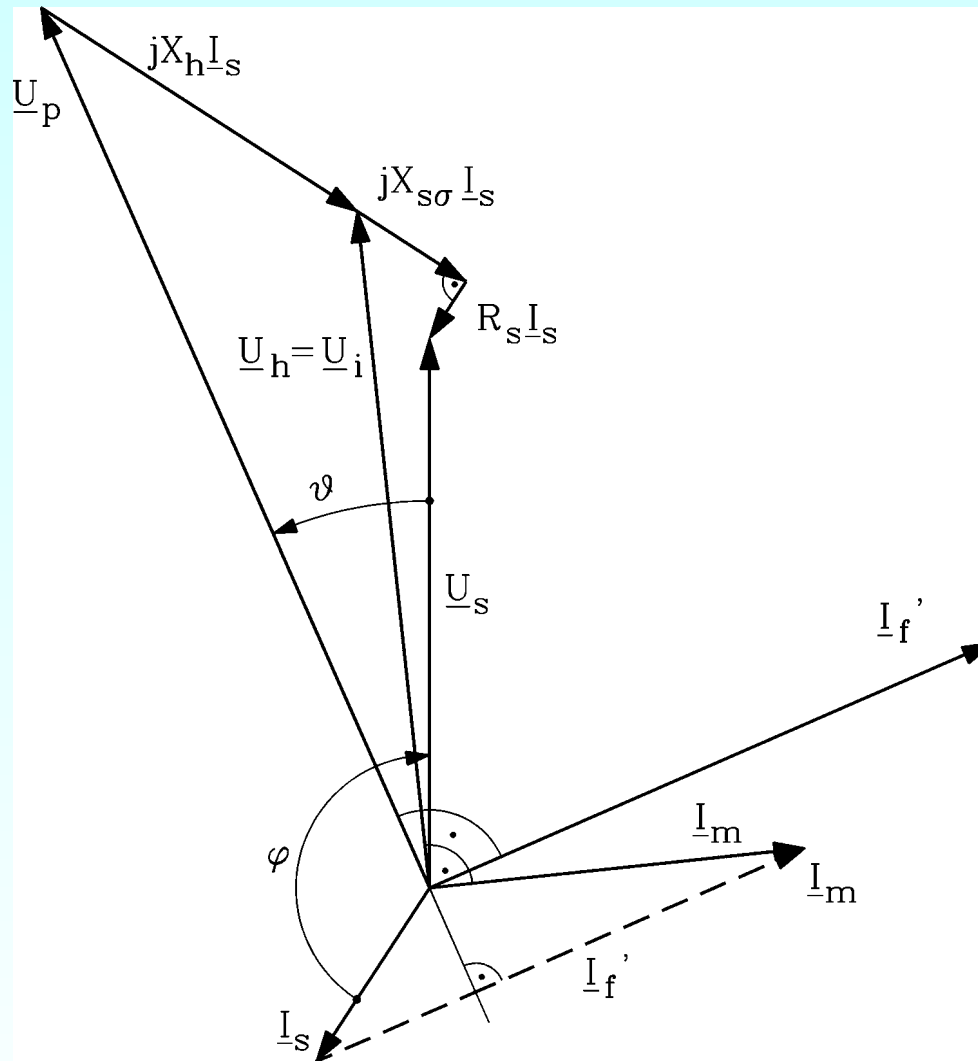
- **This defines transfer ratio of field current $\ddot{u}_{If}$:** $I'_f = \frac{1}{\ddot{u}_{If}} I_f$

$$I'_f = \frac{U_p}{U_{s,s}} I_s = \frac{B_p}{B_{s,\delta}} I_s = \hat{V}_f \cdot \frac{I_s}{\hat{V}_s} : \text{ shall be } \frac{1}{\ddot{u}_{If}} I_f$$

$$\text{With } \hat{V}_f = \frac{2}{\pi} \cdot \frac{N_f}{p} \cdot k_{wf} \cdot I_f, \quad \hat{V}_s = \frac{\sqrt{2}}{\pi} \cdot \frac{m_s N_s}{p} \cdot k_{ws} \cdot I_s \quad \text{we get:}$$

$$\ddot{u}_{If} = \frac{m_s N_s k_{ws} \sqrt{2}}{2 N_f k_{wf}}$$

Phasor diagram of round rotor synchronous machine



- **Example:** Generator, over-excited:

- **a) electrical active power:**

$$P_e = m_s U_s I_s \cos \varphi$$

Phase angle φ between -90° and -180° :
Hence $\cos \varphi$ negative: P_e is negative = power delivered to the grid
(GENERATOR).

$P_e < 0$: **Generator**,

$P_e > 0$: **Motor**.

- **b) electrical reactive power:**

$$Q = m_s U_s I_s \sin \varphi$$

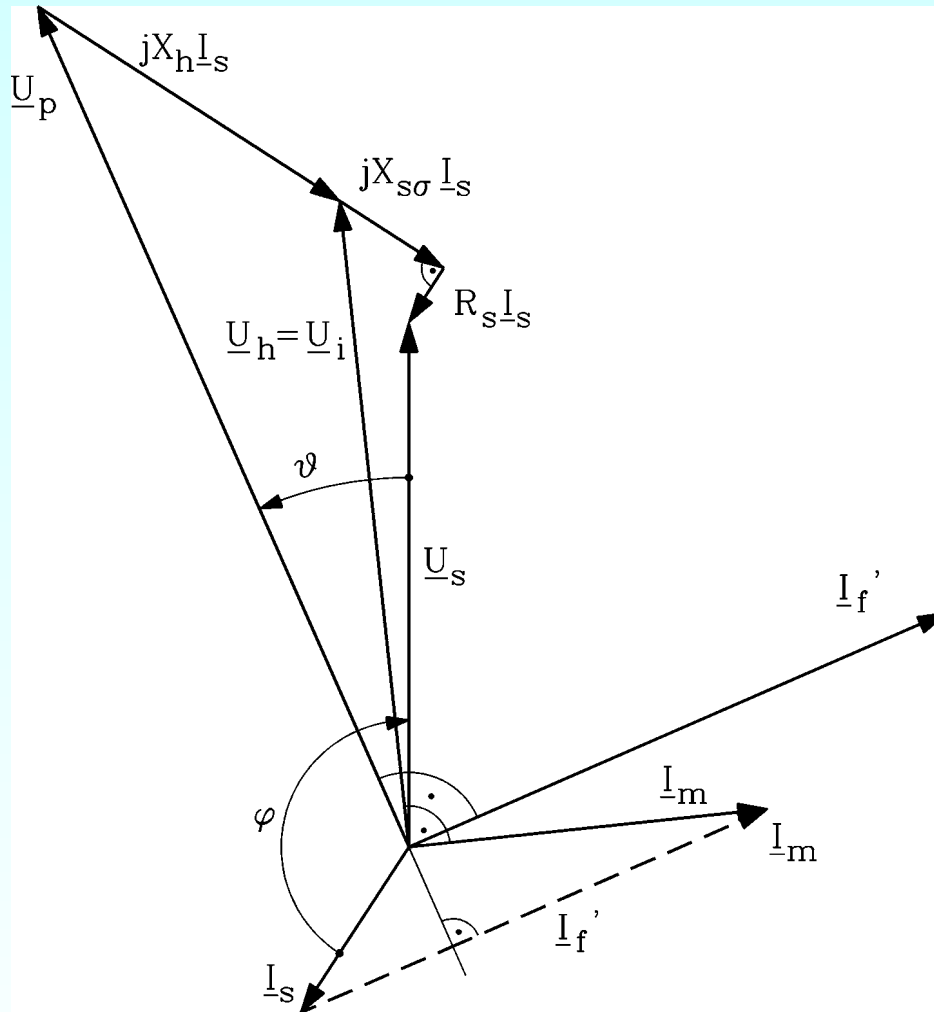
Phase angle φ negative = stator current LEADS ahead stator voltage:

$\sin \varphi$ negative: Q is negative = capacitive reactive power: Machine is **capacitive consumer**.

$Q < 0$: **over-excited**, capacitive consumer.

$Q > 0$: **under-excited**, inductive consumer.

Load angle ϑ , internal voltage U_h , magnetising current I_m



- **Load angle ϑ** between stator phase voltage $\underline{U}_s$ and back EMF phasor $\underline{U}_p$. Counted in mathematical positive sense (counter-clockwise).

- **Internal voltage U_h** is induced in stator winding by resulting air gap field (rotor and stator field):

$$\underline{U}_h = \underline{U}_p + jX_h \underline{I}_s$$

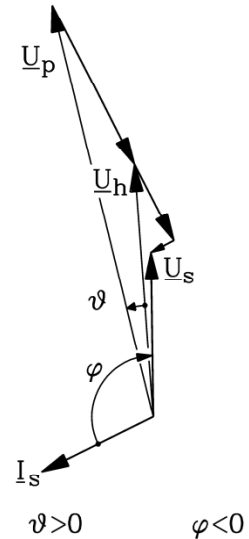
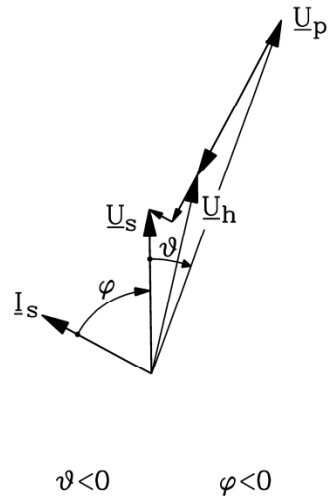
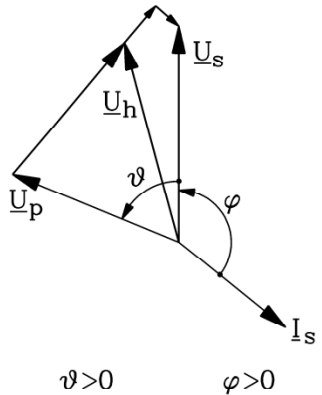
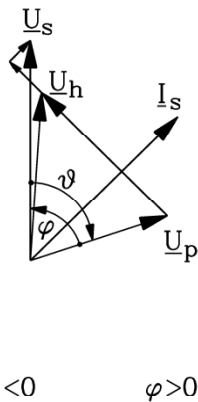
- **Magnetising current I_m :**

Fictitious stator current to excite resulting air gap field (rotor and stator field):

$$\underline{I}_m = \underline{I}'_f + \underline{I}_s$$

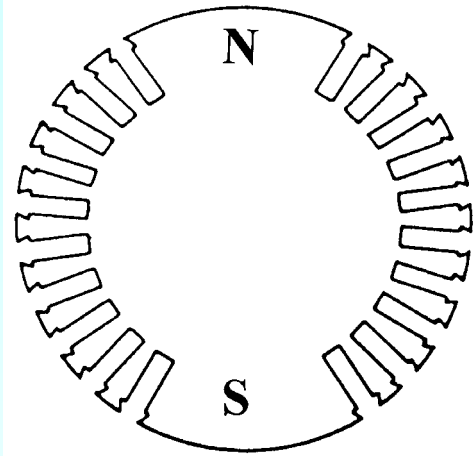
- Voltage triangle $\underline{U}_p, jX_h \underline{I}_s, \underline{U}_h$ and current triangle $\underline{I}'_f, \underline{I}_s, \underline{I}_m$ are of the same shape, but shifted by 90° .

Over-/under-excitation, generator/motor-mode

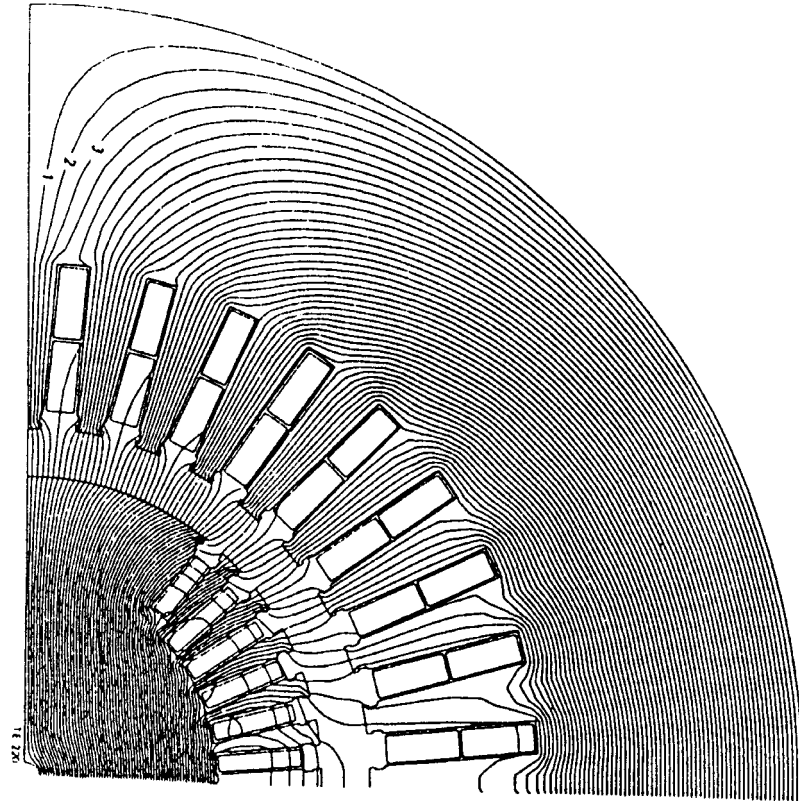
GENERATOR: rotor leading	MOTOR: rotor lagging	
 $\delta > 0$ $\phi < 0$	 $\delta < 0$ $\phi < 0$	overexcited
 $\delta > 0$ $\phi > 0$	 $\delta < 0$ $\phi > 0$	underexcited

- Generator mode: $\delta > 0$:** Rotor *LEADS* ahead of resulting rotating magnetic field = Phasor $\underline{U}_p$ *LEADS* ahead of $\underline{U}_h$.
- Motor mode: $\delta < 0$:** Rotor *LAGS* behind resulting magnetic field = Phasor $\underline{U}_p$ *LAGS* behind $\underline{U}_h$.
- Over-excitation: Machine is capacitive consumer:** Phasor $\underline{U}_p$ is longer than phasor $\underline{U}_h$: big field current I_f is needed.
- Under-excitation: Machine is inductive consumer:** Phasor $\underline{U}_p$ is shorter than phasor $\underline{U}_h$: small field current I_f is needed.
- Facit:**
Stator- and rotor field rotate always synchronously. Generator- and motor mode are only defined by sign of load angle δ .

Round rotor synchronous machine: Magnetic field at no-load



Polachse = Feldachse



Rotor cross section without field winding:

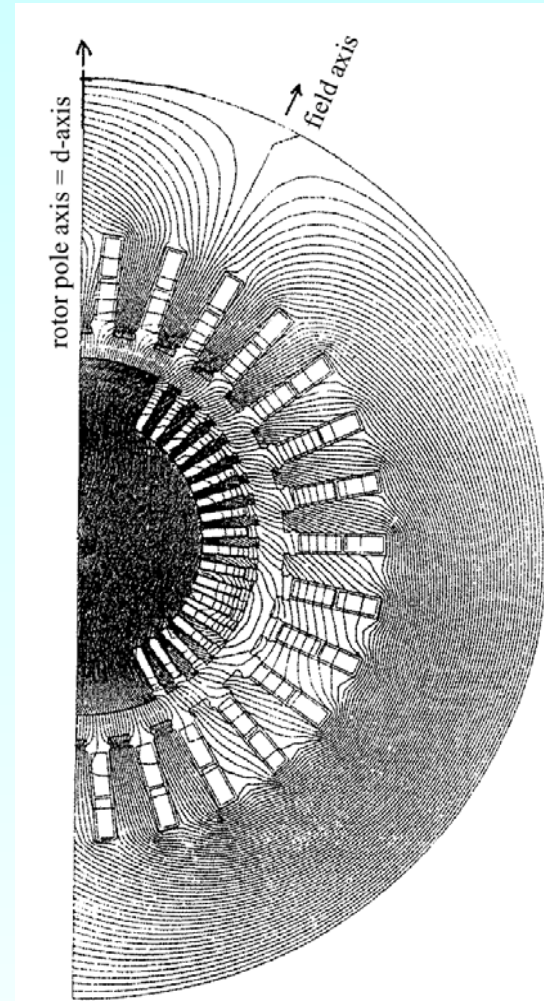
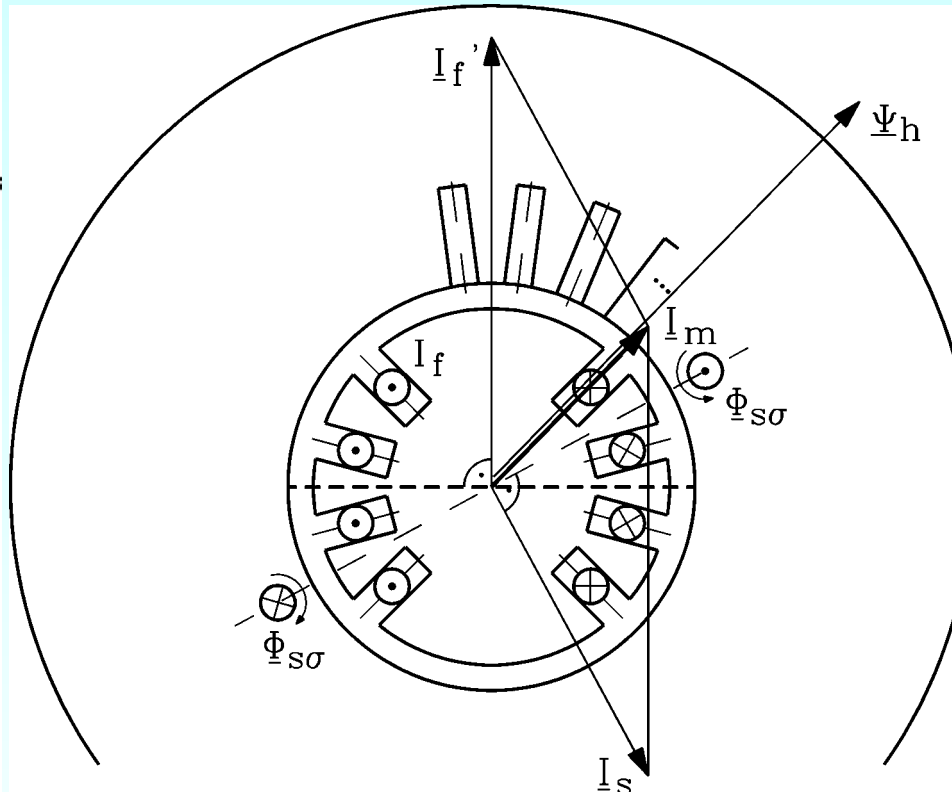
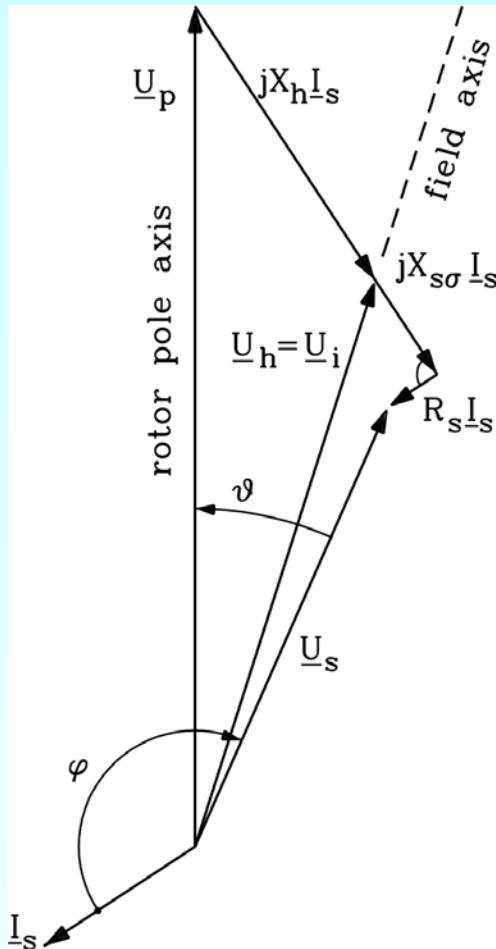
- Slots per pole $2q_r = 10$, 2-pole rotor
- Rotor may be constructed of massive iron, as rotor contains only **static magnetic field** !

Magnetic field at no-load ($I_s = 0$, $I_f > 0$):

- Field winding excited by I_f
- Stator winding without current (**no-load**)
- Field lines in air gap in radial direction = no tangential magnetic pull = **torque is zero** !

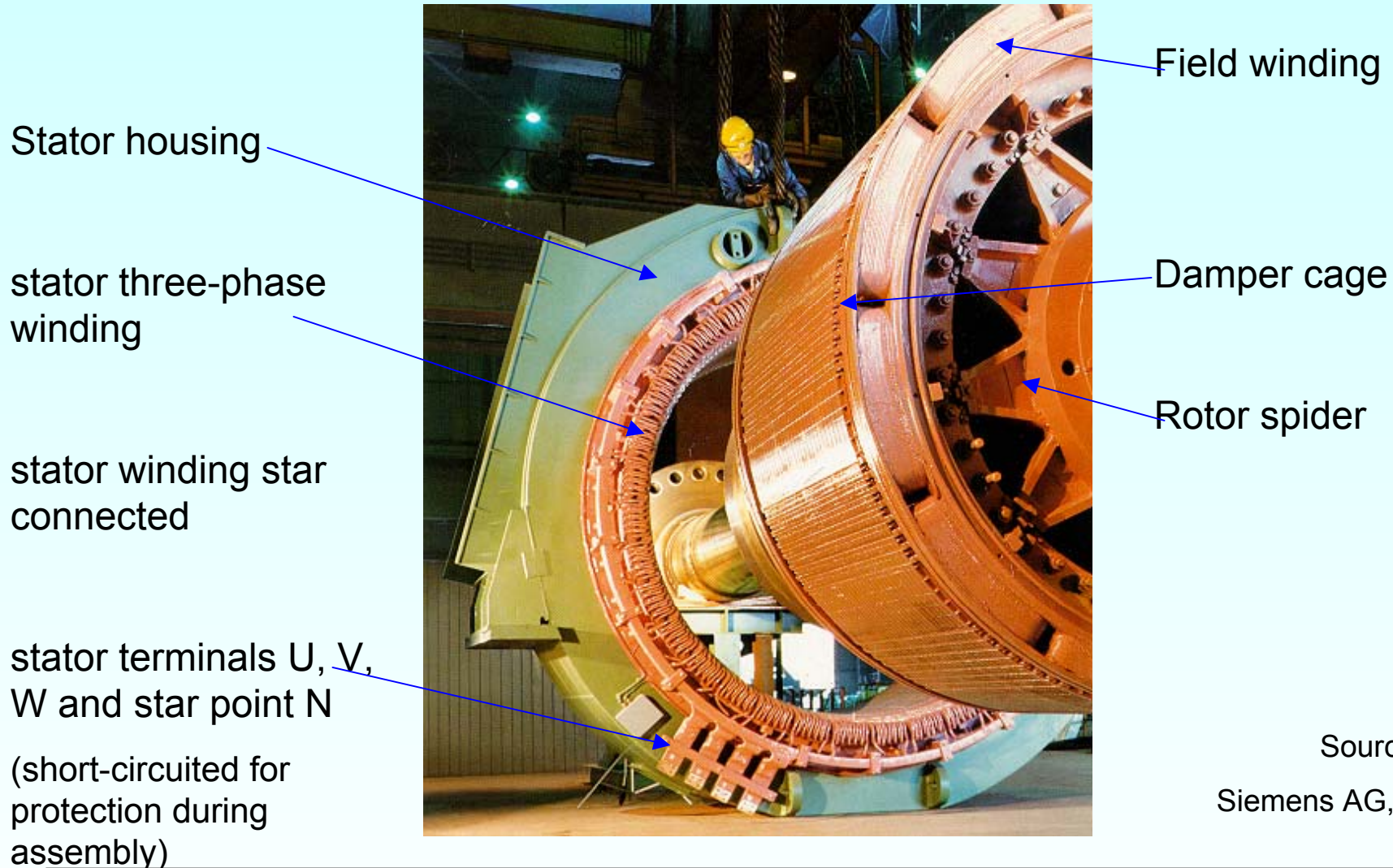
(Example: $2p = 2$, $q_s = 6$, $q_r = 6$)

Round rotor synchronous machine: Magnetic field at load



- Magnetic field at load ($I_s > 0$, $I_f > 0$): Rotor pole axis = Direction of $\underline{U}_p$, resulting field axis = Direction of $\underline{U}_h$
- Field lines in air gap have also tangential component = tangential magnetic pull = torque !

Round rotor synchronous machine for 10 poles



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Round rotor synchronous machine for 4 poles

Stacking of rotor with iron sheets

Rotor slots for field coils

Damper cage

Concentric field coils



Source:

VATech Hydro, Austria

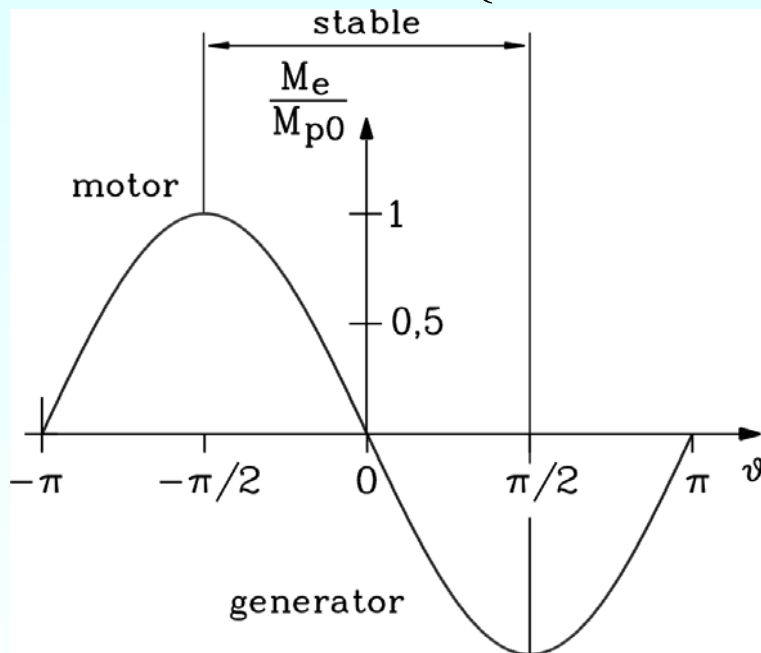
Torque of round rotor synchronous machine at $U_s = \text{const.} \ \& \ R_s = 0$

- Machine operates at RIGID grid: $\underline{U}_s = \text{constant} = U_s$ (= phasor put in real axis of complex plane):

$$\underline{U}_p = U_p (\cos \vartheta + j \cdot \sin \vartheta) \text{ and } \underline{I}_s = (U_s - \underline{U}_p) / (jX_d) \Rightarrow \underline{I}_s^* = (U_s - \underline{U}_p^*) / (-jX_d)$$

- Active power P_e : $P_e = m_s U_s I_s \cos \varphi = m_s \cdot \text{Re}\{\underline{U}_s \underline{I}_s^*\}$ (*: conjugate complex)

$$P_e = m_s \cdot \text{Re}\left\{U_s \cdot \frac{U_s - U_p (\cos \vartheta - j \cdot \sin \vartheta)}{-jX_d}\right\} = -m_s \frac{U_s U_p}{X_d} \sin \vartheta$$



- Electromagnetic torque:

$$M_e = \frac{P_m}{\Omega_{syn}} = \frac{P_e}{\Omega_{syn}} = -\frac{m_s}{\Omega_{syn}} \cdot \frac{U_s U_p}{X_d} \sin \vartheta = -M_{p0} \sin \vartheta$$

Note:

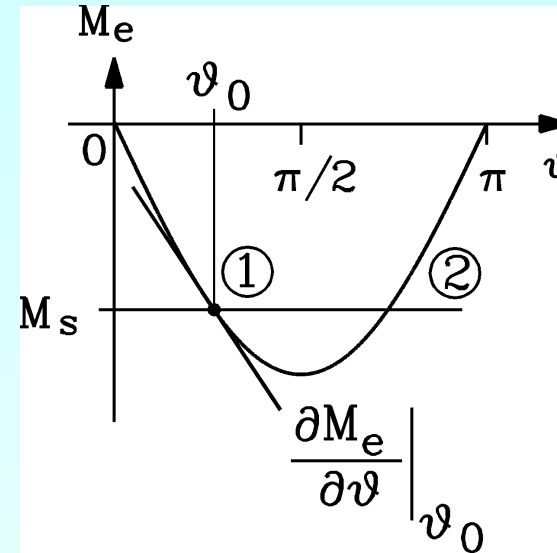
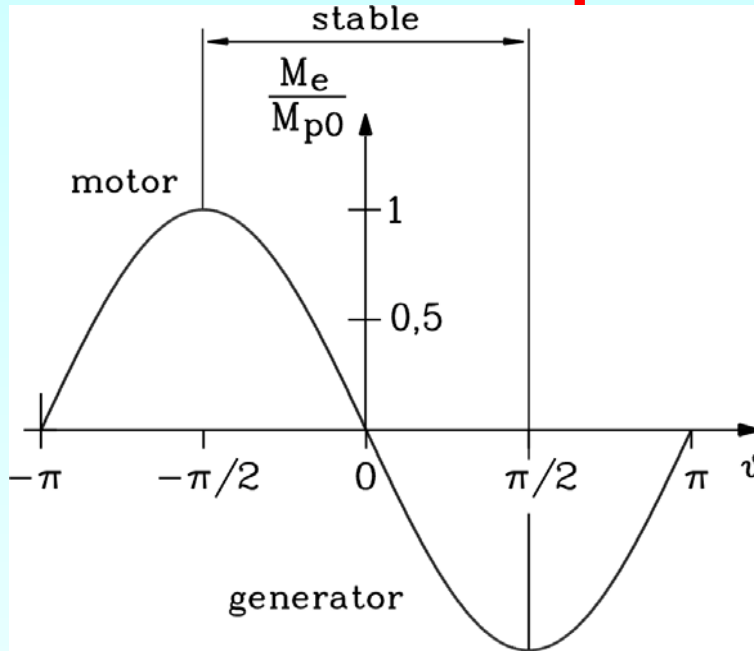
All losses neglected (“unity” efficiency).

Negative torque: Generator: M_e is braking

Positive torque: Motor: M_e is driving

Machine speed is always synchronous speed !

Stable points of operation



- **Example:** Torque-load angle curve $M(\vartheta)$: in generator mode the mechanical driving shaft torque M_s is determining operation points 1 and 2.
- Operation point 1 is **stable**, operation point 2 is **unstable**. The **stability limit** is at load angle $\pi/2$ (generator limit) and $-\pi/2$ (motor limit).

Facit: Synchronous motor and generator **pull-out torque $\pm M_{p0}$** occurs at **pull-out load angle $\pm \pi/2$** . Rotor is "**pulled out**" of synchronism, if load torque exceeds pull-out torque. Result: Pulled-out rotor does not run synchronously with stator magnetic field, which is determined by the grid voltage. The rotor slips ! No active power is converted any longer.

Stability analysis of operation points

- Torque-load angle curve** $M_e(\vartheta)$ linearized in operation point ϑ_0 : **Tangent** as linearization: $M_e(\vartheta) \cong M_e(\vartheta_0) + \partial M_e / \partial \vartheta \cdot \Delta \vartheta$ with $\Delta \vartheta = \vartheta - \vartheta_0$

$$c_\vartheta(\vartheta_0) = \partial M_e / \partial \vartheta \big|_{\vartheta_0} : \text{Equivalent spring constant} \Leftrightarrow \Delta M_e = c_\vartheta \cdot \Delta \vartheta$$

- Change of** load angle with time causes **change of speed** $\Delta \Omega_m$:

$$d\Delta \vartheta / dt = p \cdot \Delta \Omega_m \Rightarrow \Omega_m(t) = \Omega_{syn} + \Delta \Omega_m(t)$$

- NEWTON' s law of motion** $J \frac{d\Delta \Omega_m}{dt} = M_e(\vartheta) - M_s(\vartheta) = c_\vartheta \cdot \Delta \vartheta = J \frac{d\Delta \Omega_m}{dt}$ leads to

$$J \frac{d^2 \Delta \vartheta}{dt^2} - p \cdot c_\vartheta \cdot \Delta \vartheta = 0 \quad \text{a) } |\vartheta| < \pi/2 : c_\vartheta = -|c_\vartheta| < 0, \quad \text{b) } |\vartheta| > \pi/2 : c_\vartheta = |c_\vartheta| > 0$$

$$\text{a) } |\vartheta| < \pi/2 : \Delta \ddot{\vartheta} + (p \cdot |c_\vartheta| / J) \cdot \Delta \vartheta = 0 \Rightarrow \Delta \ddot{\vartheta} + \omega_e^2 \Delta \vartheta = 0 \Rightarrow \Delta \vartheta(t) \sim \sin(\omega_e t)$$

Deviation of load angle from steady state point of operation remains limited: **STABLE** operation

$$\text{b) } |\vartheta| > \pi/2 : \Delta \ddot{\vartheta} - (p \cdot |c_\vartheta| / J) \cdot \Delta \vartheta = 0 \Rightarrow \Delta \ddot{\vartheta} - \omega_e^2 \Delta \vartheta = 0$$

$\Rightarrow \Delta \vartheta(t) \sim \sinh(\omega_e t)$ Deviation of load angle from operation point increases: **UNSTABLE**

Torsional oscillations of synchronous machine

- Deviation of load angle in stable point of operation due to disturbance:

$$|\vartheta| < \pi/2: \quad \Delta \ddot{\vartheta} + (p \cdot |c_{\vartheta}| / J) \cdot \Delta \vartheta = 0 \Rightarrow \Delta \ddot{\vartheta} + \omega_e^2 \Delta \vartheta = 0 \Rightarrow \Delta \vartheta(t) \sim \sin(\omega_e t)$$

leads to differential equation **with oscillation as solution**. Rotor oscillates around steady state point of operation ϑ_0 , which is defined by the stator field, that is generated by the “rigid” grid.

Natural frequency of oscillation (eigen-frequency):

$$f_e = \frac{\omega_e}{2\pi} = \frac{1}{2\pi} \sqrt{\frac{p|c_{\vartheta}|}{J}}$$

Facit: The synchronous machine is performing like a (non-linear) torsional spring.

Example: Operation at no-load ($M_e = 0$, $\vartheta_0 = 0$):

$$|c_{\vartheta}| = |-M_{p0} \cdot \cos(0)| = M_{p0}$$

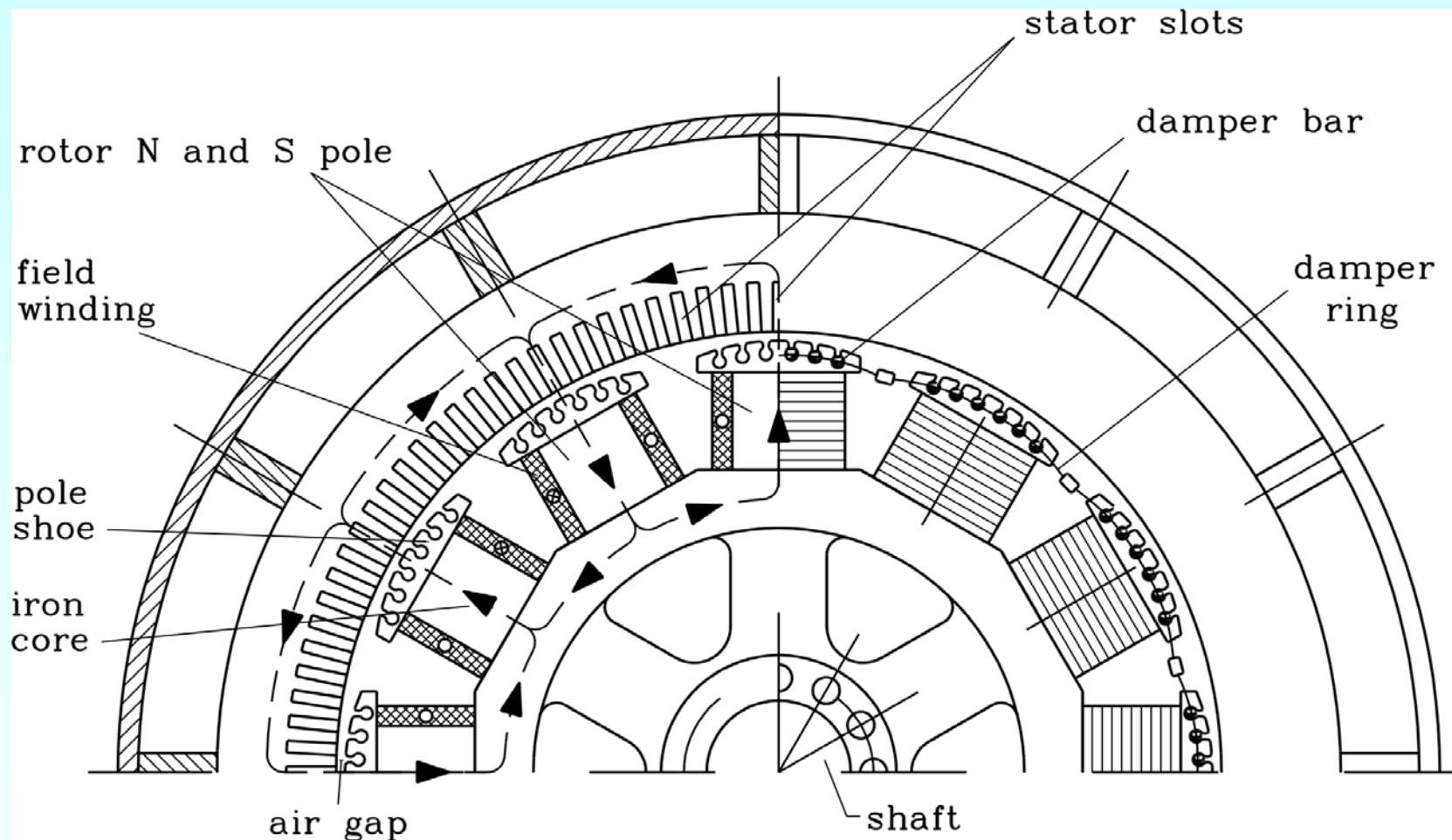
With $p\Omega_{syn} = \omega_N$ and rated acceleration time $T_J = \frac{J \cdot \Omega_{syn}}{M_N}$ we get: $f_e = \frac{1}{2\pi} \sqrt{\frac{\omega_N}{T_J} \cdot \frac{M_{p0}}{M_N}}$

Synchronous motor driving a fan blower for a wind tunnel:

$P_N = 50 \text{ MW}$, $f_N = 50 \text{ Hz}$, $T_J = 10 \text{ s}$, $M_{p0}/M_N = 1.5$,

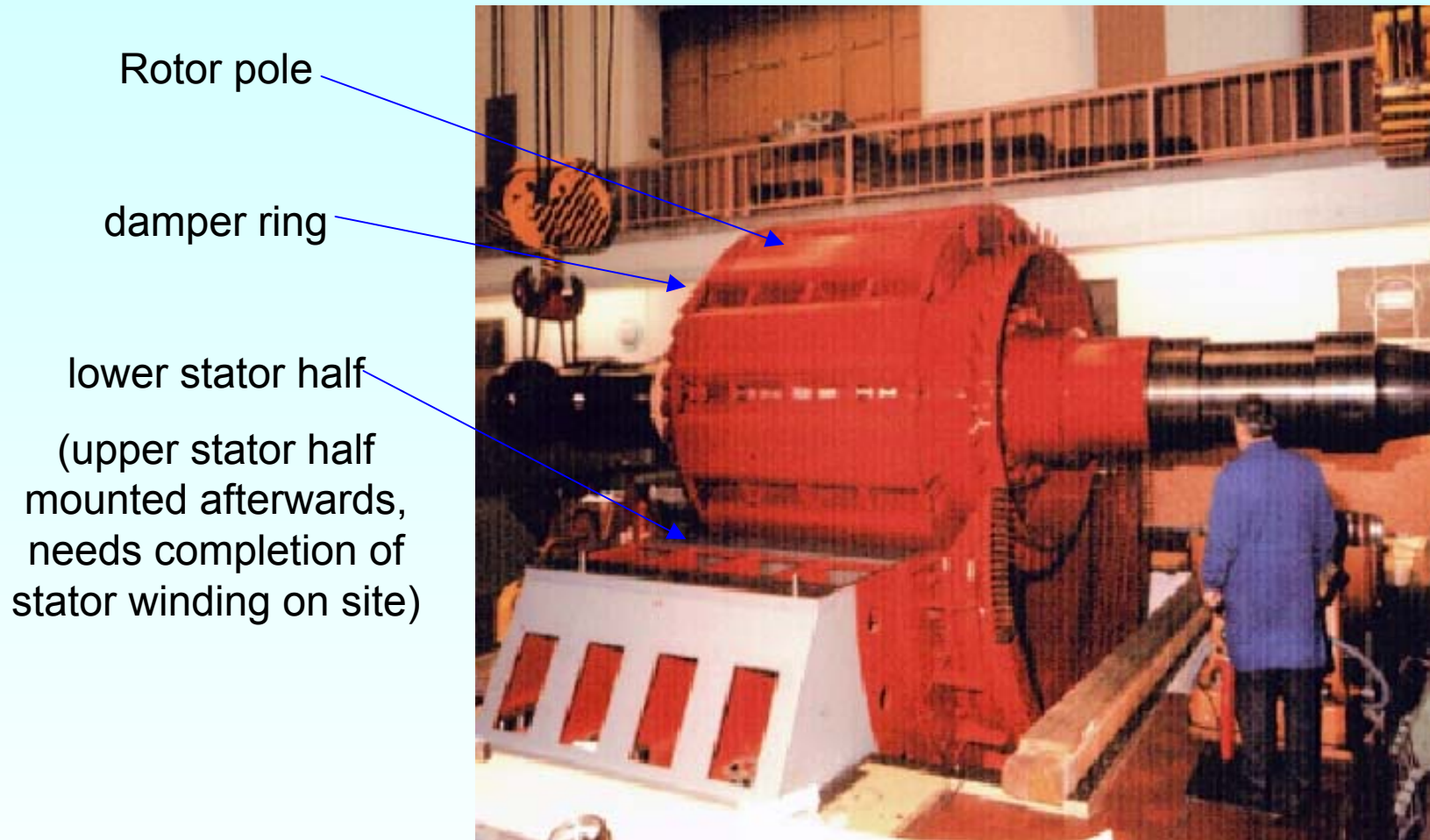
$$f_e = \frac{1}{2\pi} \sqrt{\frac{2\pi 50}{10} \cdot 1.5} = \underline{\underline{1.09 \text{ Hz}}}$$

Synchronous machine with salient pole rotor



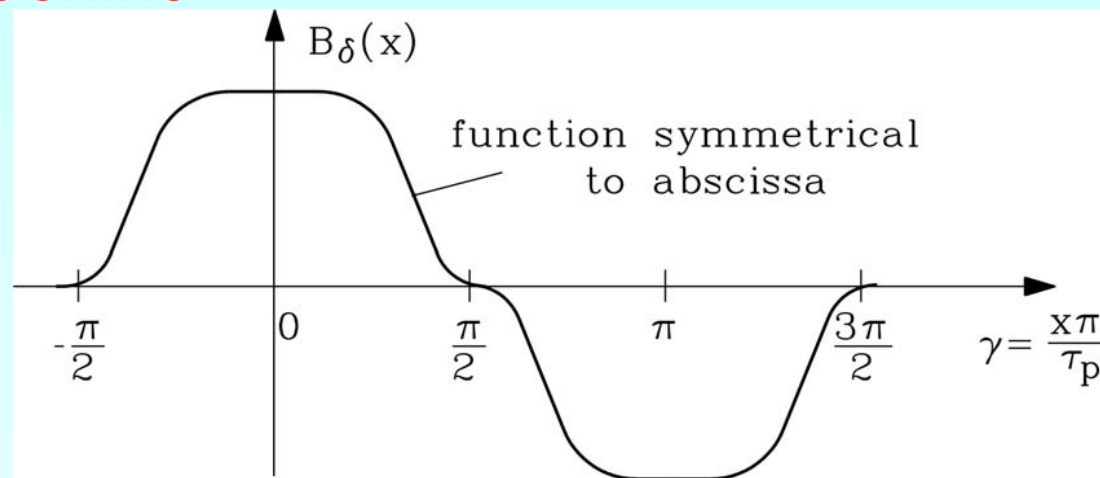
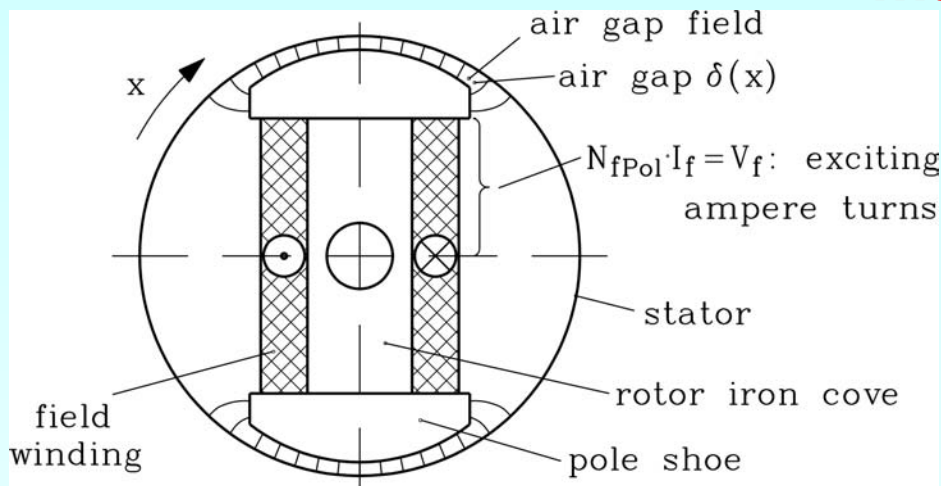
12 pole configuration, for direct grid operation, damper cage to extinguish load angle oscillations

Salient eight pole rotor of pump storage power plant *Kaprun/Austria* during inserting



Source:
VA Tech Hydro,
Austria

Rotor field and back EMF of salient pole synchronous machine



- **Bell shaped rotor air gap field curve $B_\delta(x)$:** A constant m.m.f. V_f excites with a variable air gap $\delta(x)$ a bell shaped field curve. Fundamental of this “bell-shape” ($\mu = 1$):

$$B_\delta(x) = \mu_0 \frac{V_f}{\delta(x)} \rightarrow \text{FOURIER-fundamental wave: Amplitude } \hat{B}_p \text{ proportional to } I_f$$

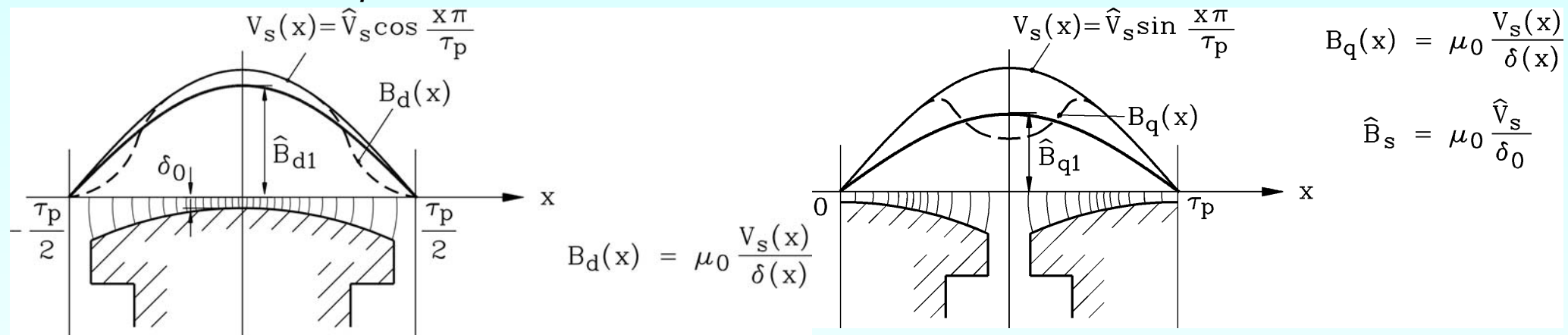
- **Back EMF U_p :** Sinusoidal rotor field fundamental wave B_p induces **in three-phase stator winding** at speed n a three-phase voltage system U_p

$$U_p = \omega \cdot \Psi_p / \sqrt{2} = \omega \cdot N_s k_{w,s} \cdot \Phi_p / \sqrt{2} = \sqrt{2} \pi f \cdot N_s k_{w,s} \cdot \frac{2}{\pi} l \tau_p \hat{B}_p$$

with **frequency** $f = n \cdot p \Rightarrow$ Stator current I_s is flowing in stator winding.

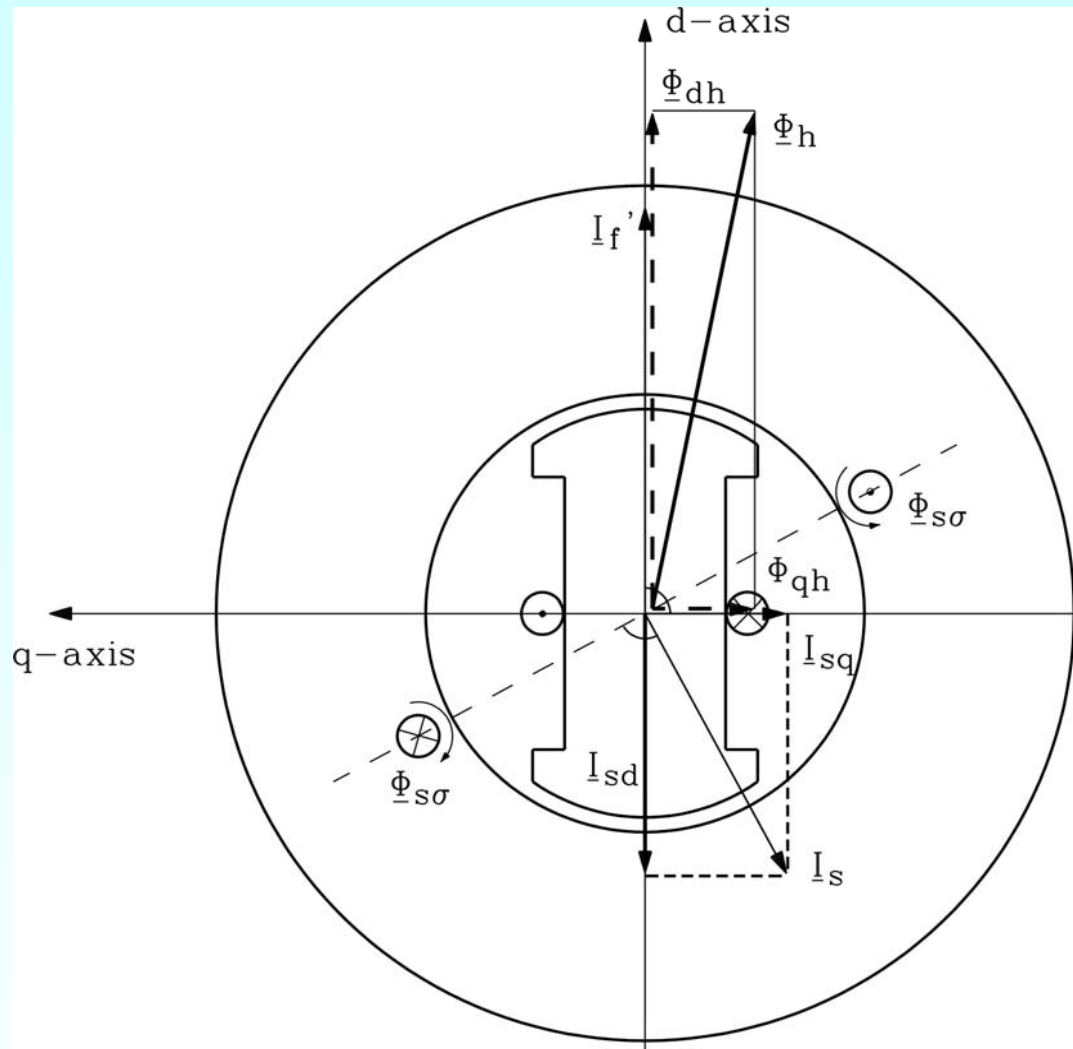
Salient pole synchronous machine: Magnetizing inductance L_h

- Stator winding** is three-phase winding like in induction machines, BUT the air gap is **LARGER** in neutral zone (inter-pole gap of q -axis) than in **pole axis (d -axis)**. Hence for equal m.m.f. V_s (sinus fundamental $\nu = 1$) the corresponding air gap field is **SMALLER** in q -axis than in d -axis and NOT SINUSOIDAL.



- Stator field in d -axis (direct axis):** Fundamental of field a little bit smaller than for constant air gap δ_0 : $c_d = \hat{B}_{d1} / \hat{B}_s < 1$ **ca. 0.95, thus:** $L_{dh} = c_d \cdot L_h$
- Stator field in q -axis (quadrature axis):** Fundamental of field significantly smaller than at constant air gap δ_0 : $c_q = \hat{B}_{q1} / \hat{B}_s \ll 1$ **ca. 0.4 ... 0.5, thus** $L_{qh} = c_q \cdot L_h$

Stator current I_s : d - and q -component



Stator current phasor I_s decomposed into d - and q -component:

$$\underline{I}_s = \underline{I}_{sd} + \underline{I}_{sq}$$

I_{sd} is in phase or opposite phase with fictitious current I_f' . So it excites a stator air gap field in d -axis (in rotor pole axis), which together with rotor field gives d -axis air gap flux Φ_{dh} .

I_{sq} is phase-shifted by 90° to I_{sd} and excites therefore a stator air gap field in q -axis (inter-pole gap). The corresponding air gap flux is Φ_{qh} .

Stator self-induced voltage consists of two, by 90° phase shifted components:

$$j\omega_s L_{dh} \underline{I}_{sd}$$

$$j\omega_s L_{qh} \underline{I}_{sq}$$

and of self-induced voltage of stator leakage flux:

$$j\omega_s L_{s\sigma} \underline{I}_s$$

Stator voltage equation of salient pole synchronous machine

- **Stator voltage equation per phase:** Considering self-induction of main and leakage flux L_{dh} , L_{qh} , $L_{s\sigma}$ and of rotor phase resistance R_s we get :

$$\underline{U}_s = R_s \underline{I}_s + j\omega_s L_{s\sigma} \underline{I}_s + j\omega_s L_{qh} \underline{I}_{sq} + j\omega_s L_{dh} \underline{I}_{sd} + \underline{U}_p$$

or

$$\underline{U}_s = R_s \underline{I}_s + j\omega_s L_{s\sigma} (\underline{I}_{sd} + \underline{I}_{sq}) + j\omega_s (L_{qh} \underline{I}_{sq} + L_{dh} \underline{I}_{sd}) + \underline{U}_p$$

- X_d : **"synchronous d-axis reactance"**: $X_d = X_{s\sigma} + X_{dh} = \omega_s L_{s\sigma} + \omega_s L_{dh}$
- X_q : **"synchronous q-axis reactance"**: $X_q = X_{s\sigma} + X_{qh} = \omega_s L_{s\sigma} + \omega_s L_{qh}$
- **Typical values:** Due to inter-pole gap it is $X_d > X_q$ (typically: $X_q = (0.5 \dots 0.6) \cdot X_d$)
e.g. salient pole hydro-generators, diesel engine generators, reluctance machines, ...
- **Note:** **Round rotor synchronous machine** may be regarded as "special case" of salient pole machine for $X_d = X_q$.

The slot openings of rotor field winding in round rotor machines may also be regarded as non-constant air gap, yielding also $X_d > X_q$ (typically: $X_q = (0.8 \dots 0.9) \cdot X_d$)



Torque of salient pole machine at $U_s = \text{const.}$ & $R_s = 0$

- **OPERATION at "rigid" grid:** $\underline{U}_s = \text{constant}$

We choose: d -axis = Re-axis, q -axis = Im-axis of complex plane:

$$\underline{U}_s = U_{sd} + jU_{sq} \quad \underline{I}_s = I_{sd} + jI_{sq} \quad \underline{U}_p = jU_p$$

$$R_s = 0: \quad \underline{U}_s = jX_d I_{sd} + jX_q I_{sq} + \underline{U}_p \quad \Rightarrow \quad \underline{U}_s = jX_d I_{sd} - X_q I_{sq} + jU_p$$

- **Active power P_e :** $P_e = m_s U_s I_s \cos \varphi = m_s \cdot \text{Re}\{\underline{U}_s \underline{I}_s^*\} = m_s (U_{sd} I_{sd} + U_{sq} I_{sq})$
 $P_e = m_s (-X_q I_{sq} I_{sd} + X_d I_{sd} I_{sq} + U_p I_{sq})$

- **Electromagnetical torque:**

$$M_e = \frac{P_m}{\Omega_{syn}} = \frac{P_e}{\Omega_{syn}} = \frac{m_s}{\Omega_{syn}} \cdot (U_p \cdot I_{sq} + (X_d - X_q) \cdot I_{sd} \cdot I_{sq})$$

- **Two torque components:**

a) prop. U_p as with round rotor machines

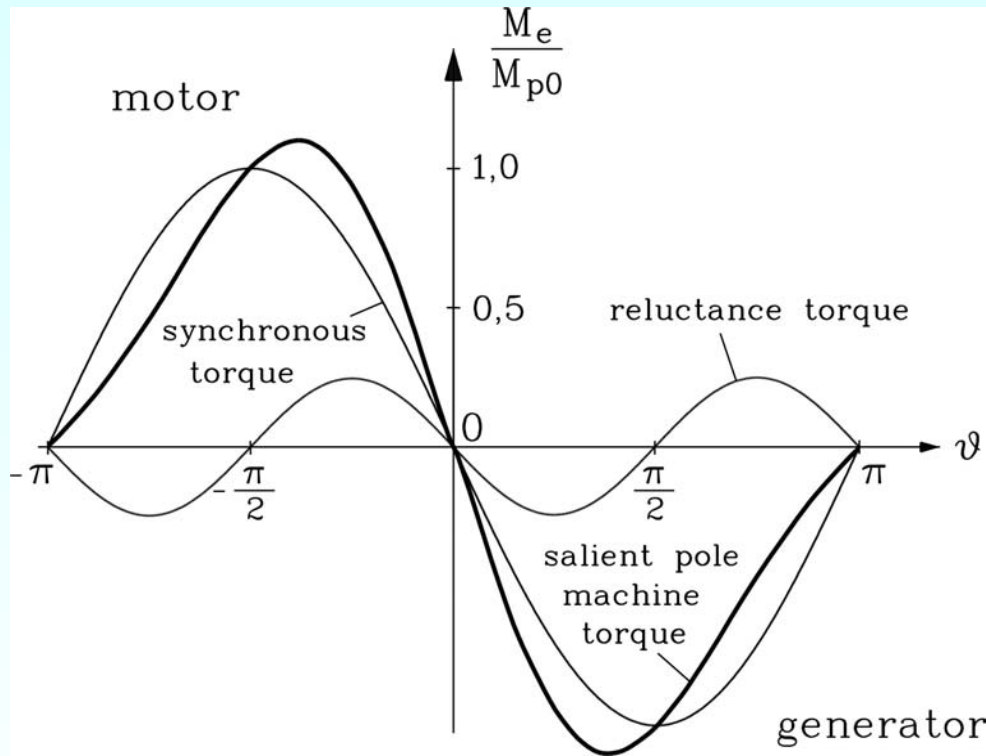
b) **"Reluctance" torque** due to $X_d \neq X_q$. NO rotor excitation is necessary!

Synchronous reluctance machine: Reluctance torque = robust rotor WITHOUT ANY winding, but DEEP inter-pole gaps.

Torque-load angle curve $M_e(\vartheta)$

- Torque is expressed by stator voltage, back EMF and load angle: I_{sd} , I_{sq} are expressed by U_s , ϑ :

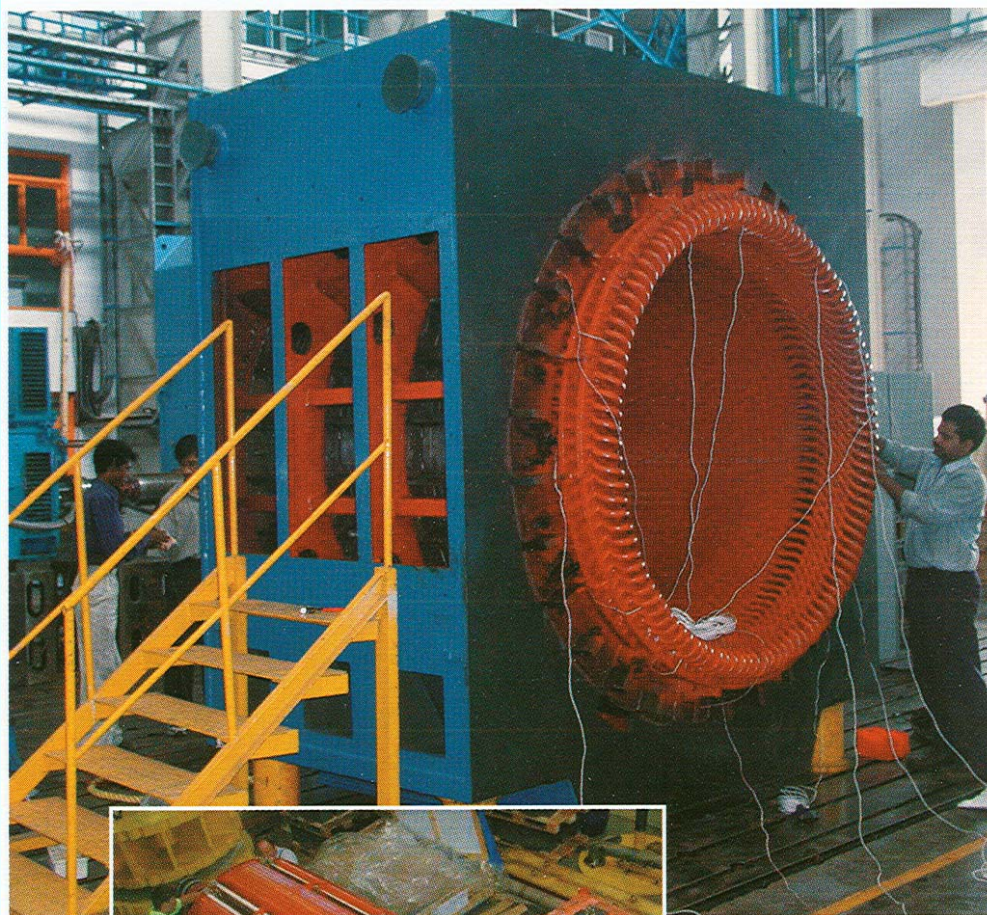
$$M_e = -\frac{p \cdot m_s}{\omega_s} \left(\frac{U_s U_p}{X_d} \sin \vartheta + \frac{U_s^2}{2} \left(\frac{1}{X_q} - \frac{1}{X_d} \right) \sin 2\vartheta \right)$$



Absolute value of pull-out load angle is $< 90^\circ$,
as pull-out torque of reluctance torque occurs at load angle $\pm 45^\circ$.

Pull-out torque is increased by reluctance torque.

Equivalent spring constant c_g
bigger than in round rotor machines,
as reluctance torque adds (“stiffer” $M_e(\vartheta)$ -curve).



Aseembling of salient pole synchronous generator (8 poles)

Stator with two layer high voltage winding for air cooling

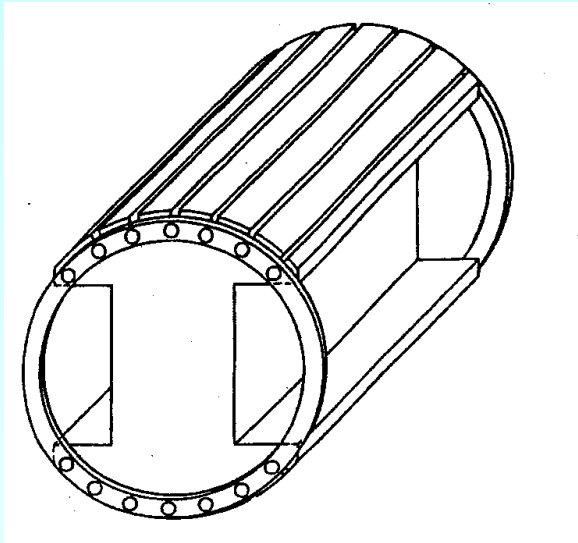


Rotor with shaft mounted fan and 8 rotor poles with damper cage

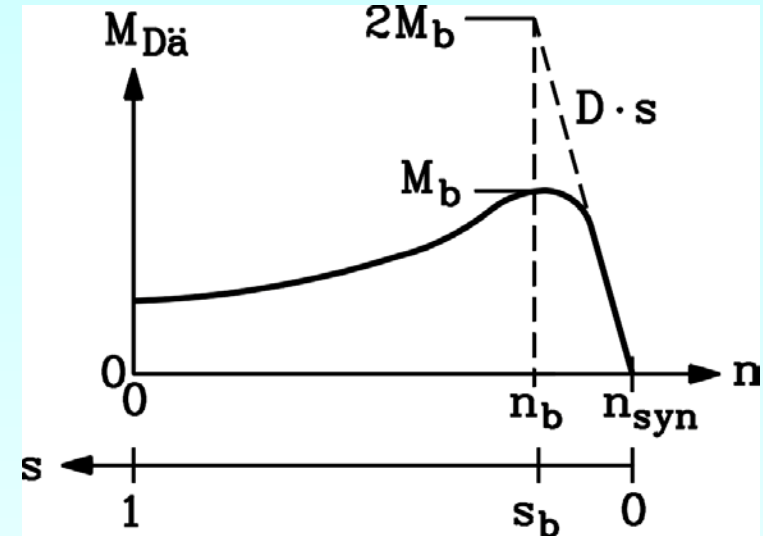
Source:

VATech Hydro,
Austria

Damper cage in synchronous machines



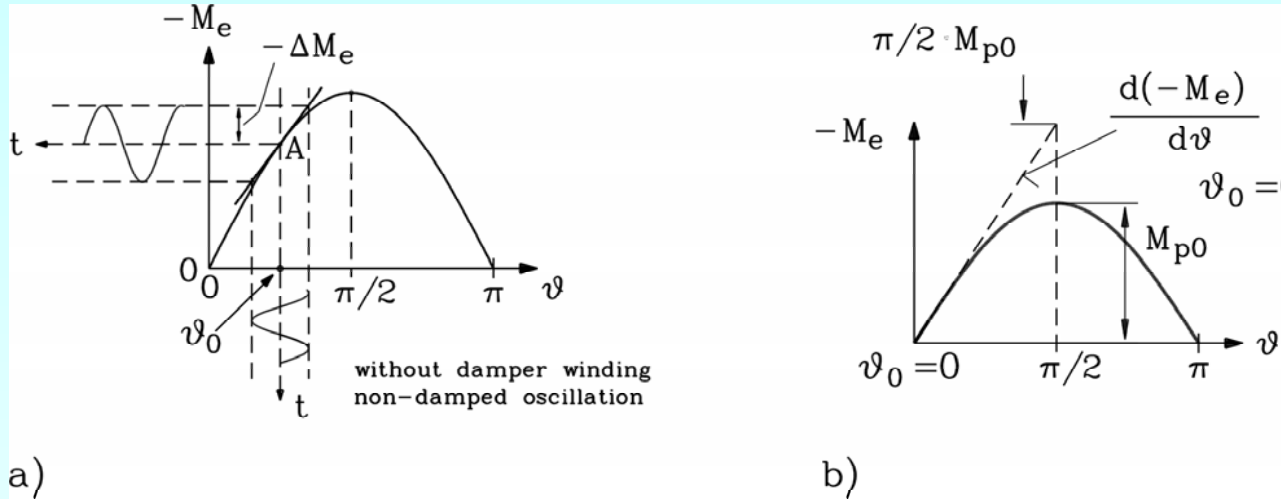
Damper cage of a 2-pole synchronous machine



Asynchronous torque of damper cage (KLOSS)

- Synchronous machines oscillate at each load step, when operating at “rigid” grid. The **damper cage** (= **squirrel cage** in rotor pole shoes) is damping these oscillations of load angle (and of speed) quickly.
- **Function of damper cage:** Speed oscillation leads to rotor slip s . $\Rightarrow$ So stator field induces damper cage. Cage current and stator field give **asynchronous torque** $M_{Dä}$, which tries to accelerate / decelerate rotor to slip zero = it damps the oscillatory movement. The kinetic energy of oscillation is dissipated as heat in the damper cage.
- For asynchronous starting, a **BIGGER starting cage** is needed due to big cage losses.

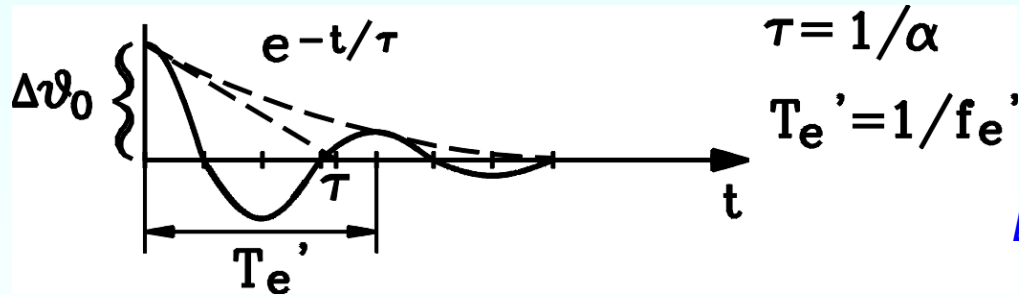
Damping of load angle oscillations



- Without damper cage: undamped oscillations at operation point: A ($-M_e$, ϑ_0):

$$f_e = \frac{1}{2\pi} \sqrt{\frac{p \cdot |c_g|}{J}}$$

- Damping asynchronous torque (KLOSS): (linearized) $M_D(s) \approx \frac{2M_b}{s_b} s = D \cdot s$



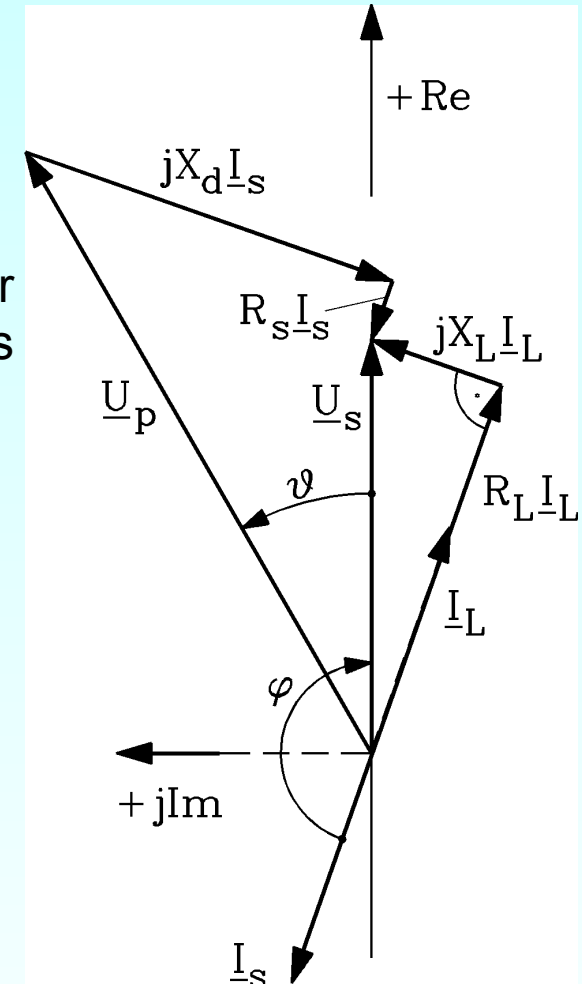
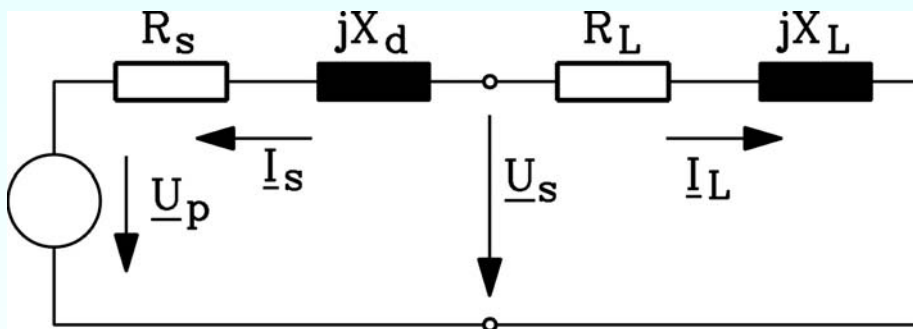
$$f_e' = \frac{\sqrt{(2\pi f_e)^2 - \alpha^2}}{2\pi}$$

E.g.: $\tau = 1/\alpha = 1/0.7 = 1.43s$

$$f_e' = \sqrt{(2\pi \cdot 1.093)^2 - 0.7^2} / (2\pi) = 1.087Hz$$

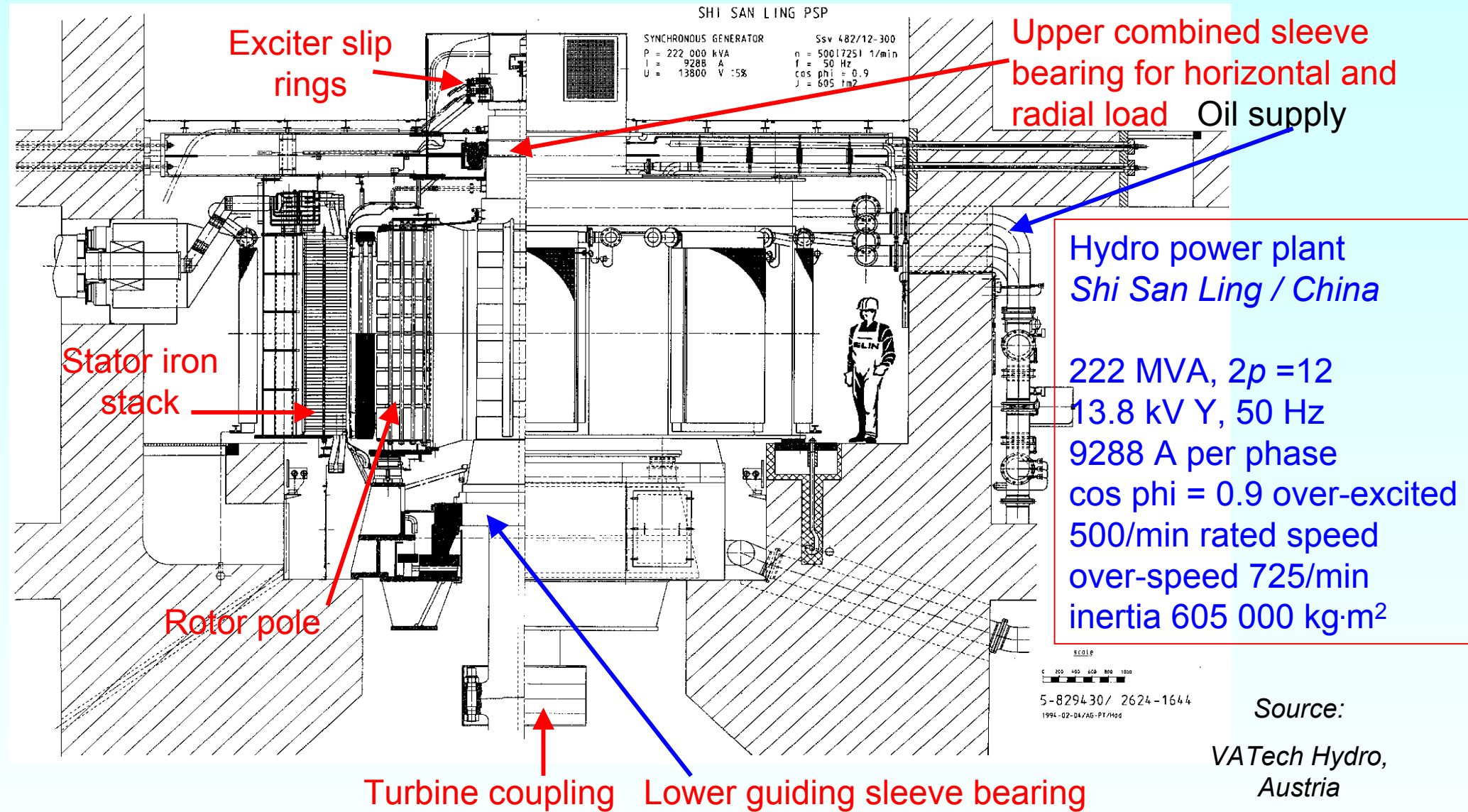
Synchronous machine in stand-alone operation

- Examples: Automotive generator, Air plane / ship generator, generator stations on islands, off-shore platforms, oasis, mountainous regions, emergency generators in hospitals, military use (e.g. radar supply)
- **No "rigid" grid available: U_s is NOT constant:** Rotor is excited and driven, field current I_f , back EMF U_p is induced as "voltage source", U_s is depending on load. E.g.: round rotor synchronous machine:
No $M_e \sim \sin \vartheta$ - curve,
No rotor pull out at $\vartheta = \pm 90^\circ$
- Example: Mixed OHM' ic-inductive load $\underline{Z}_L$ (Load current $\underline{I}_L = -\underline{I}_s$)

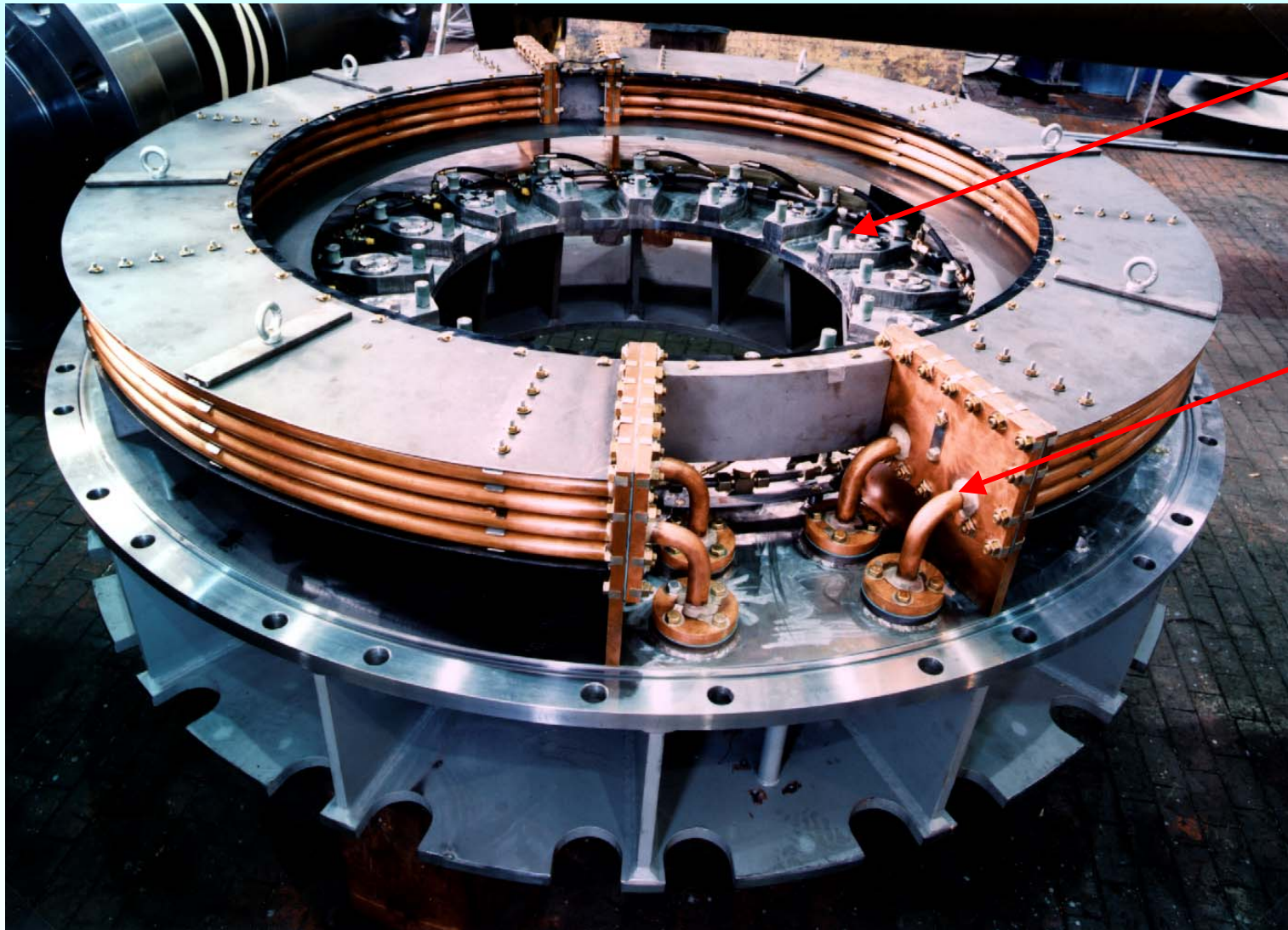


Load impedance: $\underline{Z}_L$ (here: $\underline{Z}_L = R_L + jX_L$)

Vertically mounted salient pole “big hydro” generator



Segment sleeve bearing for vertical load



Bolts for
bearing
segments

Oil supply
for
lubrication
and cooling

Source:

VATech Hydro,
Austria



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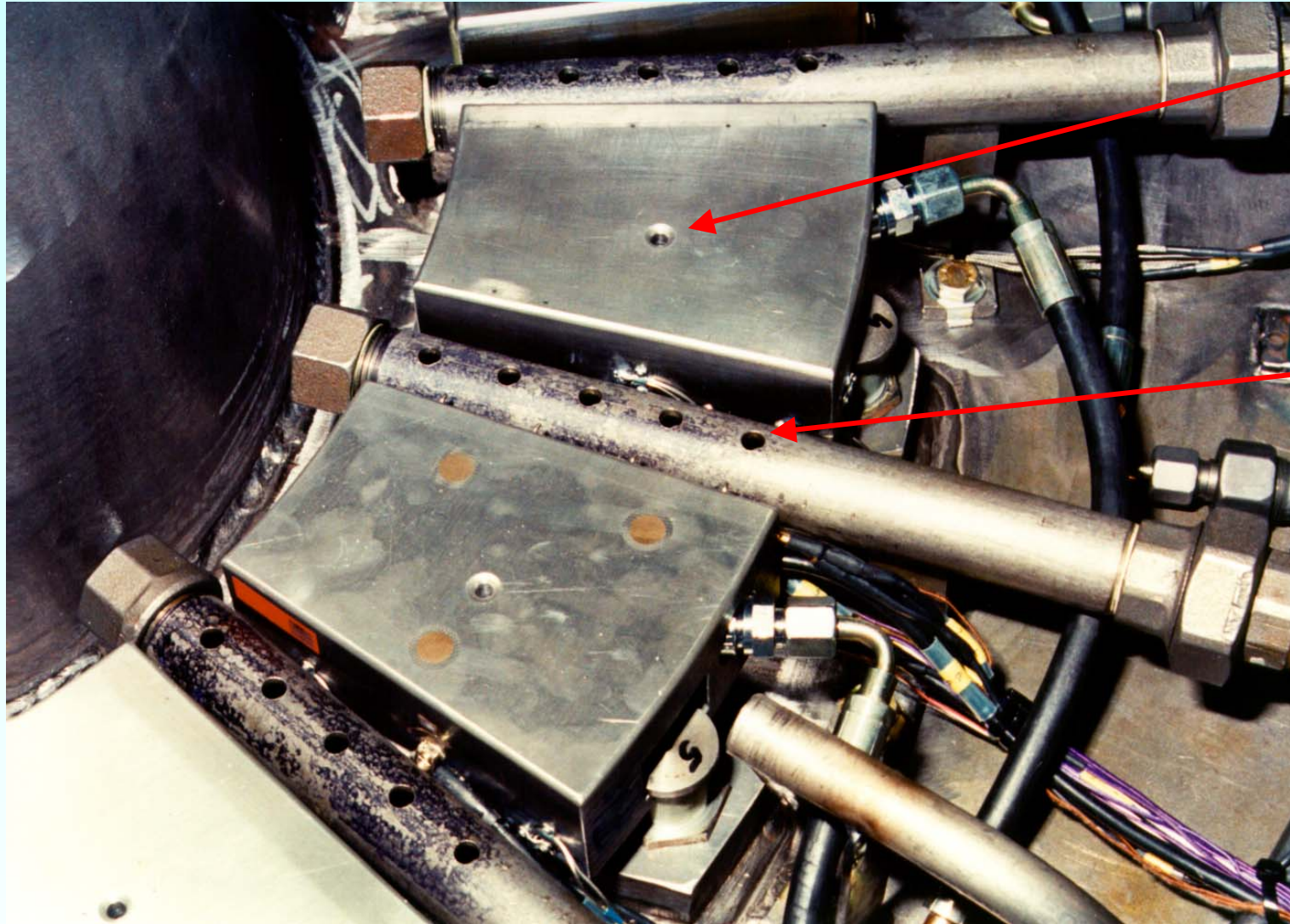
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CO-OPERATION OFFICE

Segment sleeve bearing for vertical load



Bearing segments for vertical load

Oil outlet for lubrication

Source:

VATech Hydro,
Austria



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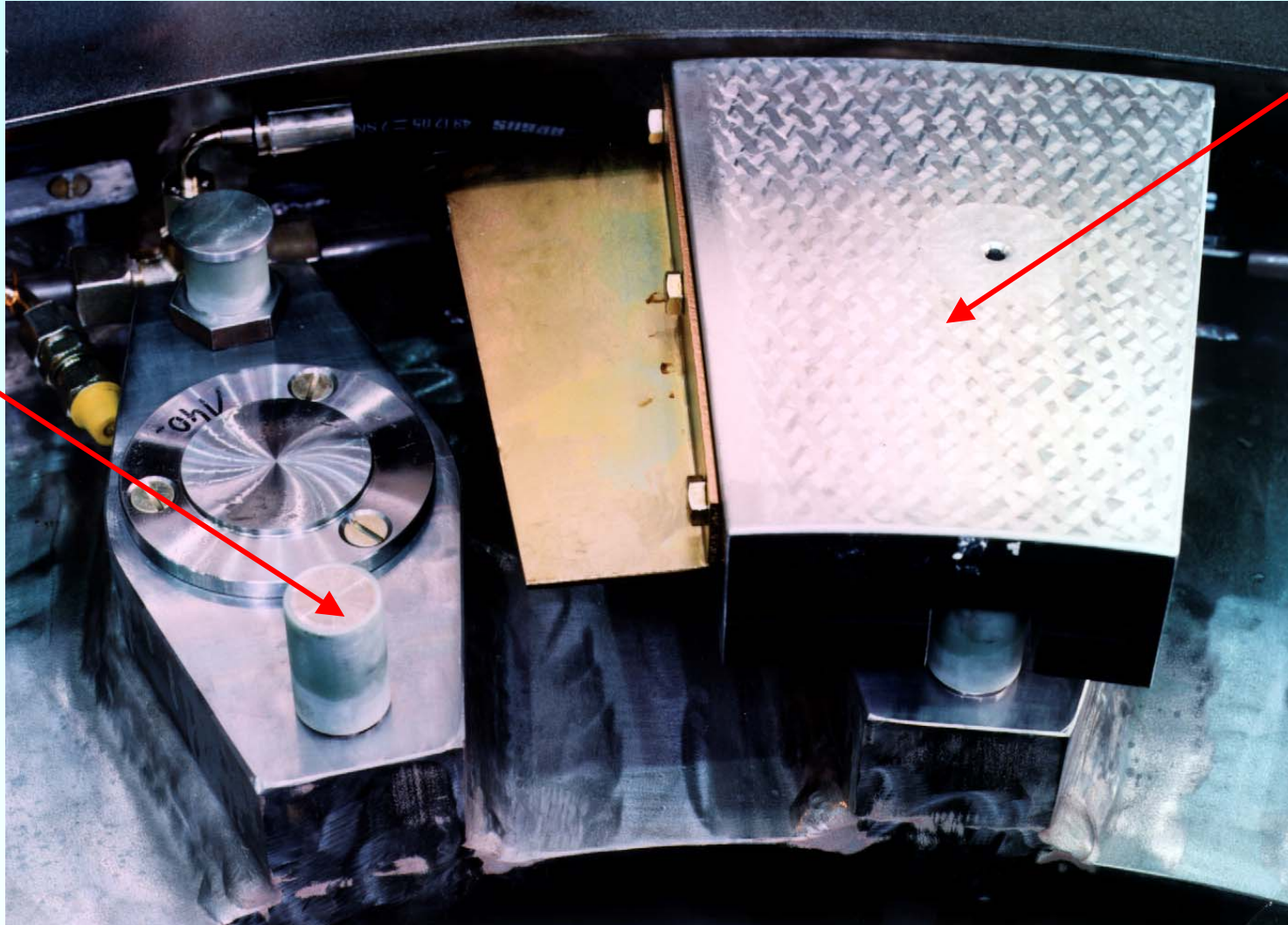


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Mounting of sleeve bearing segments for vertical load

Bolts for
segments



Bearing
segments
for vertical
load

Source:
VATech Hydro,
Austria



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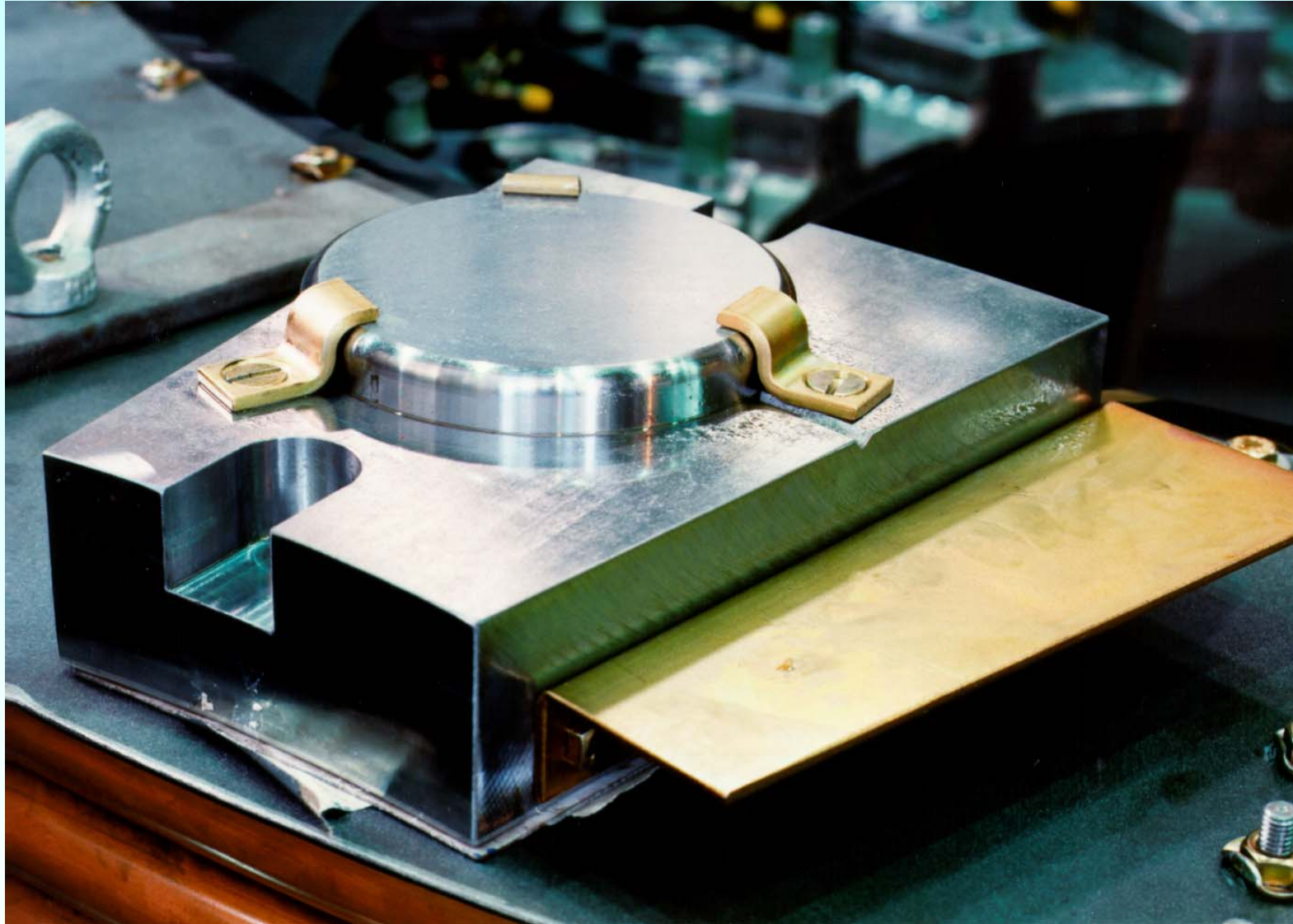
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Detailed view of bearing segments for vertical load



Source:
VATech Hydro,
Austria



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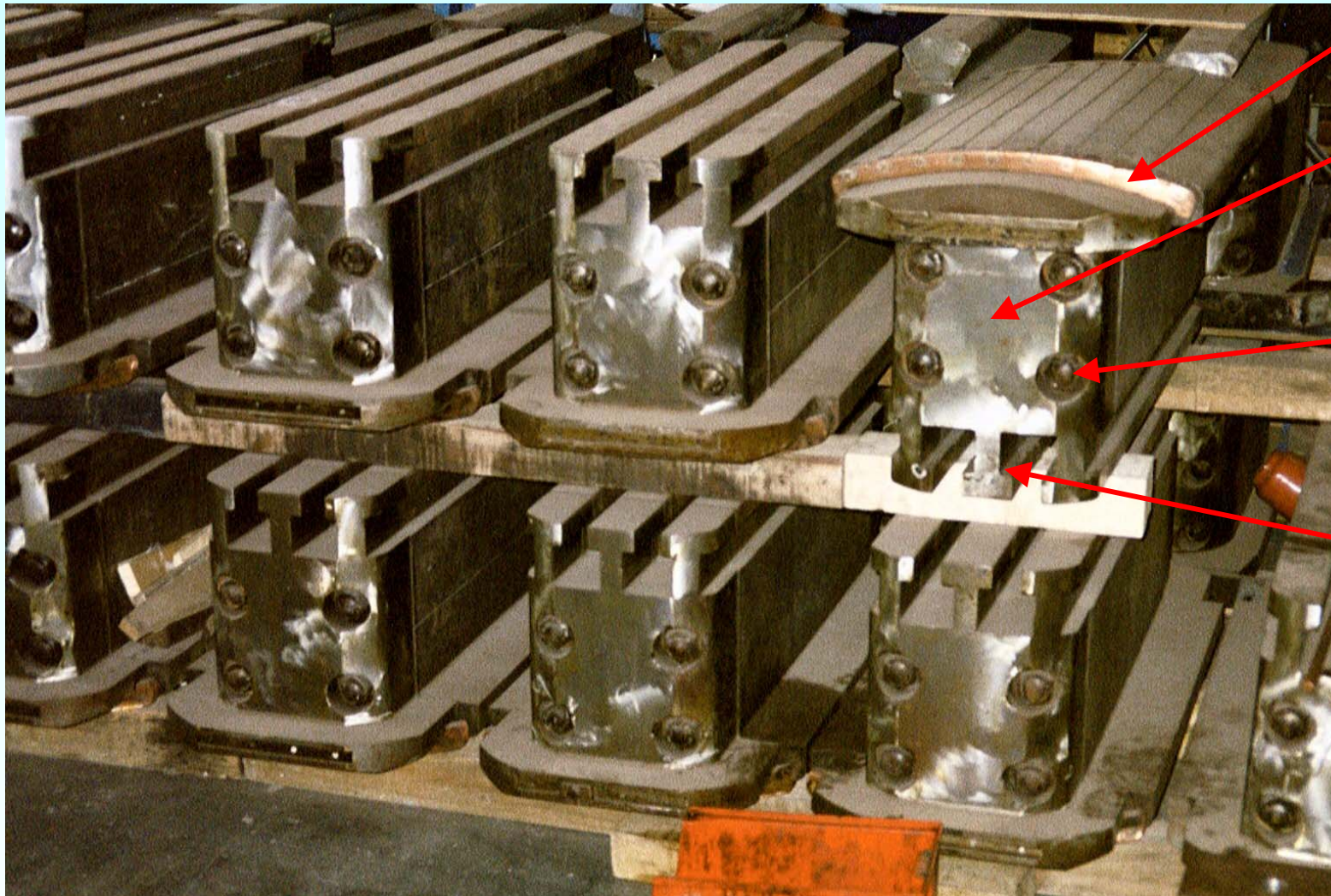
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Fixation of rotor poles for high centrifugal forces (e.g. pump storage plants)



Damper ring segment

pole press plate

pole joint bolts

three-fold hammer head fixation

Source:

VATech Hydro,
Austria



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Manufacturing of field winding for salient pole machines

Non-insulated flat copper winding provides good heat transfer to cooling air at front sides

Inter-turn insulation

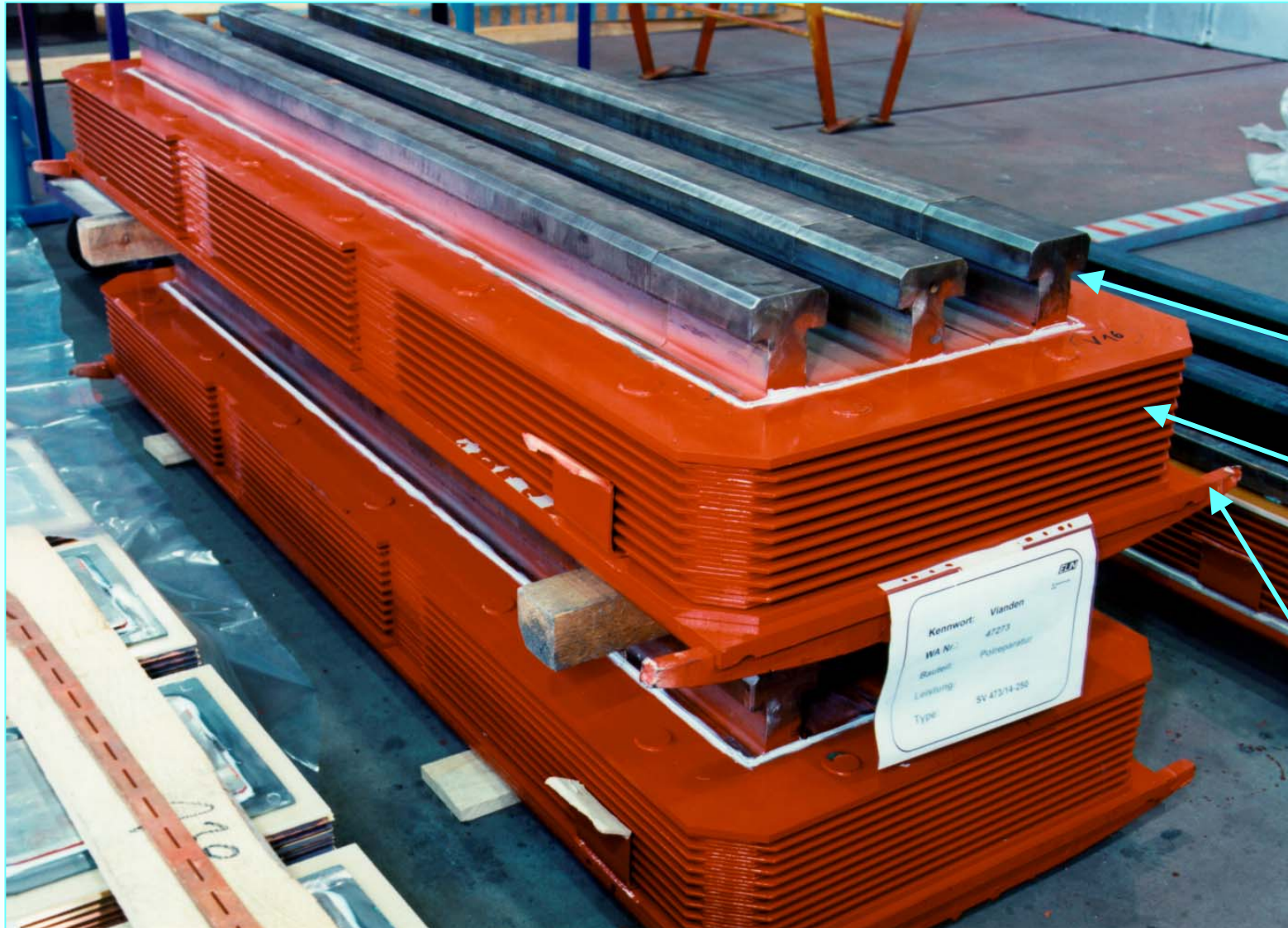
“Cooling fins” by increased copper width

Source:

VATech Hydro,
Austria



Completed salient pole before mounting



Pump storage
hydro power plant
Vianden/Belgium

Refurbishment

Three-fold hammer
head fixation

“Cooling fins” by
increased copper
width

Damper ring
segments

Source:

*VATech Hydro,
Austria*



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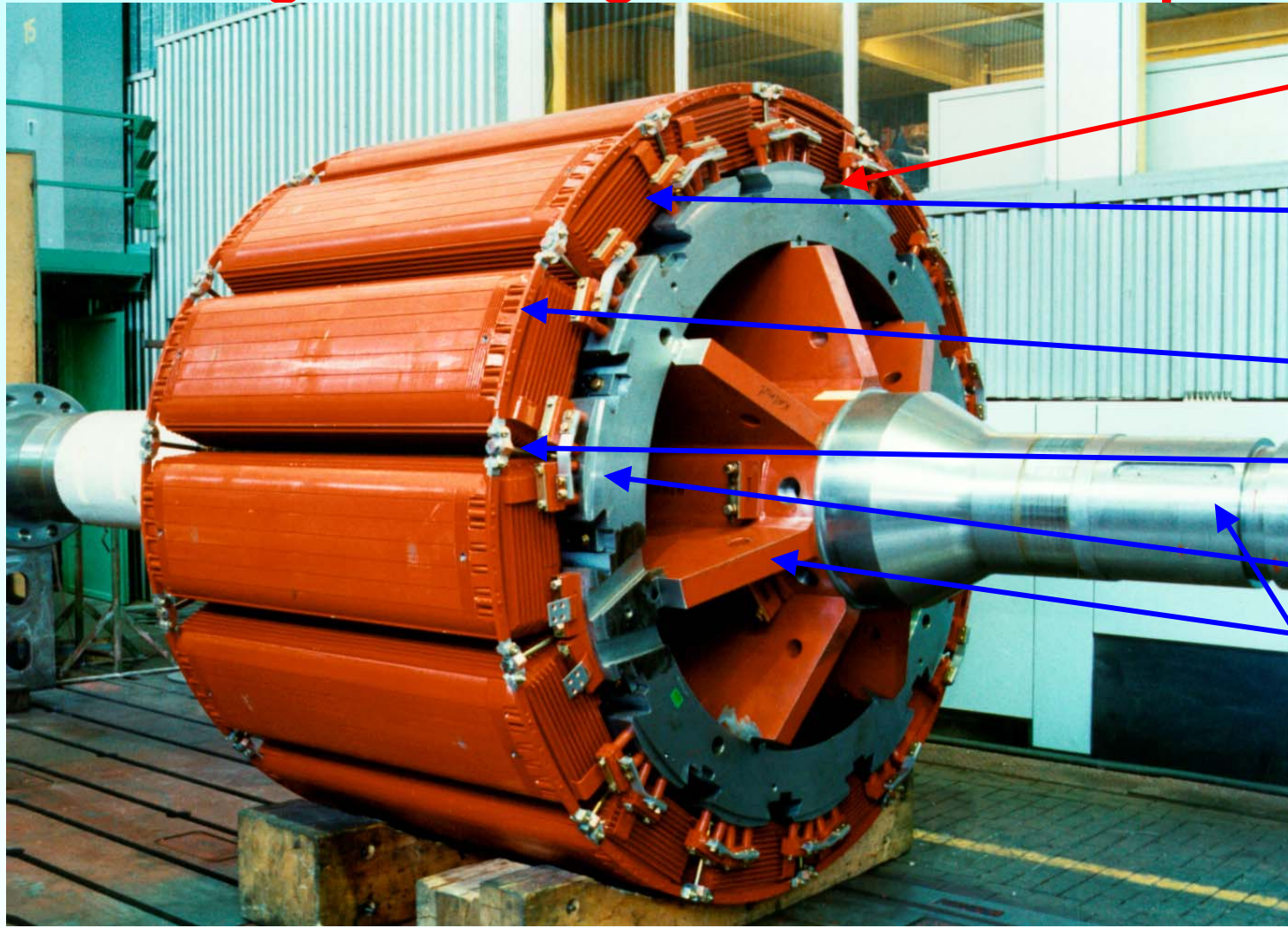


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Completed “big hydro” salient pole synchronous rotor for high centrifugal force at over-speed, 14 poles



Dove tail fixation of rotor poles

“Cooling fins” by increased copper width

Damper ring

Damper retaining bolts

Rotor back iron

Rotor spider

Generator shaft

Source:

VATech Hydro,
Austria

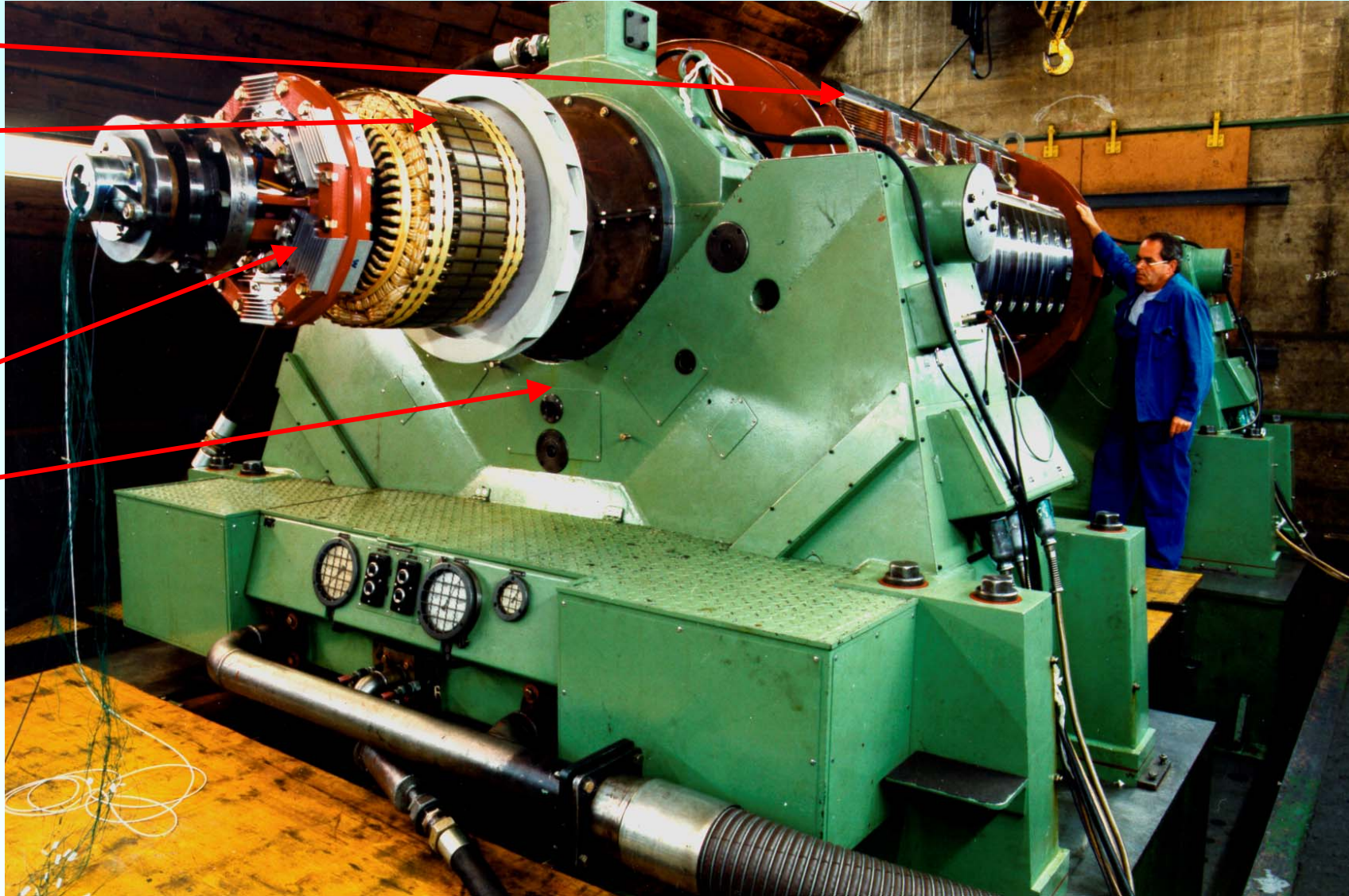
Balancing & over-speed test of salient 4 pole rotor in test tunnel

4 pole rotor

Exciter
generator 3-
phase winding

Rotating diode
rectifier

Balancing
bearing
(Schenck
Company,
Darmstadt)



Source:

VATech Hydro,
Austria



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Ring synchronous generator with high pole count for river hydro power plant (bulb type generators)

Rotor with spider, rotor poles with field winding and damper cage

At plant site
Freudenau/Vienna, Austria

River *Danube*

Mounting of rotor to turbine shaft



32 MVA, 50 Hz
92 poles
rotor diameter 7.45 m
rated speed 65.2/min
over-speed 219/min

circumference velocity at over-speed:

$$v_{u,max} = 85 \text{ m/s}$$

centrifugal acceleration at over-speed: $a/g = 200$

Source:

VATech Hydro, Austria



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Rotor spider during milling before mounting of rotor yoke



Manufacturing of
bulb type hydro
generator for
Freudenau power
plant

Source:

*VATech Hydro,
Austria*



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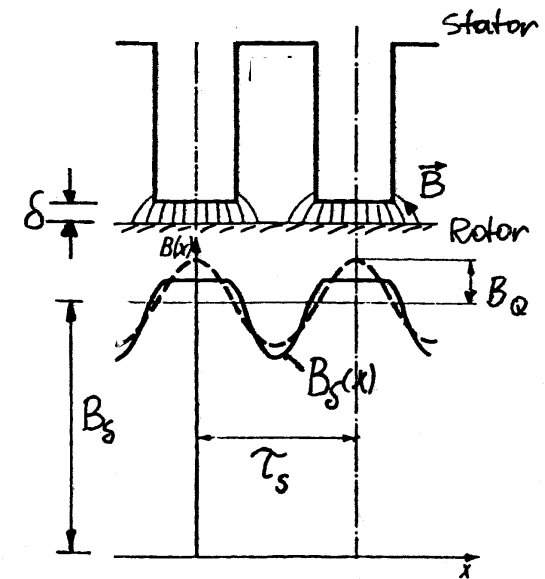


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A photograph showing five curved metal test specimens, labeled 30 through 34, arranged in a row on a red-painted metal surface. The specimens are made of a light-colored metal, possibly aluminum, and have a curved, channel-like shape. Each specimen has several small circular features along its length. A red arrow points to the top surface of specimen 32.

Slots for damper bars



Source: VA Tech Hydro, Austria

Massive rotor pole shaft welded to laminated pole shoes



Source:
VATech Hydro,
Austria



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Drilling holes into massive pole shaft to fix them to rotor yoke ring with screws



Welding machine

Welding of massive pole shaft o laminated pole shoes

Source:

VATech Hydro,
Austria



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